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14 **An uncertainty spreadsheet for the k_0 -standardisation**
15 **method in Neutron Activation Analysis**

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21 **Abstract**

22 This paper focuses on the use of the spreadsheet technique to set up the uncertainty budget
23 for the k_0 -standardisation method in Neutron Activation Analysis. The adopted
24 measurement model included most of presently recognized error sources and was written
25 to limit the covariances between input quantities. The calculations were implemented in a
26 worksheet file and tested in a multi-elemental analysis of a biological material. Besides, it
27 was demonstrated that the k_0 -standardisation turns to the relative-standardisation when the
28 monitor element corresponds to the analyte element. The developed worksheet is available
29 and suitable for the analysis of other materials in different experimental conditions.

30 **Keywords**

31 k_0 -standardisation method, uncertainty budget, spreadsheet technique, correlated input
32 quantities, cerebrospinal fluid

33 **Introduction**

34 In 1995, a guide was published by EURACHEM/CITAC [1] to illustrate the use in
35 chemistry measurements of the general rules outlined in the Guide to the Expression of

36 Uncertainty in Measurement (GUM) [2] for the evaluation and expression of uncertainty.
37 Afterwards, since specific applications in nuclear chemistry measurements were missing
38 in the guide, practical examples for the most common nuclear analytical techniques were
39 included in a report of the International Atomic Energy Agency (IAEA) [3].

40 The Neutron Activation Analysis (NAA) was addressed in the IAEA report, as regards the
41 existing standardisation methods, i.e. the relative- and k_0 -NAA. A detailed list of sources
42 of error were identified and grouped in four categories: i) preparation of samples, ii)
43 neutron irradiation, iii) γ -spectrometry measurements and iv) radiochemical separation, if
44 executed. Two uncertainty budgets were given as examples for the relative-NAA, the first
45 dealing with vanadium in coal fly ash by Instrumental NAA (INAA) and the latter with
46 manganese in animal freeze dried blood by Radiochemical NAA (RNAA). Only one
47 example for the k_0 -NAA was cited, with a reference to the (preliminary) evaluation
48 performed by de Corte [4].

49 Next, several studies focused on the k_0 -NAA. Robouch et al [5] suggested the use of the
50 spreadsheet technique developed by Kragten [6] and recommended a general equation to
51 express the uncertainty of the results. Younes et al [7] showed that the sensitivity
52 coefficients, computed by finite difference approximations in the spreadsheet technique,
53 could also be expressed in analytical form. In fact, subsequent works were all based on
54 analytical expressions of the sensitivity coefficients [8, 9].

55 To date, the most comprehensive examples of uncertainty budgets for k_0 -NAA were
56 reported in [9] and concerned the determination of Au, Cr, Rb and Sb in compressed
57 cellulose pellets. The covariances between input quantities, in practice always neglected in
58 the previously available literature, were to some extent considered. However, values and
59 expressions of correlation and sensitivity coefficients were omitted.

60 In this study, we adopted a measurement equation modeling most of the acknowledged
61 sources of error and written to limit the covariances. Due to the complexity of the resulting
62 functional relationship, we used the spreadsheet technique and the matrix formalism to
63 propagate the uncertainties, including the outstanding correlations. The formulae were
64 implemented and tested for the determination of trace elements in a biological material.

65 Details on the neutron activation experiment as well as on the characterization of the
66 detection system are here presented to assign estimates, uncertainties and correlation
67 coefficients of the input quantities. Lastly, the uncertainty budgets are briefly discussed to
68 point out the main contributors to the combined uncertainties of the results.

69 **Model**

70 The theoretical basis of k_0 -NAA is well established and extensively reported in literature.
71 Simonits et al. proposed the original idea in 1975 [10] following a preliminary study carried
72 out by Girardi et al. [11]. In 1987, de Corte published the most comprehensive development
73 of the method [4], including references to previous papers focused on definitions and
74 assumptions of the standardisation. Here, the basic concepts are briefly recalled to term the
75 input quantities of the measurement model.

76 The formalism underlying the method is based on a rather simple description of the reaction
77 rate per target nuclide, R , following the Høgdahl convention [12] in the case of a (target)
78 nuclide having a $1/E^{1/2}$ dependence of the (n,γ) cross section function, $\sigma(E)$, versus the
79 neutron energy, E .

80 According to the convention, the neutron spectrum is divided in the sub- and epi-cadmium
81 regions, respectively below and above the cadmium cut-off energy fixed to 0.55 eV. The
82 fission component is neglected under the hypothesis that the corresponding contribution to
83 R is small. Accordingly:

$$84 \quad R = G_{\text{th}} \Phi_s \sigma_0 + G_e \Phi_e I_0(\alpha), \quad (1)$$

85 where Φ_s and Φ_e are the (conventional) sub- and epi-cadmium neutron fluxes, G_{th} and G_e
86 are correction factors accounting for the thermal and epithermal neutron self-shielding, σ_0
87 is the thermal cross section, and $I_0(\alpha)$ is the resonance integral for a $1/E^{1+\alpha}$ neutron
88 spectrum in the epi-cadmium region.

