



ISTITUTO NAZIONALE DI RICERCA METROLOGICA Repository Istituzionale

Interplay between powder catchment efficiency and layer height in self-stabilized laser metal deposition

This is the author's accepted version of the contribution published as:

Original

Interplay between powder catchment efficiency and layer height in self-stabilized laser metal deposition / Donadello, Simone.; Furlan, Valentina.; Demir, Ali Gökhan; Previtali, Barbara. - In: OPTICS AND LASERS IN ENGINEERING. - ISSN 0143-8166. - 149:(2022), p. 106817. [10.1016/j.optlaseng.2021.106817]

Availability:

This version is available at: 11696/73255 since: 2022-07-04T07:10:14Z

Publisher:

ELSEVIER SCI LTD

Published

DOI:10.1016/j.optlaseng.2021.106817

Terms of use:

This article is made available under terms and conditions as specified in the corresponding bibliographic description in the repository

Publisher copyright

(Article begins on next page)

Interplay between powder catchment efficiency and layer height in self-stabilized laser metal deposition

Simone Donadello^{a,b}, Valentina Furlan^{a,*}, Ali Gökhan Demir^a, Barbara Previtali^a

^a*Department of Mechanical Engineering, Politecnico di Milano, Via La Masa 1, 20156 Milan, Italy*

^b*Istituto Nazionale di Ricerca Metrologica, INRIM, Strada delle Cacce 91, 10135 Turin, Italy*

Abstract

In laser metal deposition (LMD) the height of the deposited track can vary within and between layers, causing significant deviations during the process evolution. Previous works have shown that in certain conditions a self-stabilizing mechanism occurs, maintaining a regular height growth and a constant standoff distance between the part and the deposition nozzle. Here we analyze the link between the powder catchment efficiency and the deposition height stability. To this purpose, a monitoring system was developed to study the deposition in different process conditions, using inline measurements of the specimen weight in combination with the layer height information obtained with coaxial optical triangulation. An analytical model was used to estimate the deposition efficiency in real-time from the height monitoring and the process parameters, which was verified by the direct mass measurements. The results show that the track height stabilization is associated to a reduction of the powder catchment efficiency, which is governed by the melt pool relative position with respect to the powder cone and the laser beam. For a given set of parameters, the standoff distance can be estimated to achieve the highest powder catchment efficiency and a regular height through the build direction.

Keywords: laser metal deposition; additive manufacturing; process monitoring; deposition efficiency; process stability; optical metrology

1. Introduction

Laser metal deposition (LMD) is an additive manufacturing (AM) process belonging to the directed energy deposition (DED) family [1]. In the conventional LMD implementation, a laser beam creates a melt pool that captures the coaxial powder stream which is blown to the deposition region, generating the deposition tracks. Complex and large parts with variable slicing axis can be made by the consecutive deposition of adjacent tracks and layers [2, 3]. LMD is also capable to produce parts with multi-material deposition [4], build features on existing components, and repair damaged parts [5]. Despite these several advantages, the LMD process is still not widely applied on an industrial scale. Some of the key issues limiting its industrial application are the limited geometrical stability and the requirement of post-processing [6]. In LMD the deposited track dimensions vary as a function of the process parameters, but can also depend on the deposition trajectory and part geometry. While, for instance, in laser powder bed fusion the layer height relies on the powder bed lowering, in LMD the deposition track height can vary with the same set of parameters and material due to the thermal history of the process.

In industrial practice, the LMD process parameters are set for achieving mainly pore and crack free deposits [7]. However, when these parameters are used for generating complex geometries, they can often fail to respect the required geometrical tolerances [8]. Such kind of problem may rise from heat accumulation

*Corresponding author

Published version: doi.org/10.1016/j.optlaseng.2021.106817

during the process in acute corners or the decrease of the scanned section area, where the deposit height can increase compared to the nominal one. Inversely, the process may derive to a colder stage with long deposition tracks: in this case, the deposit height can be lower than expected and the part may fail to grow. One aspect which is directly correlated to the laser parameters is the cooling rate. For example, a change in the parameter set can increase the temperature gradient between the deposition site and the substrate. Since the main cooling mechanism in this technology is conduction, a higher thermal gradient involves a higher cooling rate. This can translate in a different temperature profile along the deposited layers over the substrate [9]. Indeed temperature can influence the deposition growth. At the initial layers the deposition is carried out close to the substrate, which behaves as a heat sink with a lower initial temperature [10]. As the deposition proceeds over the layers, the conduction behavior changes due to the heat buildup, which also may affect the material microstructure, as well as the porosity formation and the layer thickness uniformity.

Thermal effects can be mitigated by choosing the optimal set of process parameters from preliminary experimental campaigns or numerical simulations [11]. While this approach is effective in resolving bigger issues such as part failure, offline optimization can be time-consuming and does not allow the system to autonomously operate: the actual process fluctuations related to the powder-laser interaction remain uncontrolled, leading to unrepeatability results. Therefore industrial LMD systems can operate with closed-loop controllers, commonly relying on coaxial pyrometers [12], digital cameras [13], or composite systems [14]. These devices aim to maintain a required process temperature and stable deposition conditions. However they require careful calibration methods, which can also differ from bulky to thin structures. Other inline monitoring devices such as optical triangulation [15] or low-coherence interferometry [16] have been also proposed for a direct measurement of the deposit height, which can be compensated by the machine axis movement. Despite several achievements to control these changes in the deposited track height, more attention is required for developing a fundamental understanding of the process physics.

The material deposition stability is strictly related to the capacity of the process to maintain the rate of powder being fused. For instance, the LDM process is characterized by higher resolution but lower deposition efficiency if compared to its counterpart that uses wire feedstock, the laser metal wire deposition [17]. In particular, powder catchment efficiency is a key parameter that defines the amount of material being deposited in comparison with the amount being released to the deposition area. This relies on the interplay between powder jet, laser beam, and laser process parameters, which determine the deposition track geometry [18]. Powder catchment efficiency has been one of the earliest research questions of LMD [19]. The main importance has been given to the material usage, as the main aim has been to identify the conditions for an environmentally and economically viable process [20]. For more expensive alloys, such as Ti- and Ni-alloys, the material cost can become a significant fraction of the overall operation costs in LMD based production. The optimization of the laser-powder interaction enables new high-speed deposition technologies [21]. Nonetheless, the powder catchment efficiency can be a key element for understanding the deposition stability. Recently a method for the powder flow measurement by a precision scale has been demonstrated and correlated to the actual deposition efficiency measured from single tracks [22]. On the other hand, to the authors' knowledge no previous work attempted to measure the powder catchment efficiency in real time on multiple-track and multiple-layer depositions.

The layer height in LMD is known to vary starting from the first deposition stages, since the initial layers are characterized by a certain kind of process instability [23]. This behavior is determined by layer growth rate variability given by the mismatch between deposition height and part design, which can move on a stable value during the deposition progress [24, 25]. Such self-regulation mechanism can be related to a change in the powder catchment efficiency during the deposition: this can eventually converge to a stationary regime, although generating transitory geometric inaccuracies [26]. Accordingly different works faced up to the influence of powder distribution and defocusing on height variability and deposition efficiency while building multi-layer parts [27, 28]. However an extensive study and modeling regarding the interplay between deposition growth and powder catchment efficiency is still required for a full comprehension of deposition stabilization and optimization. This way, the phenomena behind the geometrical deviations, especially in the deposition height, can be revealed and compensated throughout the process evolution.

This work presents an innovative approach to study the powder catchment efficiency in LMD for multi-track multi-layer parts in real-time. The role of deposition height in the mechanism of passive process

stabilization was investigated. An analytical model was developed to link the powder catchment efficiency to the deposition height growth and to the main process parameters. An inline experimental setup was developed to measure the mass increase of the deposit during the process. The deposition height was simultaneously measured via coaxial optical triangulation. Different process conditions were considered for the deposition of AISI 316L cubic samples using a LMD setup based on a three-jet nozzle and a multimode fiber laser. The measurements obtained from the multiple instruments were used in a complementary way to identify the factors that influence the powder catchment efficiency. The results clearly indicated that self-regulation is associated to the powder catchment efficiency reduction. In the future, the proposed model might be used to identify the optimal parameters in terms of both process stability and efficiency, and it can be functional for an active control of the deposition accuracy by means of dimensional optical monitoring.

Nomenclature	
η_m	powder catchment efficiency
η_m^*	effective powder catchment efficiency
η_{path}	deposition path coefficient for η_m
η_h	geometrical powder catchment efficiency
η_{th}	theoretical powder catchment efficiency
η_{en}	energetic coefficient for η_{th}
η_{int}	powder-laser interaction coefficient for η_{th}
\dot{m}_{dep}	deposition mass rate
\dot{m}_{tot}	total delivered powder mass flow rate
Δt_{dep}	total deposition time interval
Δt_{proc}	processing interval during Δt_{dep}
A_{cs}	single track cross-section area
\bar{h}	average layer height
h_{th}	theoretical layer height
S	standoff distance
S_0	reference standoff distance
S_{th}	theoretical standoff distance
r_x, r_z	robot path transverse and height increments
Δh	height mismatch between \bar{h} and r_z
v	transverse scanning speed
P	processing laser power
P_0	critical power for powder melting
ρ	solid material density
C_p	solid material specific heat capacity
\mathcal{L}	material fusion latent heat
\mathcal{A}	material optical absorptance
T_m	material melting point
ΔT	temperature increase during deposition
A_p	powder spot area
A_{int}	laser-powder interaction area
d_{p0}, x_{p0}	diameter and radial distance of powder orifices
x_{p1}, z_{p1}	extrapolated coordinates of powder cone apex
α_p, β_p	half-divergence and inclination of powder jets
x_p, x_l	coordinates of powder and laser spot borders
c_g	geometrical correction factor to x_l
w_{l0}, θ_l	laser beam waist radius and half-divergence
z_{l0}	laser focus axial coordinate

2. Model

In the following sections the deposition efficiency will be discussed from different point of views. Section 2.1 provides a general definition of the powder catchment efficiency in terms of the deposited mass. In section 2.2 a model for the layer height provides an alternative definition of powder catchment efficiency from geometrical considerations. Finally, section 2.3 presents a semi-empirical model for the interpretation of the deposition process stability, where the powder catchment efficiency is expressed as a function of the process parameters and of the standoff distance. Such theoretical background links the self-stabilization mechanisms in the deposition height growth to the powder catchment efficiency variability, determined by the variable interaction between the powder and laser beams.

2.1. Definition of powder catchment efficiency

The powder catchment efficiency η_m is defined as the ratio between the deposition mass rate \dot{m}_{dep} , i.e. the increase of the deposit mass in a given time interval, and the total mass flow rate \dot{m}_{tot} of the metallic powder which gets delivered during the deposition:

$$\eta_m = \frac{\dot{m}_{dep}}{\dot{m}_{tot}}. \quad (1)$$

The total powder flow \dot{m}_{tot} includes losses caused by inefficiency in the process of powder catchment, thus $\eta_m < 1$.

A direct estimation of η_m can be obtained by measuring the mass Δm_{dep} deposited during a finite time interval Δt_{dep} , e.g. the interval for the deposition of a layer. The average efficiency over the corresponding interval is therefore

$$\bar{\eta}_m = \frac{\Delta \bar{m}_{dep}}{\Delta t_{dep} \dot{m}_{tot}}. \quad (2)$$

The deposition procedure for non-trivial geometries can include intervals where the deposition is suspended. For example, in robotized systems, the laser emission can be disabled during the position settlement of the deposition head between different tracks or layers. Conversely the powder feed is typically kept constant in order to maintain a stationary flow. Of course the powder which gets delivered when the processing laser is not emitting cannot be deposited and gets lost. Indeed the average powder catchment efficiency defined in Eq. (2) includes an implicit coefficient η_{path} that is not related to the process itself, but which is set by the chosen deposition path strategy. This can be expressed as the ratio between the actual processing time Δt_{proc} over the total deposition time interval Δt_{dep} :

$$\bar{\eta}_{path} = \frac{\Delta t_{proc}}{\Delta t_{dep}}. \quad (3)$$

Therefore, in real-world measurements, the average efficiency $\bar{\eta}_m$ must be normalized to $\bar{\eta}_{path}$ to eliminate the dependence on the specific deposition strategy, hence introducing the effective powder catchment efficiency $\bar{\eta}_m^*$ related only to the process physics and defined as

$$\bar{\eta}_m^* = \frac{\bar{\eta}_m}{\bar{\eta}_{path}}. \quad (4)$$

2.2. Calculation of efficiency from deposition layer height

The powder catchment efficiency can be defined also from geometrical considerations. Assuming the absence of porosity, the deposition mass rate is related to the cross-section area A_{cs} of a single deposition track as

$$\dot{m}_{dep} = A_{cs} v \rho, \quad (5)$$

with v being the transverse scanning speed and ρ the bulk material density.

We consider the deposition of a simple prismatic geometry composed of multiple tracks and multiple layers, referred to as bulk deposition from hereon. Each layer is composed of several adjacent tracks separated by a path transverse increment r_x , which is assumed constant in the current discussion. In common practice each track partially overlaps with the previous one: this translates in an actual height growth excess, and inclined tracks are typically observed in multi-track LMD [29–31]. The general experimental evidence is characterized by an initial transient in the track shape, which converges to a stationary regime within few adjacent tracks. From purely geometrical considerations, discussed in the Supplementary Material, the average contribution given by each track to the deposition layer is equivalent to a rectangular cross-section, whose dimensions are approximated by the path transverse increment r_x and by the average layer height \bar{h} as represented in Figure 1(a):

$$\bar{A}_{cs} \simeq r_x \bar{h}. \quad (6)$$

It follows that the powder catchment efficiency can be calculated in terms of geometrical parameters by inserting Eq. (5) into the general definition of Eq. (1), and taking the average cross-section area of Eq. (6) over a multi-track layer. Therefore, if the deposition parameters r_x , \dot{m}_{tot} and v are fixed, and if the deposition process is stationary within each layer, $\bar{\eta}_h$ depends only on the average layer height \bar{h} :

$$\bar{\eta}_h \simeq \bar{h} \frac{r_x v \rho}{\dot{m}_{tot}}. \quad (7)$$

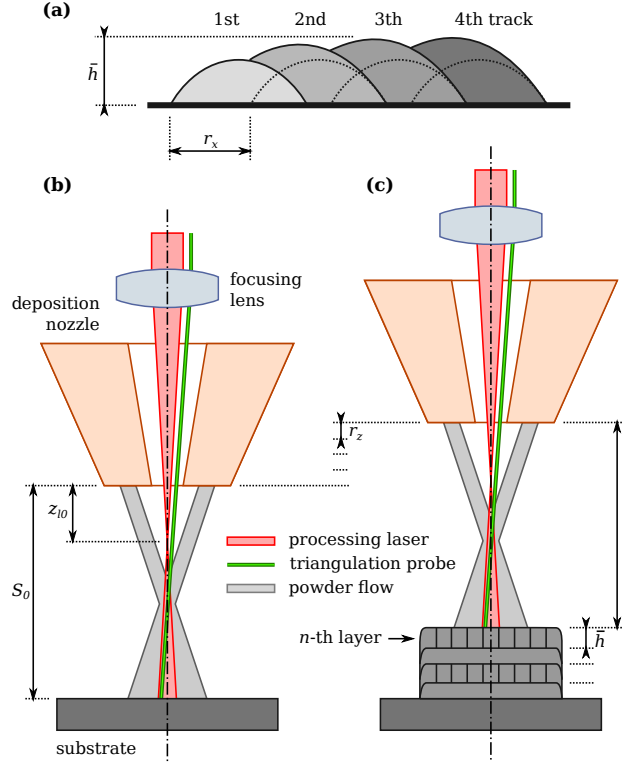


Figure 1: (a) Cross-section representation of partially overlapping deposition tracks. (b-c) Schematic representation related to the multi-layer deposition height, in the initial condition and after the deposition of some layers.

It is important to highlight that the geometrical definition of $\bar{\eta}_h$ is equivalent to the general one of $\bar{\eta}_m^*$ given in Eq. (4): they provide different ways to estimate the average powder catchment efficiency, respectively from dimensional and weight measurements. In particular, since $\bar{\eta}_h$ in bulk depositions is determined by the layer height \bar{h} , the study of powder catchment efficiency can be performed using a displacement sensor which measures the standoff distance S , defined as the distance between the deposition nozzle tip and the deposition surface. Accordingly \bar{h} can be extracted differentiating S , as shown in the Supplementary Material.

2.3. Model for efficiency and height self-regulation

Considering a LMD system based on a robotized deposition head, during a multi-layer deposition the robot height is incremented by r_z for each layer, as represented in Figure 1(b-c). In an open-loop approach r_z is kept constant. For an ideal process growth, such robot height increment should match the deposited layer height \bar{h} to keep a constant standoff distance. However this condition is unlikely satisfied in real-world cases: a height mismatch $\Delta h = \bar{h} - r_z \neq 0$ is typically present if the process parameters are not carefully modeled or controlled. Moreover Δh can change during the deposition due to the intrinsic process efficiency

variability. A positive height mismatch $\Delta h > 0$ corresponds to a growth which is faster than the robot movement along the build direction, and leads to a lower standoff distance; on the contrary, a negative mismatch $\Delta h < 0$ leads to a greater standoff distance, hence to a departure of the deposition area from its initial relative position.

A monotone mismatch $\Delta h \neq 0$ would cause a standoff distance divergence, eventually ending with a failure of the process itself when the deposition surface becomes too far or too close relatively to its optimal value. However, when the laser and powder beams are focused along the axial direction, variations in the standoff distance S are also associated to modifications in the process conditions related to laser intensity and powder flux on the deposition area [25]. In particular situations the presence of a non-zero gradient of Δh with S can lead to a stationary regime where $\Delta h = 0$. This corresponds to a transient which brings the process growth to match the robot movements, hence to maintain a steady standoff distance [26]. Process stabilization during the deposition of complex parts can be directly observed using inline optical monitoring [23]. In general this mechanism is favorable, because it reflects passive process robustness against perturbations, and because it corresponds to enhanced geometrical accuracy since the actual deposition process tends to match the design model.

The relation between deposition self-regulation and efficiency must be investigated in terms of energy and powder transverse distributions [22]. The current work considers the case study configuration where the focal points of the laser and powder beams lay between the powder nozzle tip and the initial substrate position. In this common condition the open-loop self-stabilizing regime can be observed after a transient to smaller standoff distance values, i.e. with a positive layer mismatch $\bar{h} > r_z$. Such initially faster growth can be interpreted as the result of an increasing substrate temperature that favors powder melting at the beginning, in combination with a powder flux abundance which allows to deposit the first layers with high efficiency. Substrate temperature stabilization occurs typically after few layers [29], thus the effects of energy and powder spatial distributions dominate on the subsequent deposition growth rate, once a stable thermal condition is reached. The initial values of standoff distance and layer height increment also play an important role in the dynamics of process stabilization [27]. It follows that the powder flux fraction available for catchment into the melt pool generated by the laser radiation changes while approaching the powder nozzle tip. This can introduce a powder catchment efficiency reduction, corresponding to a braking-like effect for the deposition growth, as a natural feedback mechanism which leads to a stationary regime where $\bar{h} = r_z$.

Several approaches can be followed for modeling the deposition height in terms of laser-powder interaction [32–34]. We propose a semi-empirical model for a quantitative interpretation of the process self-regulation, extending the results reported in other works [9]. Accordingly the powder catchment efficiency will be derived with an explicit dependence on the standoff distance S and on the process parameters, assuming a stationary deposition for bulk geometries.

Here the theoretical powder catchment efficiency η_{th} is defined as the product of two coefficients, one related to energetic factors η_{en} , the other depending on the powder-laser spatial interaction η_{int} :

$$\eta_{th} = \eta_{en}\eta_{int}. \quad (8)$$

The laser-powder interaction is assumed to happen only within an area A_{int} , corresponding to the intersection between the respective beams on the deposition surface. This determines the effective powder mass rate that can be captured in the melt pool generated by the laser radiation. The approximation of uniform powder mass flux and laser intensity over the respective spot areas is introduced for simplicity. Therefore, if the powder flux is distributed over an area $A_p \leq A_{int}$, the spatial interaction coefficient is

$$\eta_{int} = \frac{A_{int}}{A_p}. \quad (9)$$

From an energetic point of view, efficiency is typically observed to grow while increasing the laser power, until a saturation condition is reached, with an effect on the substrate dilution phenomenon [35, 36]. Accordingly, here η_{en} is modeled as the fraction of powder flux which can be melt by the energy provided over the interaction area A_{int} . Specifically η_{en} corresponds to the ratio between the laser power P and

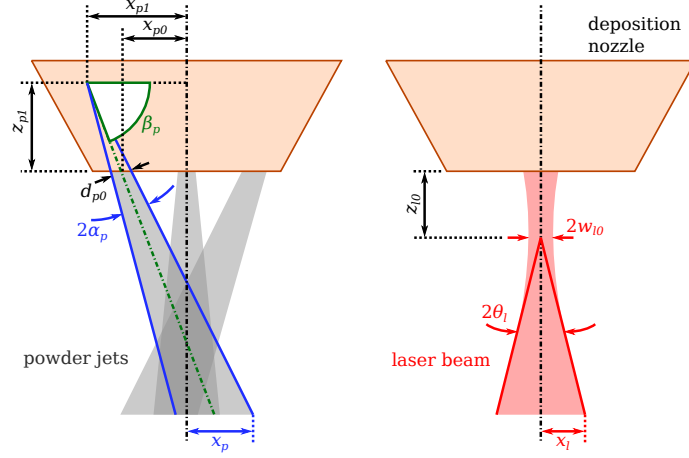


Figure 2: Side-view representation of the powder nozzle, with the main dimensions related to the 3 powder jets and to the laser beam.

the critical power P_0 , the latter representing the minimum energy rate that would be required to fuse the incoming powder flow rate. Since both P and P_0 should be normalized to A_{int} , η_{en} does not depend on the spatial interaction, which characterizes the term η_{int} . A conservative estimation of the critical power P_0 can be obtained neglecting the energy required for the substrate melting during the fusion bond with the powder particles: this contribute is small in the assumption that the substrate is in a stationary thermal condition after being preheated by the previous deposition layers, and that only a thin surface layer gets melted, hence with a reduced substrate dilution. Therefore:

$$P_0 = \dot{m}_{tot} \frac{\mathcal{C}_p \Delta T + \mathcal{L}}{\mathcal{A}}, \quad (10)$$

where \mathcal{C}_p is the material specific heat, $\Delta T = T_m - T_0$ is the excursion between room temperature T_0 and melt pool temperature T_m , \mathcal{L} is the fusion latent heat, and \mathcal{A} is the material optical absorptance. In usual conditions T_m can be roughly approximated with the material melting point. A gaussian sigmoid function is applied to P/P_0 to empirically express the energetic coefficient η_{en} :

$$\eta_{en} = 1 - \exp\left(-\frac{P}{P_0}\right). \quad (11)$$

This allows for a simplified phenomenological description of the efficiency saturation that is typically observed for $P \rightarrow P_0$. Such analytical representation is convenient in view of numerical calculations, since it exhibits a smooth connection between η_{en} in the linear scaling regime for $P \ll P_0$, while tending asymptotically to 1 for $P \gg P_0$. Moreover, for $P \sim P_0$, the corresponding value of η_{en} closely matches the efficiency calculated from the lumped heat capacity model in similar conditions [37]. It follows that the semi-empirical relation for the theoretical powder catchment efficiency becomes

$$\eta_{th} = \frac{A_{int}}{A_p} \left[1 - \exp\left(-\frac{PA}{\dot{m}_{tot}(\mathcal{C}_p \Delta T + \mathcal{L})}\right) \right]. \quad (12)$$

An approximated geometrical model for the powder distribution can be provided for the calculation of A_{int} and A_p , based on simple geometrical considerations for a specific deposition nozzle. Similar methods have been reported for the description of different configurations [38]. Here a three-jet nozzle is considered, composed of 3 powder streams arranged with axial symmetry at 120° , as represented in Figure 2. The jets are tilted to form a hollow cone-like powder stream, coaxial to a focused laser beam passing along the nozzle axis. A_p can be calculated as a function of the standoff distance S knowing the divergence angle $2\alpha_p$ of the

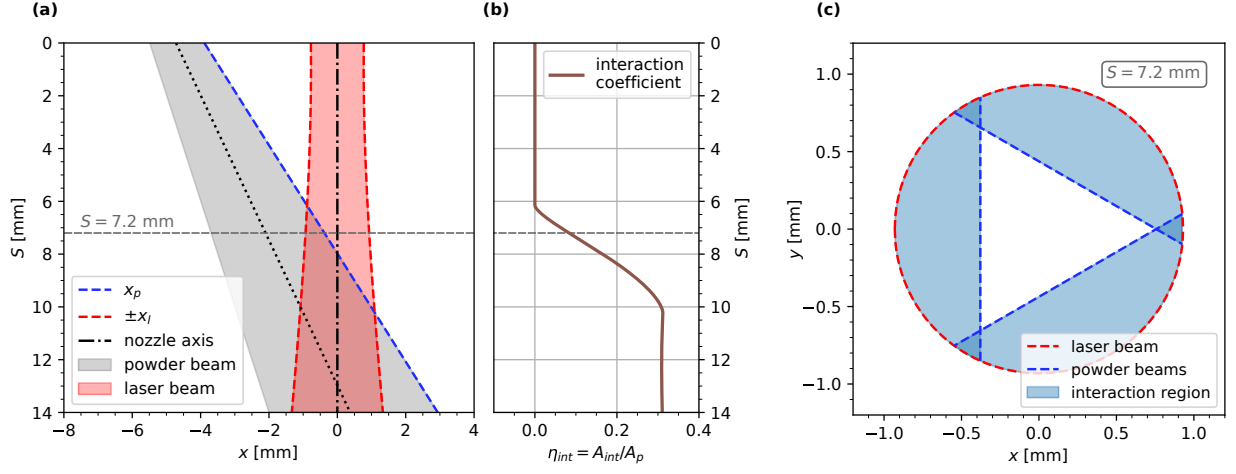


Figure 3: (a) Quantitative representation of the coaxial laser beam and one of the powder beams; the origin is placed at the nozzle tip and the model correction factor is $c_g = 2$. (b) Laser-powder interaction coefficient calculated as a function of standoff distance. (c) Transverse section of the intersections between laser and powder beams at an example standoff distance.

powder cones, the tilting angle of their axes β_p , and other geometrical parameters of the deposition nozzle. The details are reported in the Supplementary Material.

Figure 3 reports the quantitative calculations relative to η_{int} for the nozzle geometry considered in the current study. The shaded regions in (c) represent the approximated laser-powder interaction area, taken at the example standoff distance represented by the dashed gray line in (a-b). The following regimes can be identified for the calculation of the interaction area A_{int} , depending on the standoff distance S .

- Closer than a minimum standoff distance value there is no intersection between the laser and powder spots, thus $A_{int} = 0$ and the melt pool does not intercept the metallic powder flux.
- Above a characteristic standoff distance the laser spot fully overlaps with the powder area. If the powder spot diameter is bigger than the laser spot diameter the interaction area is limited by the laser beam itself. The initial standoff distance S_0 is typically chosen in this regime when precision depositions with good transverse resolution are required.
- In the intermediate region there is a strong dependence of A_{int} on S , since only part of the melt pool area can intercept the powder flux. In a first approximation the interaction area can be calculated as the sum of 3 circular segments. This assumption is valid if the laser spot diameter is significantly smaller than the elliptical axes of the powder cone sections. Such typical condition is verified in the considered configuration.
- Above a certain standoff distance another zone of partial intersection is present, tending to $A_{int} = 0$. However this case is neglected in the current model since it lays far from the common working conditions, and because it corresponds to an unstable deposition regime.

The coordinates for the powder and laser spot borders relatively to the nozzle axis are represented in Figure 3(a). These are defined as

$$x_p = \frac{S + z_{p1}}{\tan(\beta_p - \alpha_p)} - x_{p1} \quad (13a)$$

$$x_l = c_g \sqrt{w_{l0}^2 + \theta_l^2 (S - z_{l0})^2} \quad (13b)$$

in the plane of the respective powder and laser beam axes and referred to the nozzle tip center, with x_{p1} and z_{p1} depending on the nozzle geometry (see Supplementary Material). x_p represents the inner cone border of the powder jet. The laser spot limit x_l is assumed as the gaussian beam radius, and it can be calculated at the standoff distance S knowing the $1/e^2$ beam waist radius w_{l0} , the beam half-divergence θ_l , and the focus position z_{l0} along the beam axis. A dimensionless geometrical factor c_g is included in x_l : it summarizes the effects of the approximations introduced in the geometrical model, and in particular the discrepancy between laser spot and the actual melt pool size. This parameter will be determined *a posteriori* by fitting the model predictions to the experimental results, finding values of about 2. Such empirical calibration approach is convenient due to the complexity of providing a comprehensive quantitative model for the actual interaction between laser and powder beams. In fact it must be noted that c_g can be influenced also by thermal accumulation effects, with a not trivial dependence on the chosen deposition strategy and parameters.