89 The knowledge of the time dependence of the amount of produced radionuclide during and
90 after activation combined to the counting of the emitted γ -photons links the number of

91 target nuclides in a sample, N_t , to the number of counts in the full-energy peak of the
 92 collected γ -spectrum, n_p , via R .

93 With the exception of branching activation and mother-daughter decay, and neglecting
 94 burn-up effects, the relation between N_t and n_p is:

$$95 \quad R N_t \varepsilon_p^{\text{geo}} P_\gamma = \frac{\lambda n_p (\delta \xi / \text{COI})}{(1 - e^{-\lambda t_i}) e^{-\lambda t_d} (1 - e^{-\lambda t_c})}, \quad (2)$$

96 where $R N_t$ is the total reaction rate, $\varepsilon_p^{\text{geo}}$ is the full-energy γ -peak detection efficiency for
 97 the actual position and geometry of the sample, P_γ is the absolute emission probability of
 98 the γ -photons, t_c and t_i are the counting and live times of the detection system, t_i is the
 99 irradiation time, t_d is the decay time after irradiation, COI is the true-coincidence
 100 correction factor, $\lambda = \ln(2) / t_{1/2}$ is the decay constant of the produced radionuclide, given
 101 its half-life $t_{1/2}$, $\delta = t_c / t_i$ is the dead time correction factor and $\xi = e^{\mu(1 - t_i / t_c)}$ is the
 102 excess counting loss correction factor, given the excess counting loss constant of the
 103 detection system, μ , defined in [13].

104 In the case that the (target) nuclide is an isotope of an element in a m mass sample, N_t can
 105 be expressed as:

$$106 \quad N_t = \frac{w m x N_A}{M}, \quad (3)$$

107 where x is the abundance of the isotope, N_A is the Avogadro constant, and w and M are the
 108 mass fraction and molar mass of the element in the sample, respectively.

109 From eqs. (1), (2) and (3), it follows:

$$110 \quad \frac{\sigma_0 P_\gamma x N_A}{M} = \frac{\lambda n_p (\delta \xi / \text{COI})}{(1 - e^{-\lambda t_i}) e^{-\lambda t_d} (1 - e^{-\lambda t_c}) \varepsilon_p^{\text{geo}}} \frac{1}{m w \phi_s \left(G_{\text{th}} + \frac{G_e Q_0(\alpha)}{f} \right)}, \quad (4)$$

111 where $Q_0(\alpha) = I_0(\alpha) / \sigma_0$ and $f = \Phi_s / \Phi_e$. The $Q_0(\alpha)$ value is obtained by applying the
 112 formula $Q_0(\alpha) = (Q_0 - 0.429) \bar{E}_r^{-\alpha} + 0.429 / [0.55^\alpha (1 + 2\alpha)]$, where $Q_0 = I_0 / \sigma_0$ is the

113 ratio of the resonance integral (for a $1/E$ neutron spectrum in the epi-cadmium region) to
 114 the thermal cross section and \bar{E}_r is the effective resonance energy of the target nuclide.

115 It is worth remarking that the parameters on the left-hand side of (4) are independent of the
 116 experimental conditions of irradiation and γ -counting. In fact, the product $\sigma_0 P_\gamma N_A$ is a
 117 constant quantity and the ratio x/M depends on the isotopic composition.

118 The k_0 -NAA measurement model is derived from the application of (4) to the element to
 119 be quantified, i.e. the analyte, and to an element used as a monitor of the of the neutron
 120 fluence rate.

121 The following equation holds under the assumption that analyte and monitor are exposed
 122 to the same (constant) values of Φ_s and Φ_e during the irradiation:

$$123 \quad W_a = \frac{\left. \frac{\lambda n_p \delta \xi}{(1-e^{-\lambda t_i}) e^{-\lambda t_d} (1-e^{-\lambda t_c})} \right|_a}{\left. \frac{\lambda n_p \delta \xi}{(1-e^{-\lambda t_i}) e^{-\lambda t_d} (1-e^{-\lambda t_c})} \right|_m} k_{0 \text{ Au}}(m) \frac{(G_{\text{th } m} + \frac{G_{e m} Q_{0 m}(\alpha)}{f}) \varepsilon_{p m}^{\text{geo}} \text{COI}_m m_m}{k_{0 \text{ Au}}(a) (G_{\text{th } a} + \frac{G_{e a} Q_{0 a}(\alpha)}{f}) \varepsilon_{p a}^{\text{geo}} \text{COI}_a m_a} W_m, \quad (5)$$

124 where the parameters $k_{0 \text{ Au}}(m) = \frac{M_{\text{Au}} \sigma_{0 m} P_{\gamma m} x_m}{M_m \sigma_{0 \text{ Au}} P_{\gamma \text{ Au}} x_{\text{Au}}}$ and $k_{0 \text{ Au}}(a) = \frac{M_{\text{Au}} \sigma_{0 a} P_{\gamma a} x_a}{M_a \sigma_{0 \text{ Au}} P_{\gamma \text{ Au}} x_{\text{Au}}}$ are the
 125 so-called k_0 factors; subscripts a and m refer to the analyte and to the monitor, respectively.