The laser-powder interaction area is calculated from x_p and x_l considering the effect of superimposition for the 3 powder jets:

$$x_p \leq -x_l : A_{int} = 0 \quad (14a)$$

$$-x_l < x_p < x_l : A_{int} = 3 \left(x_l^2 \arccos \left(-\frac{x_p}{x_l} \right) + x_p \sqrt{x_l^2 - x_p^2} \right) \quad (14b)$$

$$x_p \geq x_l : A_{int} = 3\pi x_l^2. \quad (14c)$$

In the approximation of uniform powder and laser energy distributions within the respective spot areas, $\eta_{int} = A_{int}/A_p$ can be taken as the fraction of powder flow which can interact with laser beam, hence which can contribute to the effective melt pool and layer growth. This ratio depends on the standoff distance as plotted in Figure 3(b) for $c_g = 2$. Accordingly the theoretical powder catchment efficiency η_{th} can be determined analytically as a function of S for every process condition.

From a different point of view, the theoretical layer height can be calculated from η_{th} as a function of standoff distance exploiting Eq. (7):

$$h_{th} = \eta_{th} \frac{\dot{m}_{tot}}{r_x v \rho}. \quad (15)$$

This allows to simulate the standoff distance at layer n as

$$S_{th,n} = S_0 - \sum_{i=1}^n (h_{th,i} - r_z) \quad (16)$$

considering the initial standoff distance S_0 , and the i -th layer height $h_{th,i}$ being calculated at $S_{th,i-1}$. It can be observed that self-regulation can occur when the gradient $\partial h_{th}/\partial S > 0$ and $h_{th,0} > r_z$, necessary conditions to match $h_{th} = r_z$. The proposed model represents an interesting tool for the prediction of the deposition growth for a given set of process parameters. These methods can allow for the analytical study of the self-stabilization mechanism, as well as for the efficiency optimization and the geometrical accuracy control.

3. Materials and methods

3.1. LMD System

The LMD system is equipped with a fiber laser source (IPG Photonics YLS 3000), having 1070 nm emission wavelength and 3 kW maximum power. A 400 μ m fiber is employed to deliver the processing laser radiation to the deposition head (Kuka Industries MWO-I-Powder). The head is equipped with a 129 mm focal length lens to collimate the laser beam, and with a 200 mm focal length lens to focus it on the working area. The collimation is adjusted in order to have a 1.2 mm laser spot diameter at the reference standoff distance $S_0 = 12$ mm. Optical monitoring devices can be integrated to the deposition head exploiting a dichroic mirror.

Table 1: Chemical composition of the employed AISI 316L powder.

Element	Fe	C	Si	Mn	P	S	Cr	Mo	Ni
Weight %	(base)	0.023	0.36	1.30	0.016	0.005	16.96	2.45	10.89

Table 2: Physical properties of solid AISI 316L stainless steel [24].

Property	Value
density ρ	$8 \times 10^3 \text{ kg/m}^3$
melting temperature T_m	1670 K
specific heat \mathcal{C}_p	500 J/(kg K)
fusion latent heat \mathcal{L}	300 kJ/kg
optical absorptance \mathcal{A}	0.35

The deposition head includes a three-jet nozzle (Fraunhofer ILT 3-JET-SO16-S) for powder delivery. The powder flow is controlled by a powder feeder (GTV TWIN PF 2/2-MF). Argon is used as carrier gas to deliver the powder from the feeder to the nozzle. During the process argon is used also as shielding gas. The deposition head is mounted on a 6-axis anthropomorphic robot (ABB IRB 4600-45).

3.2. Powder and substrate materials

The employed powder is AISI 316L stainless steel, produced by Carpenter Additive. The powder chemical composition is reported in Table 1. The physical properties of bulk AISI 316L are reported in Table 2. The powder is characterized by a spherical shape, with a particle diameter in the range of $45 - 90 \mu\text{m}$. The powder was deposited on AISI 316L substrates having 10 mm thickness and $22 \times 22 \text{ mm}^2$ dimensions, without any cooling system for the substrate.

3.3. Laser and powder beam characteristics

The laser beam parameters were characterized using a beam analyzer and are reported in Table 3. The focus position z_{l0} is referred along the laser head axis, with the origin set at the powder nozzle exit.

The powder beam parameters for the three-jet nozzle are reported in Table 4. The delivery channel inclination β_p , orifice diameter d_{p0} , and orifice radial position x_{p0} were extracted from the nozzle geometrical model, defined relatively to the nozzle tip as represented in Figure 2. The powder dispersion $2\alpha_p$ was estimated by acquiring the powder beam stream with a high-speed camera (see Supplementary Material). In the considered configuration the position of laser beam waist and of the substrate in $S_0 = 12 \text{ mm}$ lay above the convergence point of the powder streamlines.

3.4. System for real-time deposition mass measurement

The system developed for the real-time measurement of the deposition mass is sketched in Figure 4. The device is designed for independent measurements of the deposited and lost powder mass as a function of time during the deposition process. Such measurements are performed with two load cells based on strain gauges, that transduce the mechanical deformation induced by mass into a variation of electrical resistance.

Table 3: Characteristics of the processing laser beam.

Property	Value
waist diameter $2w_{l0}$	0.77 mm
divergence angle $2\theta_l$	83 mrad
focus position z_{l0}	0.9 mm

Table 4: Characteristics of each jet contributing to the powder beam, referring to Figure 2.

Property	Value
powder jet half-dispersion α_p	6°
delivery channel inclination β_p	70°
delivery orifice diameter d_{p0}	1.5 mm
delivery orifice radial position x_{p0}	4.7 mm

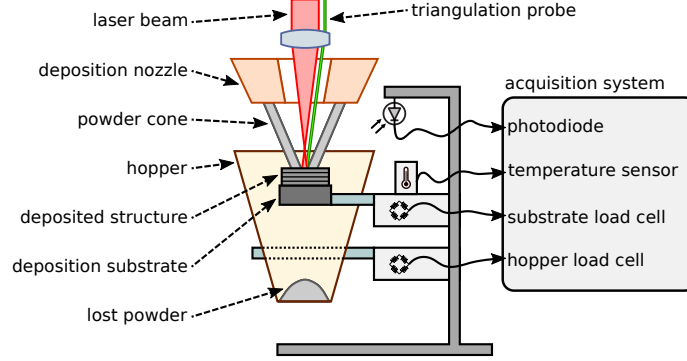


Figure 4: Scheme of the experimental setup for the real-time measurement of the deposited powder mass.

The first load cell is directly connected to the deposition substrate to measure the powder mass which gets deposited. The second load cell sustains a hopper to measure the lost powder. The hopper is used also as a protection system to avoid accumulation of powder around the measurement device. The load cells are connected to the deposition substrate and to the powder hopper by insulating glass bars to suppress thermal conduction. Possible thermal effects which might perturb the acquisitions are monitored using an analog temperature sensor placed close to the load cells.

The entire load cell system is protected with a plastic box, to avoid contamination and damaging of the electronic circuits. The box is purged by a continuous flow of argon, assuring gas recirculation and thermal stability. A photodiode is placed close to the deposition region to get a reference signal, for the synchronization of the mass measurement with the process laser emission. Moreover the measurement setup and electronics are protected from thermal irradiation using aluminum foils.

The voltage signals from the load cells, the temperature sensor, and the photodiode are acquired at 10 Hz using an acquisition board (National Instruments USB-6009) connected to a computer running a LabVIEW program. The details related to the load cell system are reported in the Supplementary Material.

3.5. Deposition height monitoring with coaxial triangulation

The standoff distance was monitored in real-time during the deposition process using a custom coaxial triangulation setup. A detailed description of the measurement working principle was reported in a previous work [23]. The optical scheme follows the former implementation, with some enhancements described in the Supplementary Material. The device is based on a low-power laser probe, superimposed to the deposition head optical chain exploiting a dichroic mirror. The probe beam reaches the 200 mm lens of the deposition head in a slightly off-axis configuration, hence introducing a small beam deflection relatively to the optical axis. Then the beam passes through the nozzle towards the deposition region. A coaxial camera acquires the probe spot position on the melt pool, whose distance can be extracted using the triangulation principle.

The probe spot position has been calibrated as a function of standoff distance [39], finding an enhanced sensitivity factor of 0.106 mm/pixel over a 20 mm range. The camera acquisition is performed at a frame rate of 400 Hz. The standoff distance is extracted in real-time using a Python algorithm. The same program is used to acquire the service variables of the robot system via an ethernet socket connection at a rate of about

Table 5: Varied and fixed parameters of the experimental campaign.

Parameter	Value
laser power P	525, 612, 700 W
scanning speed v	22, 32, 42 mm/s
powder feed rate \dot{m}_{tot}	0.11, 0.16, 0.22 g/s
robot transverse increment r_x	0.45 mm
robot height increment r_z	0.2 mm
total layer number	50
track number (for each layer)	42
initial standoff distance S_0	12.0 mm
laser spot diameter (at S_0)	1.2 mm
carrier gas flow rate	7.5 L/min
shielding gas flow rate	25.0 L/min

100 Hz. These are used to correlate the standoff distance data sets with the deposition head coordinates and with the laser emission.

4. Experimental campaign and sample analysis

The main target of the experimental campaign was the investigation of the link between powder catchment efficiency and height growth in bulk geometries. Square cuboids having $19 \times 19 \times 10 \text{ mm}^2$ nominal dimensions were produced for the scope, obtained by means of multi-layer multi-track deposition. An alternated bi-directional deposition strategy was adopted, following the deposition path sketched in Figure 5, with orthogonal scanning directions for adjacent layers.

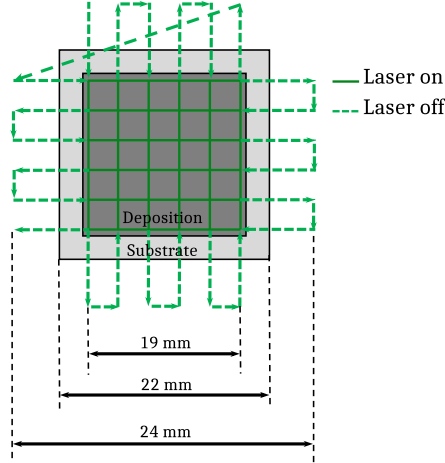


Figure 5: Deposition path strategy for building the square cuboids.

The experimental campaign followed a 2-level factorial plan for 3 varied parameters plus a central point, corresponding to a total of 9 combinations. The varied parameters were the laser power P , the scanning speed v , and the delivered powder flow rate \dot{m}_{tot} . The central point was chosen as a typical working condition, optimized for bulk depositions with good dimensional resolution, yet representing a compromise for a reduced powder catchment efficiency. A number of 3 replicates was performed for each deposition condition, for a total of 27 randomized specimens. The fixed and varied parameters of the campaign are reported in Table 5. Each combination of parameters is identified by a progressive label as reported in Table 6.

Table 6: Labels of the considered process conditions.

Label	P [W]	\dot{m}_{tot} [g/s]	v [mm/s]
■ C1	612	0.16	32
■ C2	700	0.22	22
■ C3	700	0.22	42
■ C4	700	0.11	22
■ C5	700	0.11	42
■ C6	525	0.22	22
■ C7	525	0.22	42
■ C8	525	0.11	22
■ C9	525	0.11	42

During the deposition the powder flow was kept continuous due to the slow response dynamics of the powder feeder. On the contrary, the laser operation was intermittent, with the emission enabled only for the intervals over the deposition substrate. The intervals with the laser turned off were necessary to avoid transitory effects related to acceleration and deceleration of the robot at the substrate borders, even if they introduce an unavoidable inefficiency contribution. Specifically the laser emission remained inactive for about 0.5 s between consecutive tracks, and for 2 s to 6 s between consecutive layers. The robot transverse increment $r_x = 0.45$ mm was chosen to guarantee a sufficient overlap between consecutive tracks, considering the typical single track width of about 1 mm observed in the considered conditions. The height increment $r_z = 0.2$ mm represents an optimal value for precision depositions.

The experimental conditions of the campaign are represented in the space of process parameters in Figure 6. Images of the realized samples are reported for each condition. From a qualitative point of view, the parts were deposited with a cubic shape as expected, except for condition C9: the latter represented an evident process failure, with an irregular shape and a significantly lower final height. Moreover it can be observed that the conditions at higher scanning speed showed more regular surfaces for the lateral walls, with a reduced debris attachment.

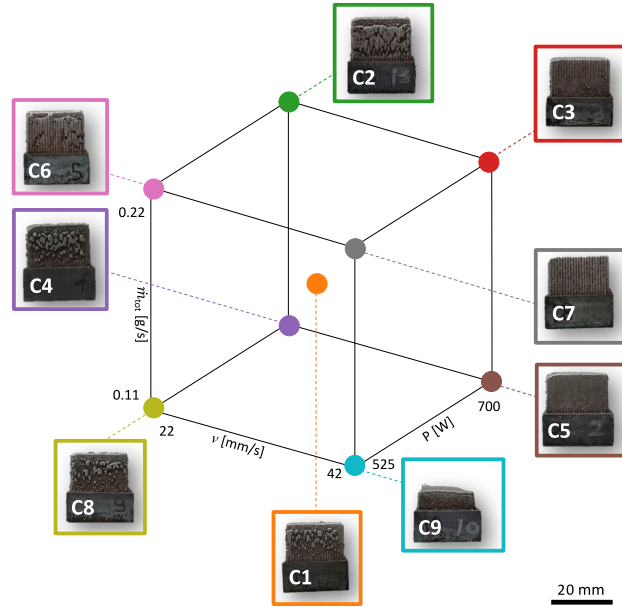


Figure 6: Samples deposited in the different experimental conditions, represented in the space of the varied process parameters.

The deposition track shape was analyzed for few samples in significant process conditions, for a qualitative check of the model hypotheses and of the dimensional measurements. Accordingly the cuboids were cut along the growth direction to highlight the cladding structures. The cross sections were polished and chemical etched using a solution of distilled water, hydrochloric acid, and nitric acid for 10s. The shapes of the deposition layers and tracks along the cross sections were analyzed using an optical microscope.

5. Results

5.1. Mass measurements

The deposition mass was measured in real-time during the process by means of the load cell system. The initial mass offsets given by substrates and supports were subtracted from the load cell readouts. Each series was grouped by track and layer number, whose intervals were identified by acquiring the process laser emission with the monitor photodiode. The data have been smoothed using a 2-nd order low-pass filter with 5 layer cutoff, to suppress intra-layer variability related to the robot positioning vibrations. Indeed the current study is focused on the overall behavior of the bulk deposition process, not on the single layer spurious fluctuations. Finally, the data of each group of 3 replicates have been averaged point-by-point to extract the mean trend for each experimental condition. The results for the average deposition mass \bar{m}_{dep} are reported in Figure 7(a) as a function of layer number. Error bars represent the standard deviation within the replicates for each process condition.

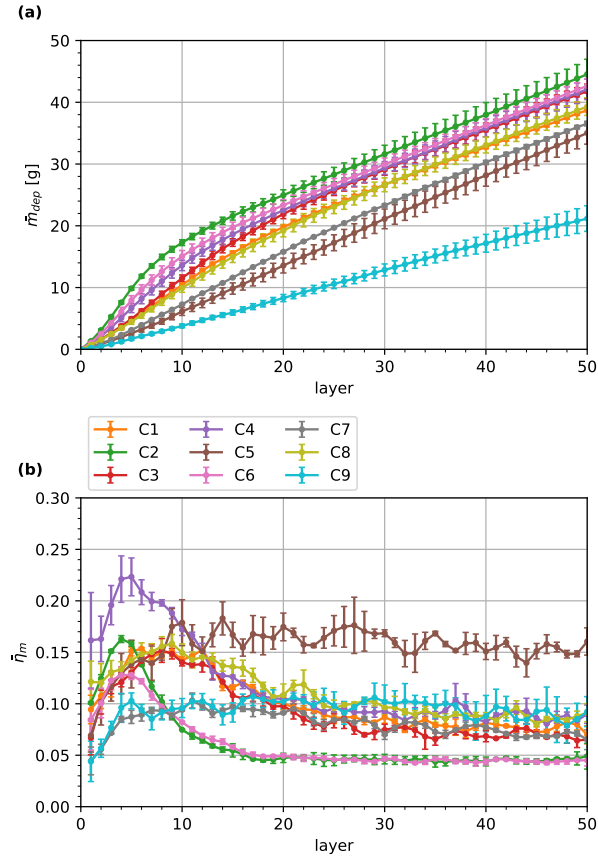


Figure 7: (a) Average deposition mass, measured as a function of layer number and grouped by experimental condition. (b) Powder catchment efficiency, including the deposition path intrinsic inefficiency.

Conversely to the substrate load cell, the hopper sensor readout showed big oscillations, probably caused by vibrations induced by the robot movements. Accordingly the acquisitions of the lost powder were used only to check its final mass value, confirming that inefficiency is mainly determined by the powder that is not captured by the melt pool and falls from the substrate, being collected by the hopper. The powder catchment efficiency of each layer was calculated using Eq. (2) by differentiating \bar{m}_{dep} , assuming the total mass flow rate \dot{m}_{tot} as a constant parameter, known from a preliminary offline calibration of the mass flow rate provided by powder feeder. The corresponding powder catchment efficiency curves are reported in Figure 7(b).

The experimental results show that, in most conditions, the trend of \bar{m}_{dep} undergoes a slope change within the first ~ 10 layers. After that, the deposition mass curves grow almost linearly with similar slopes, apart from condition C9 which departs with a clearly slower deposition rate. This behavior reflects on efficiency, with $\bar{\eta}_m$ reaching its maximum value $\lesssim 0.25$ within the initial layers for almost every condition. After such transient $\bar{\eta}_m$ stabilizes at lower values between 0.05 and 0.15, with an essentially constant trend for all the conditions.

A preliminary analysis is proposed considering the final values of the powder catchment efficiency, measured as $\bar{\eta}_m$ averaged over the last 10 layers, to highlight the role of process parameters in a stationary regime. The main effects and interaction plots of the response variable are reported in Figure 8. Each point in the plots represents the average for all the experimental runs taken at the corresponding parameter value, while the horizontal dashed line represents the average over all the experimental runs. The main effects plot implies that the strongest influence on $\bar{\eta}_m$ in the last layers derives from the delivered powder mass flow rate, \dot{m}_{tot} ; nevertheless both laser power P and transverse scanning speed v affect the powder catchment efficiency in such stationary condition. While an increase in P and v reflects in a greater efficiency, higher values of \dot{m}_{tot} appear to induce a lower $\bar{\eta}_m$. The interaction plots suggest interactions between processing laser power and deposition scanning speed ($P \cdot v$), and between processing laser power and delivered powder mass flow rate ($P \cdot \dot{m}_{tot}$). On the other hand, no strong interactions are expected between the scanning speed v and the powder mass flow rate \dot{m}_{tot} . The respective analysis of variance (ANOVA) showed that all the parameters and their second order interactions are significant; the detailed results are omitted for the sake of brevity.

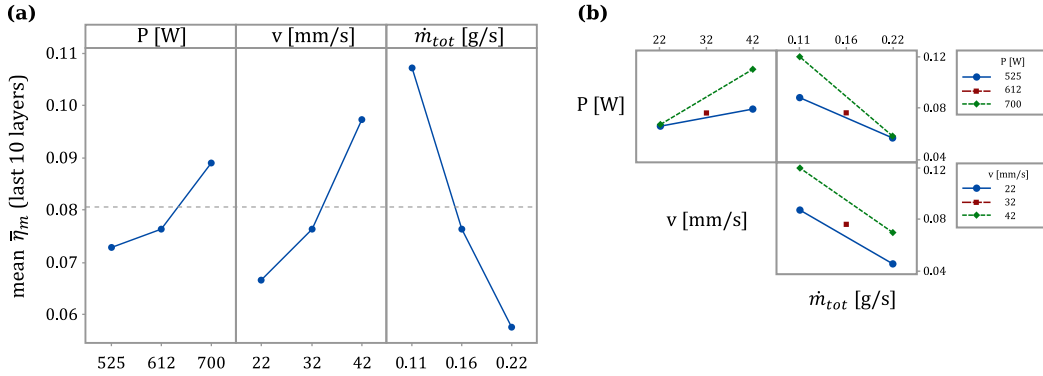


Figure 8: Main effects plot (a) and interaction plots (b) for $\bar{\eta}_m$ averaged over the last 10 layers.

The analysis reported here can be interesting from a technological point view, since the final user is typically interested to the overall efficiency, measured as the deposit mass over the total deposition time. However it must be stressed that $\bar{\eta}_m$ is not relevant for a direct description of the deposition process physics, since it is comprehensive of losses related to the deposition strategy and, in particular, its value is reduced by the presence of intervals along the deposition path where the processing laser emission is disabled. Moreover the key role of standoff distance has not been taken into account at this preliminary stage. As it will be discussed in the following sections, the depositions in the different experimental conditions stabilize at

different standoff distance values, hence in different conditions of laser-powder interaction.

5.2. Height measurements

The standoff distance was measured in real-time as a function of deposition time by means of the coaxial triangulation system. The synchronous logging of the robot coordinates was used to identify the deposition head position, thus to extract the track and layer numbers. This allowed for a tomographic three-dimensional reconstruction of the deposited samples. Similarly to the analysis of \bar{m}_{dep} , the data sets of the mean standoff distance have been averaged over the 3 replicates and low-pass filtered with a 5 layer cut-off to suppress layer-to-layer fast fluctuations. The results for the mean standoff distance \bar{S} in the different experimental conditions are reported in Figure 9(a). The curves highlight that \bar{S} departs from its initial value $S_0 \simeq 12$ mm with a slope which depends on the process condition. Apart from condition C9, all the curves show a reduction in the standoff distance, hence an actual deposit growth which is faster than the designed height. For almost every condition a stationary standoff distance is reached after the first ~ 20 layers, with the final values of \bar{S} ranging between 7 mm and 9 mm, where the process enters in the self-stabilized regime for the deposition height growth.

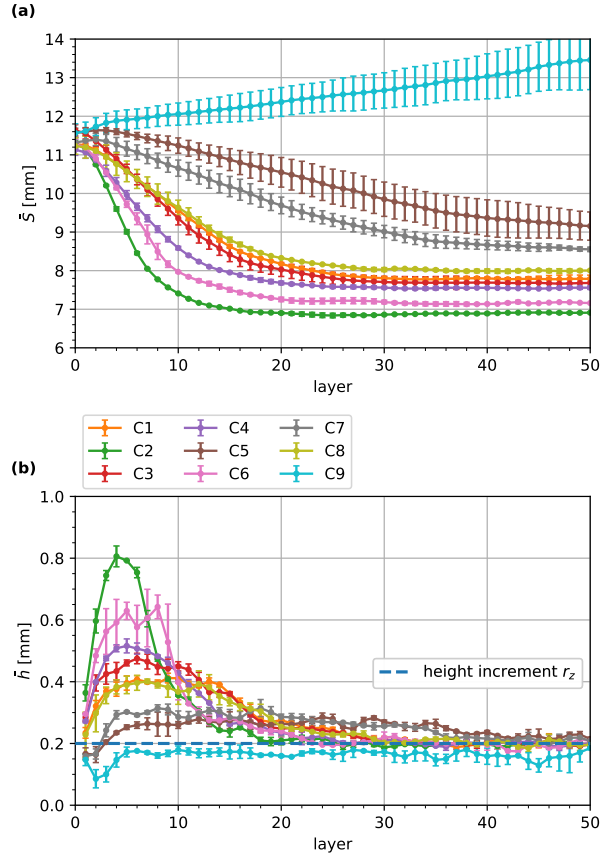


Figure 9: (a) Average standoff distance, measured as a function of layer number and grouped by experimental condition. (b) Layer height calculated from standoff distance.

The average layer height \bar{h} has been calculated differentiating the standoff distance (see the Supplementary Material). The results are reported in Figure 9(b). For almost every condition the layer height undergoes an initial positive mismatch relatively to the robot increment along the build direction, fixed to $r_z = 0.2$ mm and represented as a horizontal dashed line in the plot. Such condition corresponds to a

deposition height which grows faster than the programmed path, with \bar{h} reaching values up to 0.8 mm for condition C2, 4 times r_z . After such transient the layer height tends to r_z , hence matching the robot height increment in the self-regulated regime. The only exception is C9, where a different behavior is observed, with the layer height being always slightly below r_z : this corresponds to process instability, with a departure towards bigger standoff distance values.

Figure 10 reports the cross-section along the build direction for a sample deposited in condition C2. Horizontal lines are superimposed to the image to represent the average layer height measured with inline triangulation. Vertical lines having horizontal spacing equal to the robot transverse increment $r_x = 0.45$ mm are also reported. The picture provides a qualitative validation for the coaxial triangulation measurements for the description of the layer height during the deposition. Moreover, as it can be observed from the image magnifications, the deposition track shape changes significantly during the different process stages. Within the initial unstable layers the tracks are taller and strongly inclined, with the presence of pores caused by lack of fusion; conversely, the final self-regulated regime corresponds to a more regular track pattern, with the layer height matching the robot height increment r_z . These observations support the validity of the approximations which were introduced in Eq. (6) regarding the track cross-section geometry for a bulk deposition.

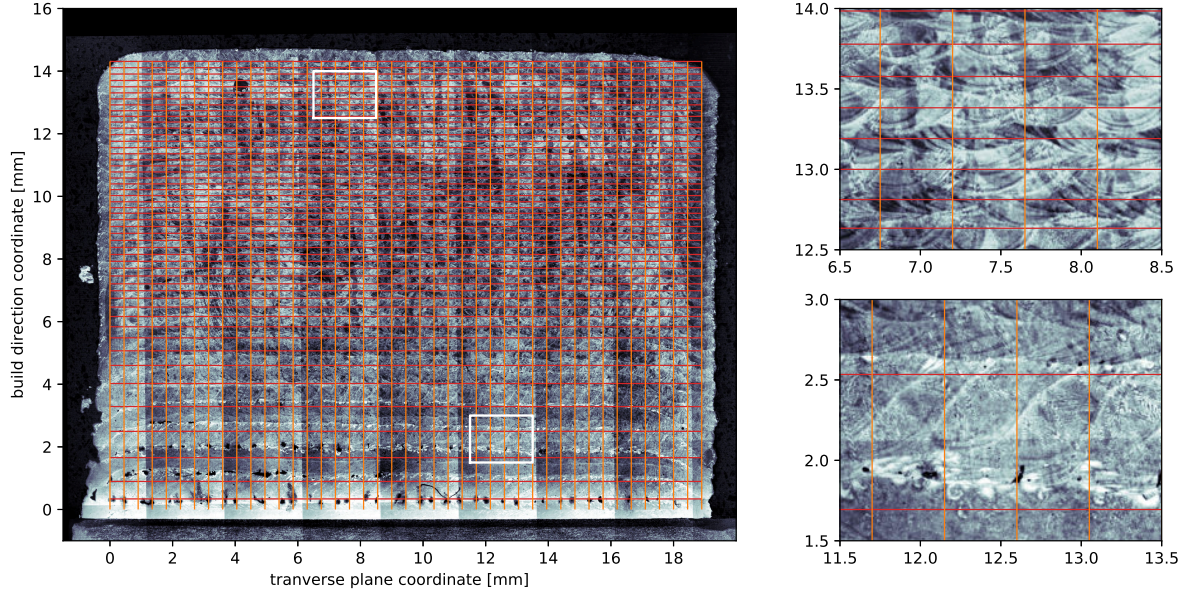


Figure 10: Cross-section of a sample in the process condition C2. Horizontal lines represent the measured layer height, vertical lines represent the robot transverse increment. Some single tracks are magnified in the bottom.

5.3. Powder catchment efficiency

The geometrical definition of powder catchment efficiency $\bar{\eta}_h$ can be calculated from the layer height measurements using Eq. (7). The results are reported in Figure 11(a). They show that efficiency typically varies between 0.08 and 0.4, with an initial transient that follows the behavior which was already observed for $\bar{\eta}_m$ in Figure 7(b). The efficiency stabilizes after about 20 layers, with C5 being the most efficient condition, while C6 and C2 correspond to the least efficient ones.