126 The k_0 values have been experimentally determined for the most important (n, γ) reactions
 127 and γ -photons energies with respect to the 411 keV γ -photons emitted by ^{198}Au produced
 128 from ^{197}Au via (n, γ) reaction. A compilation of the recommended $k_{0 \text{ Au}}$, Q_0 and \bar{E}_r values
 129 can be found in [14].

130 **Experimental**

131 To exemplify the use of the equation model (5), we measured a lyophilized sample of
 132 cerebrospinal fluid (CSF). The experiment was intended to set up the uncertainty budget
 133 and not to reach the minimum uncertainty. The results were given in terms of mass

134 concentrations, $\rho_a = w_a/v$, where v is the factor used to convert the mass of lyophilized
135 CSF to the volume of reconstituted CSF.

136 *Preparation of the samples*

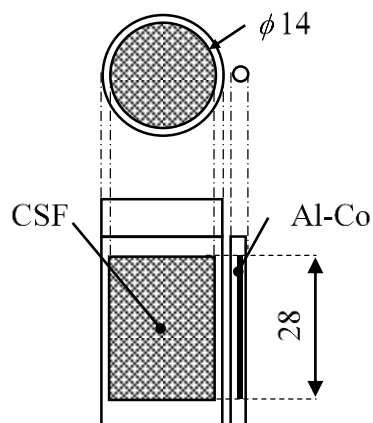
137 Ten vials of lyophilized CSF, each one corresponding to 3 mL volumes of reconstituted
138 CSF, were purchased. The content of every single vial was moved to an acid-cleaned 8 mL
139 cut polyethylene (PE) vial and sealed. The mass to volume conversion factor, $v =$
140 $99.2(12)$ mL g⁻¹, was obtained as the ratio of 3 mL to the average of the (ten) mass
141 differences between the filled and empty (washed and dried out) vials. Here and hereafter,
142 unless otherwise specified, the brackets refer to the standard uncertainty and apply to the
143 last digits.

144 One sample, about 28 mm length, of an Al-0.46%Co wire (Reactor Experiment, 99.9313%
145 purity, 0.38 mm diameter) was used as a Co monitor. The weighed mass, $m_m =$
146 $8.47(5)$ mg, was sealed in one PE micro-tube. A conservative 1% relative standard
147 uncertainty was assigned to the declared Co mass fraction value, $w_m = 4.597(46) \times$
148 10^{-3} g g⁻¹.

149 *Neutron irradiation*

150 The neutron irradiation lasted $t_i = 6.000(5)$ h and was performed in the 250 kW TRIGA
151 Mark II reactor at the Laboratory of Applied Nuclear Energy (LENA) of the University of
152 Pavia. The quoted uncertainty corresponds to a uniform probability distribution assigned
153 to the t_i value and having a 30 s half-width.

154 The vial containing the lyophilized CSF sample and the micro-tube containing the Al-Co
155 wire were put in one PE container used for irradiation and located in the central channel
156 (CC) of the reactor; the neutron flux parameters at CC, $f = 15.6(3)$ and $\alpha = -0.036(6)$, were
157 recently measured [15]. The position of the lyophilized CSF sample and of the Al-Co wire
158 during the irradiation is shown in Figure 1.



159

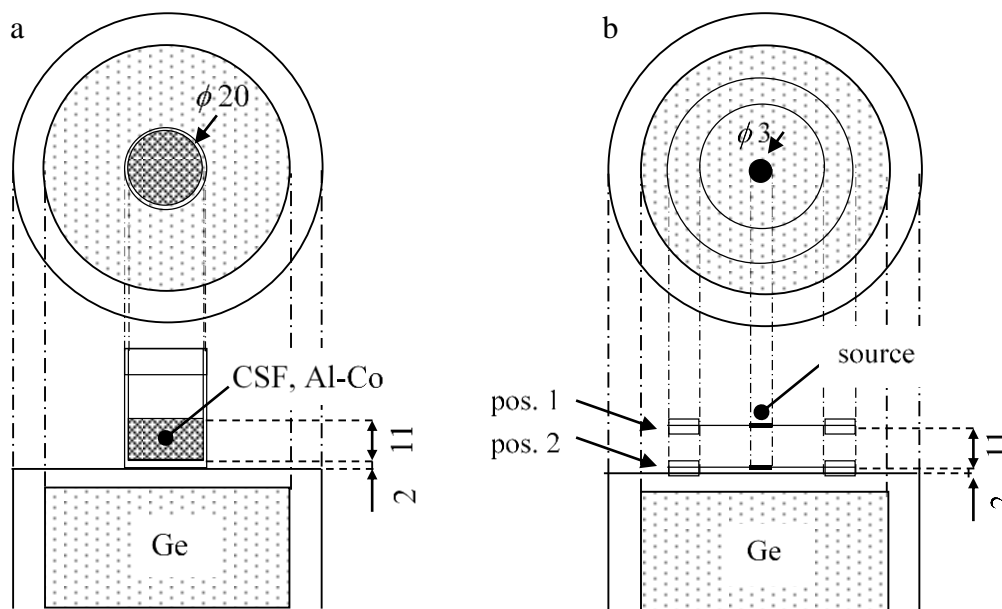
160 **Fig 1** Position of the lyophilized CSF sample and of the Al-Co wire during the
161 irradiation. Dimensions in mm