For a quantitative comparison between $\bar{\eta}_h$ and the powder catchment efficiency $\bar{\eta}_m$ obtained from direct mass measurements, the latter must be corrected to isolate the effects related to the deposition process only. Indeed the definition of the overall powder catchment efficiency introduced in Eq. (2) includes an efficiency component $\bar{\eta}_{path}$ determined by the deposition geometry and by the robot dynamical parameters. Such

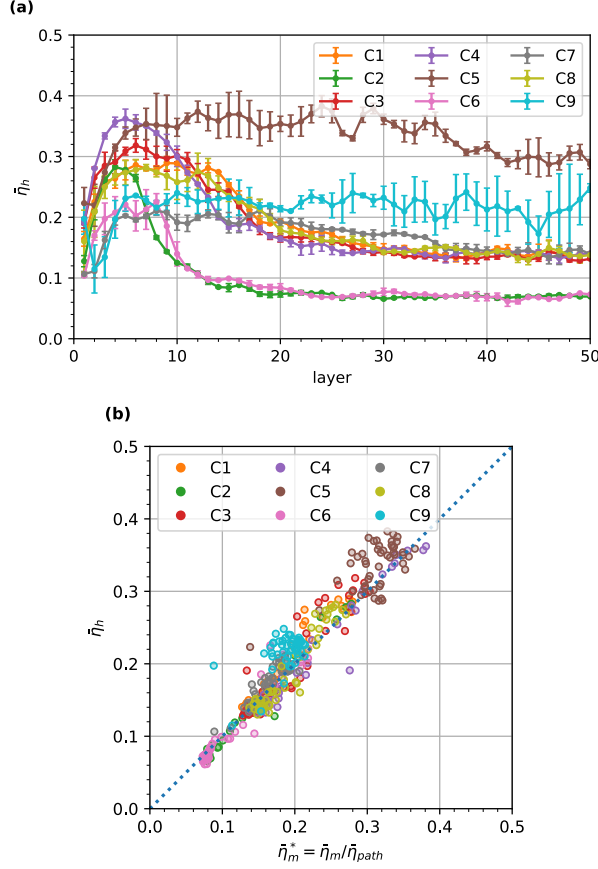


Figure 11: (a) Geometrical definition of powder catchment efficiency, calculated from the layer height measurements. (b) Comparison between the effective powder catchment efficiency and its indirect geometrical measurement.

path strategy coefficient has been estimated from the robot logs as the ratio between the laser emission intervals over the whole deposition time, following the definition of Eq. (3). The values found for $\bar{\eta}_{path}$ are reported in the Supplementary Material, and showed a dependence on the scanning speed. The average value $\bar{\eta}_{path} = 0.54 \pm 0.04$ means that a remarkable powder fraction equal to $1 - \bar{\eta}_{path}$ is lost during the robot position settlement, when the laser emission is turned off.

Although the inefficiency introduced by $\bar{\eta}_{path}$ is important from the point of view of the overall deposition costs, this is essentially determined by technical reasons, and it is not relevant for the comprehension of the deposition process physics. Therefore the effective powder catchment efficiency can be calculated as $\bar{\eta}_m^* = \bar{\eta}_m / \bar{\eta}_{path}$ as introduced in Eq. (4). The experimental values of $\bar{\eta}_m^*$ and $\bar{\eta}_h$ are compared in the scatter plot of Figure 11(b), where each point represents the average efficiency for a single layer. It can be seen that there is a good correspondence between the two efficiency measurements. Most of the experimental points lay close to the expected correspondence diagonal, with a Pearson correlation coefficient equal to 0.97. This confirms that the powder catchment efficiency is linked to the deposition height as it was derived in the layer height model, demonstrating that $\bar{\eta}_h$ can be conveniently probed by means of an indirect geometrical measurement.

The results for the effective powder catchment efficiency $\bar{\eta}_m^*$ have been analyzed to identify the influence of the deposition parameters on the process physics. Differently from the results reported in Figure 8, here the efficiency is analyzed at constant standoff distance S . This allows to suppress the strong dependence of the laser-powder interaction on S , which was discussed in the model for η_{int} . Accordingly $\bar{\eta}_m^*$ has been

interpolated at the same standoff distance value for all the experimental curves: $\bar{S}' = 10.5$ mm has been conveniently chosen as test point, since such value was crossed for almost all the conditions after few initial layers and before self-stabilization. The substrate thermalization transients expected at the beginning are therefore avoided, and data comparison can be performed with consistency. Only the unstable condition C9 was excluded from the analysis, since it never crosses $\bar{S}' = 10.5$ mm. The results for the interpolated $\bar{\eta}_m^*$ are reported in Figure 12 as a function of the varied parameters. The main effects plot shows that there is an influence of laser power and powder flow rate on efficiency: $\bar{\eta}_m^*$ grows with P , while it decreases with \dot{m}_{tot} . The ANOVA table, omitted for brevity, showed that only these two parameters are significant. Such results are in agreement with the predictions of the theoretical powder catchment efficiency η_{th} introduced in Eq. (12), essentially confirming the validity of the model hypotheses. Analogously, the lack of influence of v on $\bar{\eta}_m^*$ is in accordance with the dependence of η_{th} only on the ratio P/\dot{m}_{tot} , i.e. on the quantity of energy available for a given amount of delivered powder mass. Indeed the scanning speed is relevant for the initial transient caused by thermal accumulation and temperature rise at the beginning; however, in the stationary condition, v affects equally the energy and powder concentrations, and its effect on the effective powder catchment efficiency can be neglected in a first-order approximation.

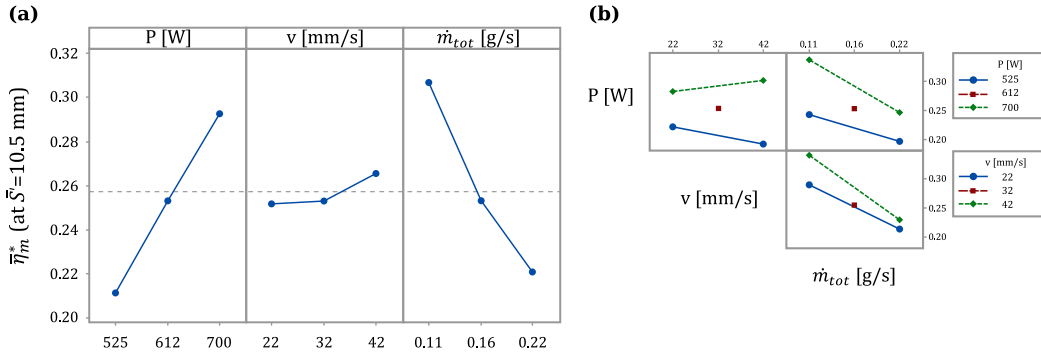


Figure 12: Main effects plot (a) and interaction plots (b) for the effective powder catchment efficiency interpolated at standoff distance $\bar{S}' = 10.5$ mm. The unstable condition C9 was excluded from the analysis.

5.4. Effects of standoff distance on efficiency and height growth

The dependence of powder catchment efficiency on standoff distance is highlighted in Figure 13(a), where η_h is plotted as a function of \bar{S} . The deposition starts around the reference value $S_0 \simeq 12$ mm, in the shaded interval of the plot. The initial transient can be attributed to thermal stabilization effects. At the initial phase of the process starting at room temperature the substrate acts as a heat sink, dissipating the laser energy by conduction in a more marked manner. As the process proceeds over the layers, the substrate and the deposited material heat up, increasing the deposition efficiency until a stationary temperature is reached. Then the process tends to lower efficiency when it enters in the self-regulated regime, occurring at smaller standoff distance values and driven by the laser-powder spatial interaction. The only exception is condition C9, which departs toward bigger \bar{S} values, hence to process instability. The highest efficiency in the self-regulated regime is observed for condition C5, which also corresponds to the smallest standoff distance mismatch relatively to its initial reference value S_0 .

In the proposed model the theoretical powder catchment efficiency η_{th} was defined in Eq. (12) from the process parameters P and \dot{m}_{tot} , with \dot{m}_{tot} determining the critical melting power P_0 introduced in Eq. (10). Moreover η_{th} depends on standoff distance S as a consequence of the variable interaction area A_{int} , which can be calculated from Eq. (14) knowing the powder and laser beam parameters. Therefore the theoretical powder catchment efficiency η_{th} can be calculated as a function of \bar{S} for each process condition.

It must be remarked that a geometrical correction factor c_g was implicitly included in the definition of η_{th} and introduced in Eq. (13). This was necessary to take into account of the approximations assumed in the discussion, in particular regarding the laser-powder interaction region and spatial beam distributions. It can

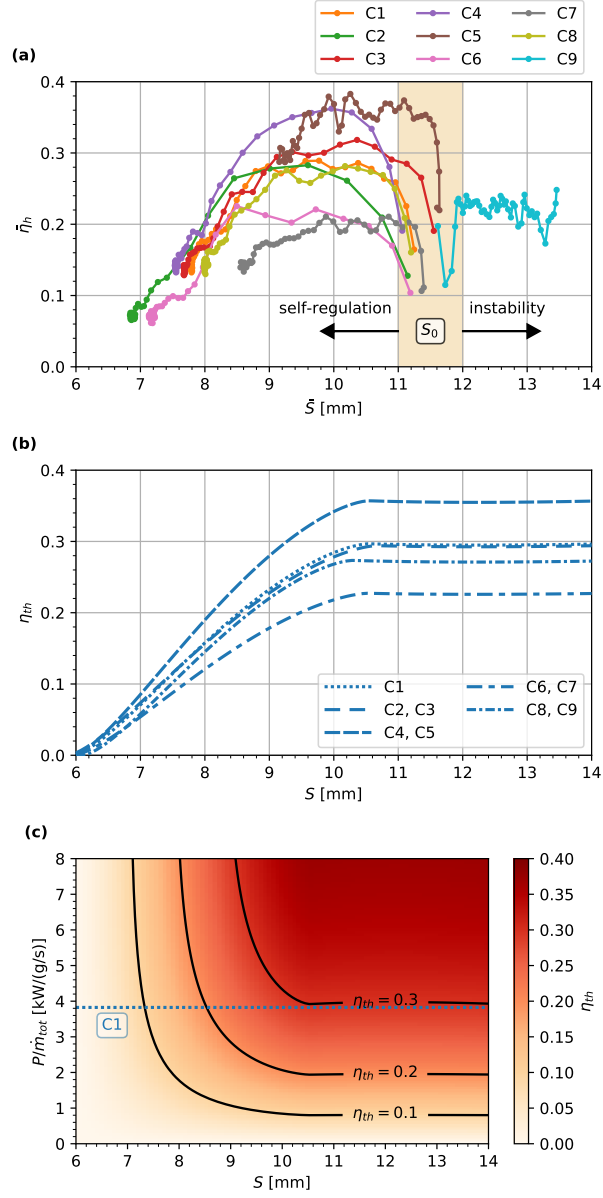


Figure 13: (a) Experimental powder catchment efficiency plotted as a function of standoff distance for the different experimental conditions. (b) Theoretical powder catchment efficiency calculated as a function of standoff distance. (c) Color map representing the theoretical powder catchment efficiency in the space of standoff distance and process parameters.

be expected that c_g is influenced by the specific deposition geometry and strategy, determining the effects of thermal accumulation and melt pool evolution during the deposition. Accordingly c_g was used as calibration parameter for the semi-empirical model, by fitting η_{th} against the corresponding experimental efficiency curves $\bar{\eta}_h$ of Figure 13(a). The optimal values found for c_g in the different conditions are reported in the Supplementary Material. The calibration factor exhibits a small dependence with the process parameters, and its average value over all the deposition conditions is $c_g = 2.19 \pm 0.17$. Since $c_g > 1$, the model underestimates the effective laser-powder interaction region. Reasonably c_g can be explained in terms of a melt pool which is bigger than the laser spot, e.g. considering an elongated melt pool, whose cue plays a relevant role in the powder catchment. It can be expected that c_g depends on the process parameters that influence the melt pool temperature.

The curves of η_{th} are reported in Figure 13(b), calculated considering the respective c_g values found from calibration. It can be observed that, although second-order corrections might be required for a quantitatively precise matching, the efficiency model is consistent with the measurements of Figure 13(a). Clearly the initial efficiency transients observed experimentally around S_0 are not reproducible, since the simulated efficiency curves assume a stationary thermal condition.

From Eq. (12) it follows that the theoretical powder catchment efficiency is determined by two independent quantities, S and the ratio P/P_0 , which reduces to P/\dot{m}_{tot} making explicit the dependence on the considered variable process parameters. Therefore η_{th} can be described in a bi-dimensional space as shown in Figure 13(c), where it is calculated considering the calibration coefficient $c_g = 2.25$ corresponding to condition C1. The color map shows a high efficiency region for big values of P/\dot{m}_{tot} around $S_0 = 12$ mm, where the laser intensity is sufficient to melt efficiently the available powder flux. Moreover efficiency decreases with S , due to the reduction of the laser-powder beam interaction. In such representation each process condition lays on a horizontal line, that is set by the values of P and \dot{m}_{tot} , determining the efficiency evolution as a function of the variable standoff distance.

The self-regulating behavior is evident in Figure 14(a), where the measured layer height \bar{h} is plotted as a function of the average standoff distance \bar{S} . The robot height increment $r_z = 0.2$ mm is reported as a horizontal dashed line. It can be seen that, starting from the standoff distance $S_0 \simeq 12$ mm within the shaded region of the plot, an initially positive height mismatch brings the deposition in the self-regulation regime, reached at lower \bar{S} values. The corresponding height variability is influenced by the specific process condition. C2 shows the bigger variability and the smaller final standoff distance, while C5 is the condition which closely matches the robot height increment r_z , ending close to the initial standoff distance S_0 . Remarkably, the reduced layer height variability observed for condition C5 is associated also to a high powder catchment efficiency, as commented for Figure 13(a). Only for condition C9 the process deviates to the unstable regime, with $\bar{h} < r_z$.

The theoretical layer height is calculated using Eq. (15) as a function of standoff distance in Figure 14(b), considering the calibration coefficients c_g that were previously determined. It can be seen that the results for h_{th} are in good accordance with the experimental curves of Figure 14(a), neglecting the transient around the initial standoff distance S_0 caused by thermal effects before substrate temperature stabilization. In Figure 14(c) h_{th} is calculated considering $c_g = 2.25$, corresponding to condition C1. The theoretical height color map is represented as a function of two independent quantities, similarly to the treatment of η_{th} : the standoff distance S (horizontal axis) and a combination of the parameters \dot{m}_{tot} , v and P (vertical axis), which can be obtained from Equations (15) and (12). Each parameter combination determines a process condition along a horizontal line. The process self-regulation is expected to happen along the isoline of the robot height increment, where the matching condition $h_{th} = r_z$ is fulfilled, with an evolution ruled by the non-zero gradient $\partial h_{th} / \partial S > 0$.