162 *Gamma spectrometry*

163 After irradiation, the lyophilized CSF sample was moved from its vial to a new 10 mL PE
164 vial and weighed; the mass, m_a , was found to be 240.00(5) mg, corresponding to 23.81(28)
165 mL volume of reconstituted CSF in the case of negligible effect due to humidity. The
166 relative loss of sample was about 20%, probably due to the lyophilized CSF residuals in
167 the vials. The Al-Co wire was removed from its micro-tube, placed in a new 10 mL vial
168 and dissolved using a few drops of nitric and hydrochloric acid (1:1) solution. After
169 complete digestion, water was added to obtain the same volume as the lyophilized CSF
170 sample.

171 The γ -spectra were recorded with a high purity germanium (HPGe) detector, ORTEC
172 GEM50P4-83 (relative efficiency 50%, resolution 1.90 keV at 1332 keV) inside a low-
173 background graded shield. The detector was connected to a digital signal processor ORTEC
174 DSPEC 502 and the data were collected and processed using the ORTEC Gamma Vision
175 software (version 6.08). The acquisition was performed in extended live-time correction
176 mode using the Gedcke-Hale method with pulse pile-up rejection in automatic set
177 threshold; the excess counting loss constant of the detection system, $\mu = 0.0445(5)$, was
178 recently measured [13].

179 The position of the lyophilized CSF and dissolved Al-Co wire samples with respect to the
 180 detector end-cap is shown in Figure 2a.



181 **Fig 2** Position of the lyophilized CSF and dissolved Al-Co wire samples (a), and of the
 182 disk source (b) with respect to the detector end-cap. Dimensions in mm

183 The collection of the γ -spectrum emitted by the CSF sample started at $t_{d\ a} =$
 184 667.890(10) h, lasted $t_{c\ a} = 359.0633(1)$ h and ended with a live time $t_{l\ a} =$
 185 351.1856(1) h. The dissolved Al-Co monitor was successively measured. The collection
 186 of the γ -spectrum started at $t_{d\ m} = 1034.10(1)$ h, lasted $t_{c\ m} = 797.0(3)$ s and ended with
 187 a live time $t_{l\ m} = 740.0(3)$ s. The quoted uncertainties correspond to uniform probability
 188 distributions assigned to the t_d , t_c and t_l values and having 60 s, 0.5 s and 0.5 s half-widths,
 189 respectively.

190 **Detection system characterization**

191 *Full-energy γ -peak detection efficiency*

192 The $\varepsilon_p^{\text{geo}}$ values in (5) depend on the actual position and geometry of the measured samples.
193 The dependence is strengthened when extensive samples are measured close to the detector
194 end-cap, as in this case.

195 In principle, the reconstruction of the $\varepsilon_p^{\text{geo}}$ versus the γ -energy, E_γ , might be performed by
196 measuring the γ -emissions of an extensive standard source having the same shape as the
197 analyte and monitor sample and located at the same position with respect to the detector
198 end-cap. In addition, the material of the source should have the same major elemental
199 composition as the monitor and analyte sample in order to mimic the γ self-absorption.

200 Actually, a more flexible procedure based on a computational technique coupled to a quasi-
201 point standard source measured at large source-detector distance is commonly adopted
202 [16]; geometries and major elemental composition of sample and layers between the Ge
203 crystal and sample are required.

204 As an approximated alternative, we recorded two γ -spectra with a disk standard source
205 positioned at the vertical ends of the measured extended samples, as shown in Figure 2b.
206 The efficiency of the (virtual) extensive source, $\varepsilon_p^{\text{ext}}$, was estimated by the average of the
207 disk efficiencies in positions 1 and 2, $\varepsilon_{p \text{ pos1}}^{\text{disk}}$ and $\varepsilon_{p \text{ pos2}}^{\text{disk}}$, respectively.