From a different point of view, the calculation of the theoretical efficiency η_{th} allows to predict the deposition growth for each set of process parameters. This has been performed using Eq. (16) to simulate the standoff distance as a function of layer number, hence summing up the predicted layer height contributions h_{th} starting from $S_0 = 12$ mm. This is equivalent to determine the process evolution along a horizontal line of the map reported in Figure 14(c). The results corresponding to each considered experimental condition are reported in Figure 15. It can be seen that there is a good correspondence with the experimental standoff distance curves reported in Figure 9(a). This means that the variable powder catchment efficiency,

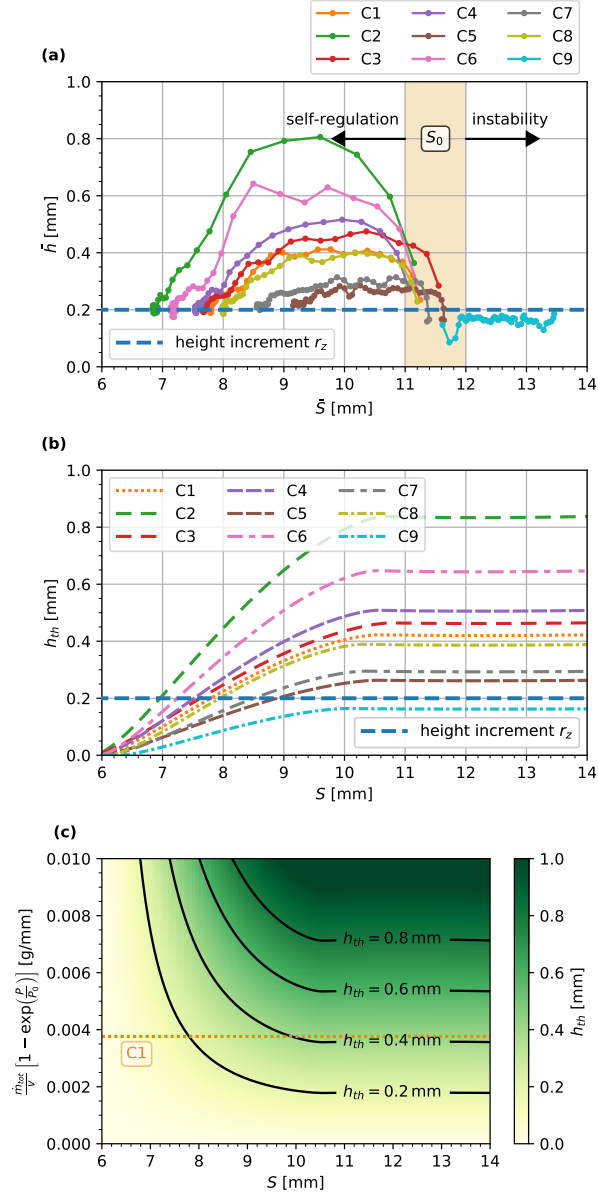


Figure 14: (a) Experimental layer height plotted as a function of standoff distance for the different experimental conditions. (b) Theoretical layer height calculated as a function of standoff distance. (c) Color map representing the theoretical layer height in the space of standoff distance and process parameters.

modeled in terms of process parameters and variable powder and energy distributions, allows to explain the experimental transient to closer standoff distances and lower efficiencies, hence providing a quantitatively valid interpretation for the process self-regulation and stabilization.

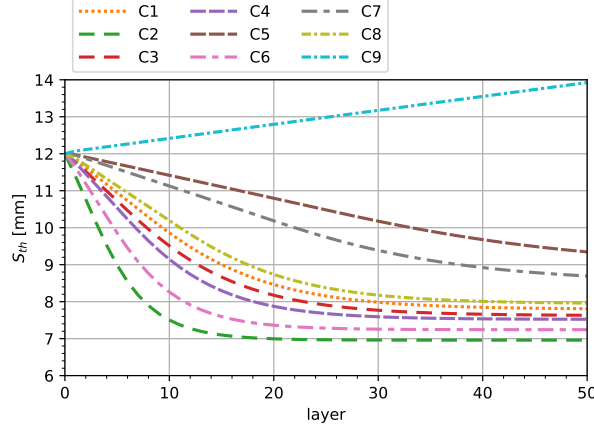


Figure 15: Evolution of the theoretical standoff distance simulated with the efficiency model.

6. Discussion

The results for the deposition height and mass measurements showed that the powder catchment efficiency can be determined by measuring the layer height. In fact the η_m^* and η_h efficiency definitions resulted highly correlated, as evident from Figure 11(b) and predicted in Section 2.2. This confirmed the validity of the model hypotheses, stressing that these were introduced in the assumption of a stationary bulk deposition. The demonstration of η_h as a good efficiency estimator allows for the possibility of using dimensional monitoring techniques also for the process optimization. Coaxial triangulation is particularly interesting for the scope, since its optical probe is essentially omnidirectional and can be easily implemented on a wide class of existing setups at a reduced cost: it allows flexibility in the deposition process monitoring, without requiring more complex and intrusive setups for the direct deposition mass measurement.

The results highlighted that the deposition growth instability is mainly caused by efficiency variability. In fact, in stationary thermal conditions, the powder catchment efficiency depends on standoff distance due to the variable spatial interaction between the laser and powder beams, as shown in Figure 13(a). This allows to explain the self-regulation process as the balance between the initial heat accumulation and subsequent powder catchment efficiency reduction. In the considered configuration such passive stabilization mechanism is observed when the layer growth overcomes the robot height increment at the beginning, as reported in Figure 14(a). However the standoff distance reduction reflects in a lower efficiency, acting as a negative feedback loop as predicted by the model and confirmed by experiments. This effect is ruled by the reduction of the laser-powder interaction below a characteristic standoff distance, as shown by the calculation reported in Figure 3(b). At the end, the deposition stabilizes when the reduced efficiency brings the deposition layer height to match the robot height increment. This happens at different final standoff distance values, depending on the process parameters.

The deposition self-regulation is desirable because it corresponds to process robustness and geometrical accuracy enhancement. However it is in concurrency with powder catchment efficiency. A compromise between the two aspects must be taken into account. Moreover stabilization can be reached after a transient in the standoff distance, hence a departure from the geometrical design. Therefore the choice of the initial process parameters is particularly important for optimizing powder catchment efficiency, process stability, growth regularity, and part accuracy. The semi-empirical model for η_{th} provides a powerful tool for this

task. Such model was developed assuming a bulk deposition in a stationary thermal regime, characterized by multiple layers with a large number of tracks, and neglecting possible second-order effects determined by the specific deposition geometry or thermal drifts.

After a preliminary model calibration through c_g , the theoretical efficiency map of Figure 13(c) allows to identify the most efficient parameter combination, related to the ratio between laser power and delivered powder rate, and the respective initial standoff distance. Analogously, the theoretical layer height map of Figure 14(c) allows to identify the stability conditions depending on the required resolution, i.e. fixing the robot height increment and the scanning speed such that $h_{th} \geq r_z$. A wise choice takes the combination of initial standoff distance and robot height increment which lays close to the layer height predicted in the corresponding map region. This means that the process will stabilize soon, without varying significantly from the initial standoff distance and from the designed geometry, while maintaining an optimal efficiency. Moreover the isoline $h_{th} = r_z$ should be crossed transversely during the standoff distance evolution to reach stability, in a condition where the gradient $\partial h_{th} / \partial S > 0$ is maximized to guarantee a robust and fast convergence.

For the considered experimental campaign the best choice seems to be represented by condition C5, which is both efficient and characterized by a height growth that closely follows the programmed robot path. In fact the energetic coefficient η_{en} is maximum for C5, since the high laser power and low powder mass flux guarantees a high melting rate, hence low powder losses. Furthermore the combination of these parameters with the respective scanning speed guarantees a layer height growth that almost matches the robot height increment at the initial standoff distance, hence process stability and deposition regularity. However it must be noted that, even in the most convenient standoff distance condition, the powder catchment efficiency is limited to less than 0.4 by the partial interaction between the laser and powder beams, expressed by η_{int} and calculated in Figure 3(b). This is given by the laser spot size, which is chosen smaller than the powder beam spot to achieve a good transverse resolution.

The model can be potentially used for an open-loop process optimization, since it predicts well the deposition growth as shown in Figure 15. Indeed the knowledge of the expected deposition growth could allow for a quantitative preliminary correction of the geometrical model to meet the design requirements. For example, this might be performed by compensating the deposition height mismatch in the programmed robot path, once the choice of the initial process parameters have been performed. Moreover the threshold between self-stabilized and unstable growth can be also identified from the model, reducing the risk of deposition failures and wastes. This represents a great advantage during the component design and realization, reducing the number of preliminary tests and manual operations required for the parameter optimization.

7. Conclusions

This work provides a systematic investigation of layer height variation and self-stabilization in LMD. Modeling and experimental methods have been developed to evaluate the powder catchment efficiency inline the process. The deposition mass and height have been monitored in real-time in different process conditions by means of a custom measurement system. The main outcomes of the work are as follows.

- The powder catchment efficiency mainly relies on the balance between laser power and delivered powder rate. The layer height depends on the interplay between powder catchment efficiency, delivered powder rate, and scanning speed.
- The standoff distance plays a crucial role in the determination of the powder catchment efficiency, hence of the layer height, because of the variable laser-powder interaction.
- The maximum achievable efficiency was limited by the partial overlap between laser and powder beams.
- The height growth deviates from the initial conditions, depending on the process parameters and on the amount of energy provided by the laser source.

- The self-stabilization mechanism is associated to efficiency reduction, which leads the deposition growth to match the height increment at different final values of standoff distance and powder catchment efficiency.
- Self-stabilization cannot be reached in conditions of low laser power, low powder flow rate, and high scanning speed, which do not guarantee a sufficient initial layer growth.
- The powder distribution, hence the nozzle design, plays a critical role on the selection of the optimal process parameters, especially of the initial standoff distance.
- The use of a load cell system is a straightforward, but intrusive, approach to measure powder catchment efficiency. The coaxial triangulation system was proven as a convenient alternative tool for the process stability comprehension.
- Process parameter maps were calculated to establish the link between powder catchment efficiency, layer height, and standoff distance, and can be used to identify the optimal process conditions.

The presented methods might be applied to closed-loop control systems for obtaining a regular deposition growth. For example, the real-time dimensional measurement by means of coaxial triangulation, eventually combined with pyrometry for a convenient temperature measurement, can be integrated with a feedback correction on the process parameters, such as laser power, scanning speed, or powder flow. Nevertheless, some aspects remain open. The approach should be further applied to conditions of higher deposition rates. The developed analytical model is dependent on the nozzle type, which should be extended to coaxial nozzles as well. Finally, the inclusion of a melt pool geometrical model could overcome the requirement of calibration to the process parameters, providing a more general analytical description.

Acknowledgments

The authors gratefully acknowledge Mr. Riccardo Caccia for his support during the experimental work. Mr. Eligio Grossi is acknowledged for his support in the design of the electronic acquisition setup, Mr. Stefano Mutti for his support in the realization of the communication software for the robot system. The authors would like to thank the BLM Group for the longstanding collaboration during the LMD cell development. The project presented in this paper has been funded with the contribution of the Autonomous Province of Trento, Italy, through the Regional Law 6/99 (Project LT 4.0). This work was supported by European Union, Repubblica Italiana, Regione Lombardia and FESR for the project MADE4LO under the call “POR FESR 2014–2020 ASSE I – AZIONE I.1.B.1.3”.

References

- [1] A. Dass, A. Moridi, State of the art in directed energy deposition: from additive manufacturing to materials design, *Coatings* 9 (7) (2019) 418. doi:10.3390/coatings9070418.
- [2] T. DebRoy, H. L. Wei, J. S. Zuback, T. Mukherjee, J. W. Elmer, J. O. Milewski, A. M. Beese, A. Wilson-Heid, A. De, W. Zhang, Additive manufacturing of metallic components – Process, structure and properties, *Progress in Materials Science* 92 (2018) 112–224. doi:10.1016/j.pmatsci.2017.10.001.
- [3] J. M. Flynn, A. Shokrani, S. T. Newman, V. Dhokia, Hybrid additive and subtractive machine tools – Research and industrial developments, *International Journal of Machine Tools and Manufacture* 101 (2016) 79–101. doi:10.1016/j.ijmachtools.2015.11.007.
- [4] K. Shah, I. U. Haq, S. A. Shah, F. U. Khan, M. T. Khan, S. Khan, Experimental Study of Direct Laser Deposition of Ti-6Al-4V and Inconel 718 by Using Pulsed Parameters, *The Scientific World Journal* 2014 (2014) 841549. doi:10.1155/2014/841549.
- [5] A. Saboori, A. Aversa, G. Marchese, S. Biamino, M. Lombardi, P. Fino, Application of directed energy deposition-based additive manufacturing in repair, *Applied Sciences* 9 (16) (2019) 3316. doi:10.3390/app9163316.
- [6] F. Bruzzo, G. Catalano, A. G. Demir, B. Previtali, Surface finishing by laser re-melting applied to robotized laser metal deposition, *Optics and Lasers in Engineering* 137 (2021) 106391. doi:10.1016/j.optlaseng.2020.106391.
- [7] N. Shamsaei, A. Yadollahi, L. Bian, S. M. Thompson, An overview of Direct Laser Deposition for additive manufacturing; Part II: Mechanical behavior, process parameter optimization and control, *Additive Manufacturing* 8 (2015) 12–35. doi:10.1016/j.addma.2015.07.002.