208 The coincidence free γ -emissions selected to reconstruct the efficiency curves were ^{241}Am
209 59.54 keV, ^{109}Cd 88.03 keV, ^{57}Co 122.06 keV, ^{139}Ce 165.86 keV, ^{113}Sn 391.70 keV, ^{137}Cs
210 661.66 keV, ^{54}Mn 834.85 keV and ^{65}Zn 1115.54 keV.

211 The $\varepsilon_{p \text{ pos1}}^{\text{disk}}$, $\varepsilon_{p \text{ pos2}}^{\text{disk}}$ and $\varepsilon_p^{\text{ext}}$ versus E_γ data were fitted by the equation model

212
$$\ln \varepsilon_p = a_1 E_\gamma + a_0 + a_{-1} E_\gamma^{-1} + a_{-2} E_\gamma^{-2} + a_{-3} E_\gamma^{-3}, \quad (6)$$

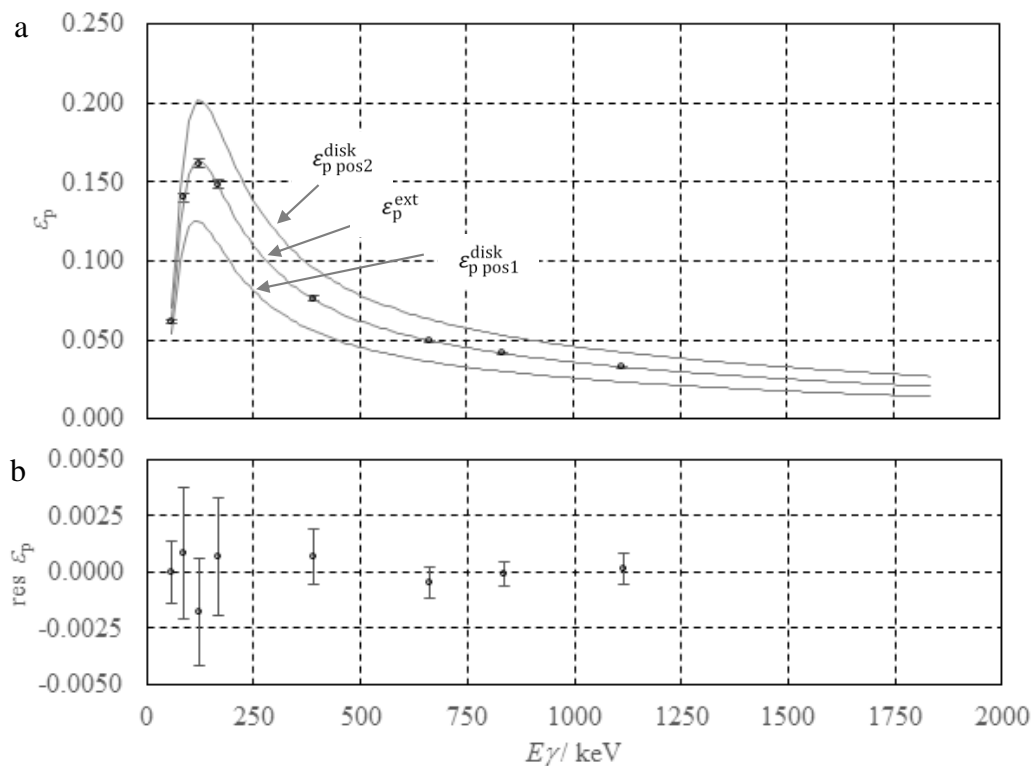
213 where a_1 , a_0 , a_{-1} , a_{-2} and a_{-3} are the fitting parameters. Best values, including
214 uncertainties and correlation matrix, were calculated using the algorithm implemented in
215 the OriginPro 2017.

216 The values obtained with the $\varepsilon_p^{\text{ext}}$ data were $a_1 = -4.72(43) \times 10^{-1} \text{ MeV}^{-1}$, $a_0 =$
 217 $-3.229(57)$, $a_{-1} = 4.03(20) \times 10^{-1} \text{ MeV}$, $a_{-2} = -3.20(22) \times 10^{-2} \text{ MeV}^2$, $a_{-3} =$
 218 $-5.73(75) \times 10^{-4} \text{ MeV}^3$; the corresponding correlation matrix is shown in Table 1.

219 **Table 1** Correlation matrix of the fitting
 220 parameters obtained with the $\varepsilon_p^{\text{ext}}$ data

	a_1	a_0	a_{-1}	a_{-2}	a_{-3}
a_1	1.000	-0.973	0.884	-0.804	0.748
a_0	-0.973	1.000	-0.957	0.896	-0.848
a_{-1}	0.884	-0.957	1.000	-0.984	0.957
a_{-2}	-0.804	0.896	-0.984	1.000	-0.993
a_{-3}	0.748	-0.848	0.957	-0.993	1.000

221 The $\varepsilon_{p \text{ pos1}}^{\text{disk}}$, $\varepsilon_{p \text{ pos2}}^{\text{disk}}$ and $\varepsilon_p^{\text{ext}}$ versus E_γ curves and the $\varepsilon_p^{\text{ext}}$ residuals are plotted in Figure 3a
 222 and Figure 3b, respectively. The error bars indicate a 95% confidence interval due to fitting,
 223 taking into account the correlations.



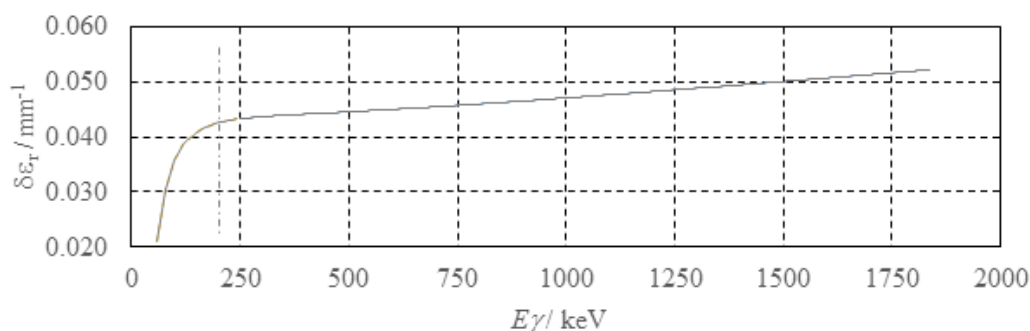
224 **Fig 3** $\varepsilon_{p \text{ pos2}}^{\text{disk}}$, $\varepsilon_p^{\text{ext}}$ and $\varepsilon_{p \text{ pos1}}^{\text{disk}}$ versus E_γ curves (a) and the residuals obtained with the $\varepsilon_p^{\text{ext}}$
 225 data (b). The error bars indicate a 95% confidence interval due to fitting

226 Possible differences in counting positions of the measured samples with respect to the
 227 (virtual) extensive source were considered according to:

$$228 \quad \frac{\varepsilon_{p\ m}^{\text{geo}}}{\varepsilon_{p\ a}^{\text{geo}}} = \frac{\varepsilon_{p\ m}^{\text{ext}} (1 - \delta\varepsilon_{r\ m} \Delta d_m)}{\varepsilon_{p\ a}^{\text{ext}} (1 - \delta\varepsilon_{r\ a} \Delta d_a)}, \quad (7)$$

229 where Δd_m and Δd_a are the vertical position differences between the dissolved Al-Co wire
 230 and the (virtual) extensive source and between the lyophilized CSF sample and the (virtual)
 231 extensive source, respectively, and $\delta\varepsilon_{r\ m}$ and $\delta\varepsilon_{r\ a}$ are the relative variations of the detection
 232 efficiency per unit of vertical position for the monitor and the analyte, respectively.

233 The $\delta\varepsilon_r$ values were obtained from the ratio of $(\varepsilon_{p\ \text{pos}2}^{\text{disk}} - \varepsilon_{p\ \text{pos}1}^{\text{disk}}) / \varepsilon_p^{\text{ext}}$ to the difference
 234 between the vertical positions 1 and 2, i.e. 11 mm, and plotted versus E_γ in Figure 4.



235

236 **Fig 4** $\delta\varepsilon_r$ versus E_γ curve. The vertical dashed line at about 240 keV splits the curve in
 237 two different regions

238 The data were fitted by $\delta\varepsilon_r = d_0 + d_1 E_\gamma$ and $\delta\varepsilon_r = e_0 + e_1 E_\gamma + e_2 E_\gamma^2 + e_3 E_\gamma^3 + e_4 E_\gamma^4$, for
 239 γ -energies above and below the 240 keV threshold, respectively. The resulting values were
 240 $e_4 = -7.10 \times 10^{-11} \text{ keV}^{-4}$, $e_3 = 5.19 \times 10^{-8} \text{ keV}^{-3}$, $e_2 = -1.43 \times 10^{-5} \text{ keV}^{-2}$, $e_1 =$
 241 $1.78 \times 10^{-3} \text{ keV}^{-1}$, $e_0 = -4.46 \times 10^{-2}$ and $d_1 = 5.56 \times 10^{-6} \text{ keV}^{-1}$, $d_0 = 4.17 \times$
 242 10^{-2} .

243 *Peak-to-total ratio*

244 True-coincidence occurs when two or more cascading γ -photons are emitted with
245 negligible time delay by a radionuclide. The effect becomes significant when samples are
246 measured close to the detector end-cap.

247 The number of counts collected in the full-energy γ -peak, n_p , is adjusted using the
248 correction factor

$$249 \quad \text{COI} = (1 - L_\gamma)(1 + S_\gamma), \quad (8)$$

250 where L_γ and S_γ are the overall probabilities for coincidence loss and summing,
251 respectively [4].