- [8] D. Eisenbarth, F. Soffel, K. Wegener, Geometry-Based Process Adaption to Fabricate Parts with Varying Wall Thickness by Direct Metal Deposition, in: H. A. Almeida, J. C. Vasco (Eds.), *Progress in Digital and Physical Manufacturing, Lecture Notes in Mechanical Engineering*, Springer International Publishing, Cham, 2020, pp. 125–130. doi:10.1007/978-3-030-29041-2_16.
- [9] S. M. Thompson, L. Bian, N. Shamsaei, A. Yadollahi, An overview of Direct Laser Deposition for additive manufacturing: Part I: Transport phenomena, modeling and diagnostics, *Additive Manufacturing* 8 (2015) 36–62. doi:10.1016/j.addma.2015.07.001.
- [10] L. Costa, R. Vilar, T. Reti, A. M. Deus, Rapid tooling by laser powder deposition: Process simulation using finite element analysis, *Acta Materialia* 53 (14) (2005) 3987–3999. doi:10.1016/j.actamat.2005.05.003.
- [11] N. Pirch, S. Linnenbrink, A. Gasser, H. Schleifenbaum, Laser-aided directed energy deposition of metal powder along edges, *International Journal of Heat and Mass Transfer* 143 (2019) 118464. doi:10.1016/j.ijheatmasstransfer.2019.118464.
- [12] L. Song, V. Bagavath-Singh, B. Dutta, J. Mazumder, Control of melt pool temperature and deposition height during direct metal deposition process, *The International Journal of Advanced Manufacturing Technology* 58 (1-4) (2012) 247–256. doi:10.1007/s00170-011-3395-2.
- [13] A. Fathi, A. Khajepour, E. Toyserkani, M. Durali, Clad height control in laser solid freeform fabrication using a feedforward PID controller, *The International Journal of Advanced Manufacturing Technology* 35 (3-4) (2007) 280–292. doi:10.1007/s00170-006-0721-1.
- [14] L. Tang, R. G. Landers, Layer-to-Layer Height Control for Laser Metal Deposition Process, *Journal of Manufacturing Science and Engineering* 133 (2) (2011) 021009. doi:10.1115/1.4003691.
- [15] A. Heralić, A.-K. Christiansson, B. Lennartson, Height control of laser metal-wire deposition based on iterative learning control and 3D scanning, *Optics and Lasers in Engineering* 50 (9) (2012) 1230–1241. doi:10.1016/j.optlaseng.2012.03.016.
- [16] M. Kogel-Hollacher, M. Strebel, C. Staudenmaier, H.-I. Schneider, D. Regulin, OCT sensor for layer height control in DED using SINUMERIK® controller, in: *Laser 3D Manufacturing VII*, Vol. 11271, International Society for Optics and Photonics, 2020, p. 112710O. doi:10.1117/12.2540167.
- [17] W. U. H. Syed, A. J. Pinkerton, L. Li, A comparative study of wire feeding and powder feeding in direct diode laser deposition for rapid prototyping, *Applied Surface Science* 247 (1) (2005) 268–276. doi:10.1016/j.apsusc.2005.01.138.
- [18] C. P. Paul, S. K. Mishra, A. Kumar, L. M. Kukreja, Laser rapid manufacturing on vertical surfaces: Analytical and experimental studies, *Surface and Coatings Technology* 224 (2013) 18–28. doi:10.1016/j.surfcoat.2013.02.044.
- [19] J. Lin, A simple model of powder catchment in coaxial laser cladding, *Optics & Laser Technology* 31 (3) (1999) 233–238. doi:10.1016/S0030-3992(99)00046-8.
- [20] S. Cacace, V. Furlan, R. Sorci, Q. Semeraro, M. Boccadoro, Using recycled material to produce gas-atomized metal powders for additive manufacturing processes, *Journal of Cleaner Production* 268 (2020) 122218. doi:10.1016/j.jclepro.2020.122218.
- [21] T. Li, L. Zhang, G. G. P. Bultel, T. Schopphoven, A. Gasser, J. H. Schleifenbaum, R. Poprawe, Extreme High-Speed Laser Material Deposition (EHLA) of AISI 4340 Steel, *Coatings* 9 (12) (2019) 778. doi:10.3390/coatings9120778.
- [22] D. Eisenbarth, P. M. Borges Esteves, F. Wirth, K. Wegener, Spatial powder flow measurement and efficiency prediction for laser direct metal deposition, *Surface and Coatings Technology* 362 (2019) 397–408. doi:10.1016/j.surfcoat.2019.02.009.
- [23] S. Donadello, M. Motta, A. G. Demir, B. Previtali, Monitoring of laser metal deposition height by means of coaxial laser triangulation, *Optics and Lasers in Engineering* 112 (2019) 136–144. doi:10.1016/j.optlaseng.2018.09.012.
- [24] A. J. Pinkerton, L. Li, The significance of deposition point standoff variations in multiple-layer coaxial laser cladding (coaxial cladding standoff effects), *International Journal of Machine Tools and Manufacture* 44 (6) (2004) 573–584. doi:10.1016/j.ijmachtools.2004.01.001.
- [25] G. Zhu, D. Li, A. Zhang, G. Pi, Y. Tang, The influence of laser and powder defocusing characteristics on the surface quality in laser direct metal deposition, *Optics & Laser Technology* 44 (2) (2012) 349–356. doi:10.1016/j.optlastec.2011.07.013.
- [26] J. C. Haley, B. Zheng, U. S. Bertoli, A. D. Dupuy, J. M. Schoenung, E. J. Lavernia, Working distance passive stability in laser directed energy deposition additive manufacturing, *Materials & Design* 161 (2019) 86–94. doi:10.1016/j.matdes.2018.11.021.
- [27] H. Tan, W. Shang, F. Zhang, A. T. Clare, X. Lin, J. Chen, W. Huang, Process mechanisms based on powder flow spatial distribution in direct metal deposition, *Journal of Materials Processing Technology* 254 (2018) 361–372. doi:10.1016/j.jmatprotec.2017.11.026.
- [28] P.-Y. Lin, F.-C. Shen, K.-T. Wu, S.-J. Hwang, H.-H. Lee, Process optimization for directed energy deposition of SS316L components, *The International Journal of Advanced Manufacturing Technology* doi:10.1007/s00170-020-06113-z.
- [29] Y. Huang, M. B. Khamesee, E. Toyserkani, A new physics-based model for laser directed energy deposition (powder-fed additive manufacturing): From single-track to multi-track and multi-layer, *Optics & Laser Technology* 109 (2019) 584–599. doi:10.1016/j.optlastec.2018.08.015.
- [30] V. Ocelík, O. Nenadl, A. Palavra, J. T. M. De Hosson, On the geometry of coating layers formed by overlap, *Surface and Coatings Technology* 242 (2014) 54–61. doi:10.1016/j.surfcoat.2014.01.018.
- [31] Z. Sun, W. Guo, L. Li, In-process measurement of melt pool cross-sectional geometry and grain orientation in a laser directed energy deposition additive manufacturing process, *Optics & Laser Technology* 129 (2020) 106280. doi:10.1016/j.optlastec.2020.106280.
- [32] Y. Huang, M. B. Khamesee, E. Toyserkani, A comprehensive analytical model for laser powder-fed additive manufacturing, *Additive Manufacturing* 12 (2016) 90–99. doi:10.1016/j.addma.2016.07.001.

- [33] J. Song, Y. Chew, G. Bi, X. Yao, B. Zhang, J. Bai, S. K. Moon, Numerical and experimental study of laser aided additive manufacturing for melt-pool profile and grain orientation analysis, *Materials & Design* 137 (2018) 286–297. doi:10.1016/j.matdes.2017.10.033.
- [34] S. Kumar, V. Sharma, A. K. S. Choudhary, S. Chattopadhyaya, S. Hloch, Determination of layer thickness in direct metal deposition using dimensional analysis, *The International Journal of Advanced Manufacturing Technology* 67 (9) (2013) 2681–2687. doi:10.1007/s00170-012-4683-1.
- [35] A. F. H. Kaplan, G. Groboth, Process analysis of laser beam cladding, *Journal of Manufacturing Science and Engineering* 123 (4) (2001) 609–614. doi:10.1115/1.1344899.
- [36] C. Zhong, T. Biermann, A. Gasser, R. Poprawe, Experimental study of effects of main process parameters on porosity, track geometry, deposition rate, and powder efficiency for high deposition rate laser metal deposition, *Journal of Laser Applications* 27 (4) (2015) 042003. doi:10.2351/1.4923335.
- [37] W. M. Steen, J. Mazumder, *Laser Material Processing*, Springer London, London, 2010. doi:10.1007/978-1-84996-062-5.
- [38] H. Tan, F. Zhang, X. Fu, J. Meng, G. Hu, W. Fan, W. Huang, Development of powder flow model of laser solid forming by analysis method, *The International Journal of Advanced Manufacturing Technology* 82 (5) (2016) 1421–1431. doi:10.1007/s00170-015-7481-8.
- [39] S. Donadello, M. Motta, A. G. Demir, B. Previtali, Coaxial laser triangulation for height monitoring in laser metal deposition, in: *Procedia CIRP*, Vol. 74 of Proceedings of the 10th CIRP conference on photonic technologies, LANE, 2018, pp. 144–148. doi:10.1016/j.procir.2018.08.066.

Supplementary Material for the article “Interplay between powder catchment efficiency and layer height in self-stabilized laser metal deposition”

Simone Donadello, Valentina Furlan,
Ali Gökhan Demir, Barbara Previtali

1 Details of the model

The main steps and quantities involved in the semi-analytical model described in the main text are summarized in Figure 1. Some specific aspects of the model are discussed in the following sections.

1.1 Deposition track cross-section

Referring to Figure 2, the cross-section area of a generic deposition track can be expressed as

$$A_{cs} = k_g w_t h_t \quad (1)$$

where h_t and w_t are the single track height and width, while k_g is a geometrical factor which depends on the track shape. E.g., in case of a half-elliptical track $k_g = \frac{\pi}{4}$, while for a rectangular track $k_g = 1$.

A requirement for a bulk deposition without empty volumes is that the single track width must exceed the path transverse increment r_x , thus $w_t > r_x$. This is a necessary condition for a partial overlap between each newly deposited track and the previous one within the same layer, introducing the overlapping factor as $0 < (w_t - r_x)/w_t < 1$. Therefore r_x is relevant for the determination of the bulk cross-section area A_{cs} , since it influences the effective track width and height. This can be understood considering that, in the presence of track overlapping, the incoming powder flow contributes to the height growth over the whole deposition region, hence also over the previous track.

From purely considerations and in the assumption of a stationary process, i.e. with the track width w_t and height h_t not varying significantly within the same layer, the average contribution given by each track to the layer deposition is equivalent to a

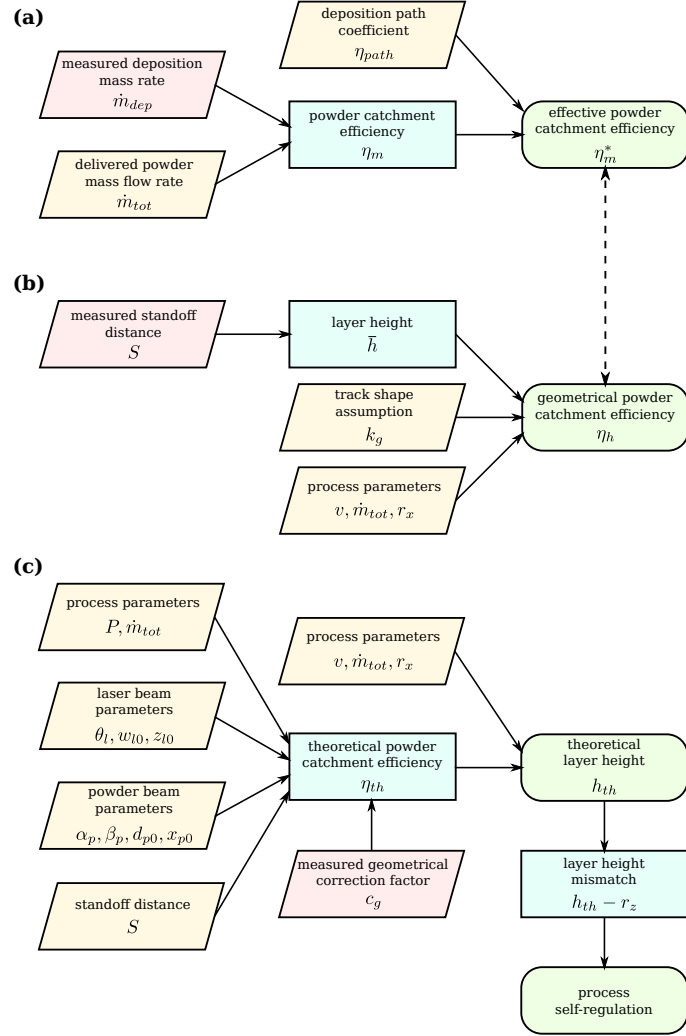


Figure 1: Main steps of the powder catchment efficiency models presented in the text.

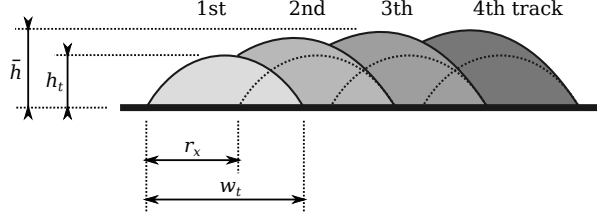


Figure 2: Qualitative cross-section representation of partially overlapping deposition tracks.

rectangular cross-section whose dimensions are set by the path transverse increment r_x and by the average layer height \bar{h} . Therefore, under the previous hypotheses, $k_g = 1$ and the cross-section area of Eq. (1) averaged over a multi-track layer becomes

$$\bar{A}_{cs} \simeq r_x \bar{h}. \quad (2)$$

If N_t is the track number for each layer, the error introduced by such approximation is of the order of $w_t \bar{h} / N_t$, whose contribution is negligible if the number of tracks which compose the layer is sufficiently big. This is a realistic condition for bulk depositions with $N_t \gg 1$.

1.2 Deposition layer height

Considering a multi-track multi-layer deposition, and referring to Figure 3, the average standoff distance \bar{S}_n for the n -th layer can be expressed as

$$\bar{S}_n = S_0 + R_{z,n} - \bar{H}_n \quad (3)$$

where S_0 is the initial standoff distance value, $R_{z,n}$ is the relative robot height coordinate after n layers, and \bar{H}_n is the deposited structure height averaged within the considered layer. During the evolution of the deposition process the standoff distance can drift from its initial value due to instabilities in the deposition height, i.e. when the deposition path does not match the deposition growth and $R_{z,n} \neq \bar{H}_n$.