252 The formulae adopted to calculate L_γ and S_γ values depend on the cascade schemes and
253 include several nuclear parameters, the most important ones being the absolute emission
254 probability of the γ -photons, P_γ , the branching ratio, a_γ , and the total internal conversion
255 coefficient, α_t . In addition, $\varepsilon_p^{\text{geo}}$ and the peak-to-total ratio, P/T , of the detection system
256 are required.

257 E.g., the probability for coincidence loss of γ_A and γ_B in the case of $\gamma_A \rightarrow \gamma_B$ decay scheme
258 is

$$259 \quad L_{\gamma_A} = a_{\gamma_B} c_{\gamma_B} \frac{\varepsilon_p^{\text{geo}}}{(P/T)_{\gamma_B}} \text{ and } L_{\gamma_B} = \frac{P_{\gamma_A}}{P_{\gamma_B}} a_{\gamma_B} c_{\gamma_B} \frac{\varepsilon_p^{\text{geo}}}{(P/T)_{\gamma_A}}, \quad (9)$$

260 respectively, where $c_\gamma = 1/(1 + \alpha_{t\gamma})$, whereas the probability for coincidence summing
261 of γ_A with the $\gamma_B \rightarrow \gamma_C$ decay scheme is

$$262 \quad S_{\gamma_A} = \frac{P_{\gamma_B}}{P_{\gamma_A}} a_{\gamma_C} c_{\gamma_C} \frac{\varepsilon_p^{\text{geo}} \varepsilon_p^{\text{geo}}}{\varepsilon_p^{\text{geo}}}. \quad (10)$$

263 A compilation of the nuclear parameters values and the cascade schemes concerning the
264 radionuclides generally used in NAA are reported in [4].

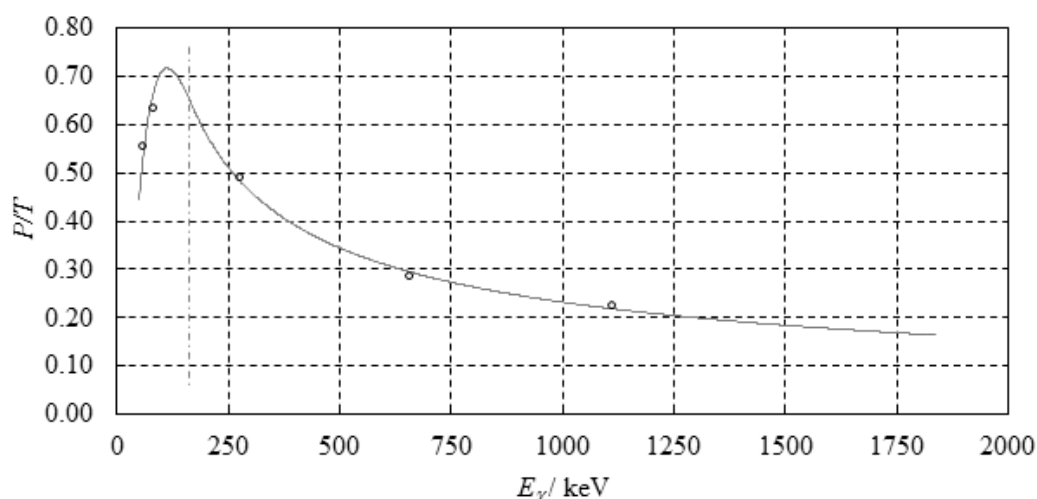
265 Similar to $\varepsilon_p^{\text{geo}}$, the P/T ratio versus E_γ data can be ideally obtained from γ -spectra of
266 coincidence free radionuclides embedded in extensive sources having the same material

267 and shape as the analyte and monitor sample and located at the same position with respect
268 to the detector end-cap. In practice, since the P/T ratio is above all depending on the
269 position and to a smaller extent on the composition and geometry of the samples, use of
270 quasi-point γ -sources might be accepted.

271 In this study, we used five γ -emissions, i.e. ^{241}Am 59.54 keV, ^{170}Tm 84.25 keV, ^{203}Hg
272 279.19 keV, ^{137}Cs 661.66 keV and ^{65}Zn 1115.54 keV, to reconstruct the P/T ratio curve.

273 The data were fitted by $\log P/T = b_0 + b_1 \log E_\gamma$ and $\log P/T = c_0 + c_1 \log E_\gamma +$
274 $c_2(\log E_\gamma)^2$, for γ -energies above and below the 170 keV threshold, respectively. To avoid
275 a discontinuity, the first derivative with respect to $\log E_\gamma$ of the latter equation model at
276 170 keV was imposed to be the b_1 value. The resulting values were $b_1 = -0.571$, $b_0 =$
277 1.079 , $c_2 = -1.625$, $c_1 = 6.678$ and $c_0 = -7.006$.