The deposit height \bar{H}_n at layer n is the sum of the layer height \bar{h}_i for all the previous layers $i = 1 \dots n$, thus

$$\bar{H}_n = \sum_{i=1}^n \bar{h}_i. \quad (4)$$

Analogously, the robot height coordinate R_n at layer n is the sum of the robot height increment $r_{z,i}$ for i ranging from 1 to n . Here $r_{z,i} = r_z$ is considered a constant parameter during the whole deposition, thus

$$R_{z,n} = \sum_{i=1}^n r_{z,i} = n r_z. \quad (5)$$

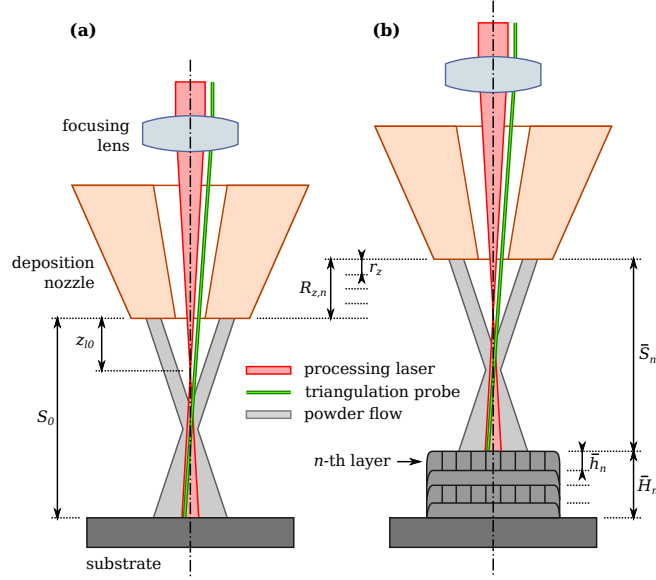


Figure 3: Schematic representation of the main dimensions related to a multi-layer deposition height in the initial condition (a) and after n layers (b).

It follows that the n -th layer height can be calculated from standoff distance differentiation as

$$\bar{h}_n = \bar{H}_n - \bar{H}_{n-1} = r_z + \bar{S}_{n-1} - \bar{S}_n. \quad (6)$$

1.3 Powder beam geometry

The study presented in the main text considers a three-jet nozzle, composed of 3 powder streams arranged with axial symmetry at 120° . Each of the 3 powder jets can be seen as a cone having divergence angle $2\alpha_p$ outgoing from the nozzle tip as shown in Figure 4, with the cone axis tilted by β_p relatively to the transverse plane. The diameter d_{p0} of the powder delivery channel at the nozzle tip exit is assumed as a constrain for the powder cone basis at $S = 0$, whose center lays at distance x_{p0} from the origin placed in the nozzle tip center. Since β_p , d_{p0} and x_{p0} are known from the nozzle geometry, while α_p can be determined experimentally by observing the powder flow with a camera, the coordinates of the hypothetical powder cone apex relatively to the nozzle tip center can be extrapolated as

$$\begin{aligned} x_{p1} &= \frac{d_{p0}}{2} \frac{\cos \beta_p}{\tan \alpha_p} + x_{p0} \\ z_{p1} &= \frac{d_{p0}}{2} \frac{\sin \beta_p}{\tan \alpha_p}. \end{aligned} \quad (7)$$

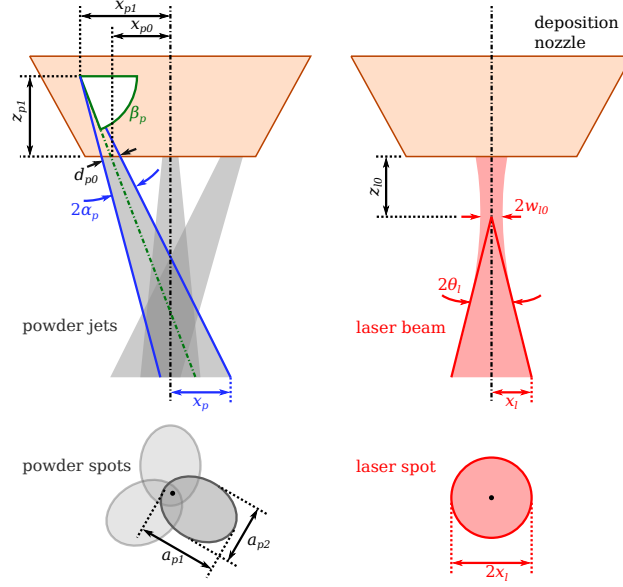


Figure 4: Qualitative side view of the powder nozzle, highlighting the dimensions related to the powder jets (left) and to the laser beam (right). The corresponding powder and laser spots in the transverse plane are represented in the bottom.

Under the previous assumptions and referring to Figure 4, it can be demonstrated that the major axis of the elliptical transverse section for each powder cone at a generic standoff distance $S > 0$ is

$$a_{p1} = (S + z_{p1}) \left(\frac{1}{\tan(\beta_p - \alpha_p)} - \frac{1}{\tan(\beta_p + \alpha_p)} \right). \quad (8)$$

The corresponding minor axis is

$$a_{p2} = 2(S + z_{p1}) \frac{\tan \alpha_p}{\sin \beta_0}. \quad (9)$$

Accordingly, the effective total area for the 3 elliptical powder sections is

$$A_p = \frac{3\pi}{4} a_{p1} a_{p2}. \quad (10)$$

2 Details of the experimental setup

2.1 Powder beam characterization

The dispersion angle of a single powder jet for the three-jet nozzle used in the LMD setup was determined experimentally by means of offline characterization, in absence of the processing laser emission. Indeed, the powder flow was acquired using a high-speed CMOS camera (Photron Fastcam Mini AX200) at 1 ms shutter time, considering the same conditions used for the experiments in terms of mass flow rate, carrier gas flow, and shielding gas flow. External illumination was used to highlight the trajectories of the powder particles, using a high-power white LED lamp. An example of image is reported in Figure 5. The half-dispersion $\alpha_p \sim 6^\circ$ was estimated as the angle which contained the 98 % of the powder particles for a single jet.

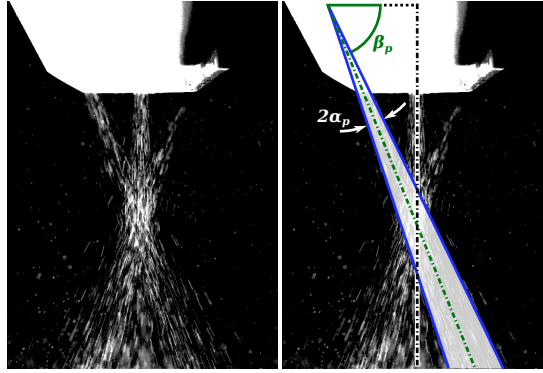


Figure 5: Image of the 3 powder jets spreading from the deposition nozzle. The characteristic angles for a single powder cone are highlighted on the right.

2.2 Mass measurement system

The system for the real-time measurement of the deposition mass is based on two load cell devices. Each load cell includes four strain gauges connected in a Wheatstone bridge configuration, insensitive to the distance of force application along the cell bar. The strain gauge bridge signal is amplified with an instrumentation amplifier circuit (Texas Instruments INA125P).

The dimension of the substrate is fitted to the programmed deposition path, allowing the unmelted powder to fall without accumulating on the substrate itself. The first load cell measures the mass of the substrate and of the deposited material, while the second load cell measures the mass of the lost powder collected by a hopper.

The hopper is made of brass sheet with 0.9 mm thickness. The choice of the material is related to the high heat dissipation of brass, which is important due to the high temperatures reached around the process region. The hopper implemented a self-balancing tip system, centered in the center of mass of a vessel which collected

the unmelted powder. The structure is also equipped with an anti-rotation system, consisting of an aluminum bar with two adjustable screws, that ensure greater stability during the deposition process by blocking excessive rotations of the brass vessel.

Thermal insulation has been treated carefully in the setup design. Indeed, the load cells can operate in a limited temperature range, up to 50 °C, and their readout can be strongly influenced by temperature variations. For this reason the load cells are placed far from the process region to avoid thermal damaging. The load cells are connected to the deposition substrate and to the powder hopper by insulating glass bars to suppress thermal conduction. Moreover the measurement setup is shielded from irradiation by aluminum foils.

The readout voltages of the load cells were calibrated using a set of standard masses, finding a proportionality factor of 0.086 V/g for the substrate cell, and of 0.0191 V/g for the hopper cell, on a scale ranging between 0 V and 10 V.

Possible thermal effects which might perturb the acquisitions were monitored using an analog temperature sensor placed close to the load cell. In fact a temperature dependence was observed above 30 °C while calibrating the load cell. However, thanks to the thermal shielding implemented in the setup, the temperature remained almost stable even in presence of the high-power processing laser radiation during long depositions. An average temperature of (28.0 ± 1.1) °C was maintained over the whole experimental campaign. This allowed to neglect the influence of ambient temperature on the mass measurements.

2.3 Coaxial triangulation system

The deposition height measurements were performed by means of triangulation system in a custom coaxial configuration. A 532 nm 4.5 mW probe laser is integrated in the deposition head optical chain, accessible through a lateral monitoring port. The collimated probe beam is deflected along the deposition optical axis by a dichroic mirror, transparent for the high-power laser wavelength, partially reflective in the visible and near-infrared (NIR) spectrum. The probe beam propagates to the 200 mm focal length lens of the deposition head in a slightly off-axis configuration, hence it gets focused with a non-zero deflection while exiting from the deposition nozzle orifice, as represented in Figure 3. This introduces a dependence of the transverse probe spot position on the standoff distance. The probe alignment offset of few mm relatively to the lens axis is chosen in order to get a small deflection angle, allowing to keep the probe spot within the melt pool considering the typical standoff distance variations during the deposition process.

The probe radiation which gets scattered from the melt pool surface is collected by the focusing lens, and back-deflected toward the monitoring port by the deposition head dichroic mirror. The beam crosses a further dichroic shortpass mirror with 650 nm cutoff, used for monitoring techniques in the NIR spectrum such as pyrometry or melt pool imaging, not considered in the current work. Half of the scattered probe radiation is deflected by a 50:50 beam splitter cube towards an iris used for spatial filtering. A 532 nm bandpass filter is used to eliminate spurious radiation. A compact Galilean-like telescope configuration is obtained by combining a 100 mm plano-convex lens with

a -25 mm bi-concave lens. Finally the probe spot is imaged on a 1.3 MP CMOS camera having $4.8\text{ }\mu\text{m}$ pixel size (Ximea XiQ MQ013MG-ON).

The probe spot position has been calibrated as a function of known standoff distances, finding a sensitivity factor of 0.106 mm/pixel over a 20 mm standoff distance range. The camera was triggered for the acquisition at 400 Hz frame rate, cropping the sensor to a 420×96 pixel area. The shutter time was limited for a short exposition time of 1 ms , thanks to the efficient light collection guaranteed by the $1''$ clear aperture of the monitoring optical chain.

The images were acquired by means of USB3 interface using a dedicated computer. A Python algorithm was used to extract the standoff distance in real-time during the process. The main steps performed for each frame are the following:

- the image is integrated along the short image axis, obtaining a 1D intensity vector along the probe beam deflection plane;
- the probe spot position and size are extracted efficiently as the vector distribution moments;
- finally the standoff distance is calculated applying a calibration curve, and stored for post-processing.

2.4 Positioning accuracy

An example of acquisition of standoff distance during the deposition of a cuboid sample is represented in 3D in Figure 6. It can be seen that the standoff distance departs from its initial nominal value $S_0 = 12\text{ mm}$ after the first layers, with the color scale gradient showing an initially faster deposition growth and a final height mismatch of about 3 mm . The observed track-to-track and layer-to-layer variability can be ascribed to inaccuracies in the robot positioning and to laser head vibrations. These were quantified from the logs of the acquired robot axis encoders. The average standard deviation for the robot height within each layer was of the order of $70\text{ }\mu\text{m}$; moreover, the robot height increment exhibited a standard deviation of about $30\text{ }\mu\text{m}$ relatively to its nominal value $r_z = 0.2\text{ mm}$, with peak mismatches up to 0.1 mm . Clearly these mechanical inaccuracies reflect on the optical distance measurement, influencing also the process conditions related to standoff distance. The robot positioning inaccuracies may play an important role at borderline conditions of process stability, since the standoff distance vibrations can eventually bring the deposition to operate in an actual condition of instability.

2.5 Model calibration and path efficiency

The parameters of the experimental conditions considered in the main text are reported in Table 1. The same table reports the calibration factor c_g , found by fitting the model for the powder catchment efficiency η_{th} to the experimental data of $\bar{\eta}_h$ in the different conditions. Finally, the table reports the efficiency coefficient η_{path} for η_m , related to the intervals of actual processing laser emission during the deposition time and measured from the robot control system.

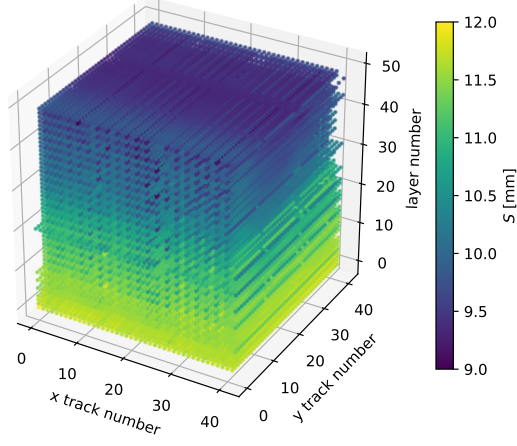


Figure 6: Three-dimensional representation of a deposited sample for the experimental condition C5 as defined in the main text. The color scale represents the measured standoff distance.

Table 1: Parameters of the considered process conditions, with the respective correction factors c_g from model calibration and deposition path coefficients η_{path} for the powder catchment efficiency.

Label	P [W]	\dot{m}_{tot} [g/s]	v [mm/s]	c_g	η_{path}
■ C1	612	0.16	32	2.25 ± 0.02	0.549
■ C2	700	0.22	22	2.35 ± 0.04	0.586
■ C3	700	0.22	42	2.42 ± 0.02	0.500
■ C4	700	0.11	22	2.26 ± 0.03	0.586
■ C5	700	0.11	42	2.24 ± 0.02	0.500
■ C6	525	0.22	22	2.24 ± 0.03	0.586
■ C7	525	0.22	42	2.09 ± 0.02	0.500
■ C8	525	0.11	22	2.06 ± 0.02	0.586
■ C9	525	0.11	42	1.85 ± 0.01	0.500