278 The P/T ratio versus E_γ curve is plotted in Figure 5.



279

280 **Fig 5** P/T ratio versus E_γ curve. The vertical dashed line at about 170 keV splits the
281 curve in two different regions

282 Results and discussion

283 The analysis of the γ -spectrum of the lyophilized CSF sample pointed out ^{233}Pa , ^{51}Cr , ^{131}Ba ,
284 ^{124}Sb , ^{46}Sc , ^{86}Rb , ^{59}Fe , ^{65}Zn and ^{60}Co γ -emissions produced by neutron capture reactions

285 from ^{232}Th , ^{50}Cr , ^{130}Ba , ^{123}Sb , ^{45}Sc , ^{85}Rb , ^{58}Fe , ^{64}Zn and ^{59}Co . The mass concentrations of
 286 the corresponding elements were quantified using the ^{60}Co γ -emission of the monitor.

287 The number of counts collected in the γ -peaks were evaluated with the algorithm
 288 implemented in the ROI32 analysis engine of the Gamma Vision software. The γ -peak
 289 energies and n_p values of the detected radionuclides in the CSF sample and monitor are
 290 reported in Table 2; the uncertainty (conservatively) assigned to E_γ corresponds to a
 291 uniform distribution with 0.2 keV half-width whereas the n_p uncertainty is due to counting
 292 statistics, including background.

293 **Table 2** γ -peak energies and corresponding number
 294 of counts of the detected radionuclides

Radionuclide	E_γ / keV	$n_p / 1$
$^{233}\text{Pa}^{(\text{CSF})}$	311.90(12)	$1.017(24) \times 10^5$
$^{51}\text{Cr}^{(\text{CSF})}$	320.10(12)	$5.26(15) \times 10^4$
$^{131}\text{Ba}^{(\text{CSF})}$	496.30(12)	$5.08(12) \times 10^4$
$^{124}\text{Sb}^{(\text{CSF})}$	1691.00(12)	$2.47(21) \times 10^2$
$^{46}\text{Sc}^{(\text{CSF})}$	889.30(12)	$1.3070(80) \times 10^5$
$^{86}\text{Rb}^{(\text{CSF})}$	1077.00(12)	$4.56(44) \times 10^3$
$^{59}\text{Fe}^{(\text{CSF})}$	1099.30(12)	$9.46(59) \times 10^3$
$^{65}\text{Zn}^{(\text{CSF})}$	1115.50(12)	$1.2260(47) \times 10^5$
$^{60}\text{Co}^{(\text{CSF})}$	1173.20(12)	$4.68(44) \times 10^3$
$^{60}\text{Co}^{(\text{monitor})}$	1173.20(12)	$1.3749(44) \times 10^5$

295 The full-energy γ -peak detection efficiencies ratio, $\varepsilon_{p\ m}^{\text{geo}}/\varepsilon_{p\ a}^{\text{geo}}$, was computed according to
 296 (7) using $a_1, a_0, a_{-1}, a_{-2}, a_{-3}$ and $d_1, d_0, e_0, e_1, e_2, e_3, e_4$ to obtain $\varepsilon_{p\ m}^{\text{ext}}/\varepsilon_{p\ a}^{\text{ext}}$ and $\delta\varepsilon_r$,
 297 respectively, as a function of E_γ . The uncertainty of the $\varepsilon_{p\ m}^{\text{ext}}/\varepsilon_{p\ a}^{\text{ext}}$ was evaluated taking into
 298 account uncertainties and correlations of the fitting parameters whereas a uniform
 299 probability distribution with a (conservative) 20% relative half-width was directly assigned
 300 to the $\delta\varepsilon_r$ value. In addition, it was assumed that the vertical position of the samples was
 301 within ± 0.5 mm with respect to the (virtual) extensive γ -source; accordingly, $\Delta d_m = \Delta d_a =$
 302 $0.00(29)$ mm, the quoted uncertainty corresponding to a uniform probability distribution
 303 having 0.5 mm half-width.

304 The true-coincidence correction factors ratio, $\text{COI}_m/\text{COI}_a$, was obtained via (8) using b_0 ,
 305 b_1 , c_0 , c_1 and c_2 to determine P/T as a function of E_γ . A uniform probability distribution
 306 with a (conservative) 20% relative half-width was directly assigned to the P/T value. The
 307 effect due to possible differences in counting positions was neglected; specifically, $\varepsilon_p^{\text{geo}}$
 308 was used instead of $\varepsilon_p^{\text{ext}}$ in (9) and (10). Cascade schemes, notations and P_γ , a_γ , α_t values
 309 proposed in [4] were adopted with uncertainties corresponding to uniform probability
 310 distributions having 0.0002, 0.02 and 0.02 half-widths, respectively.

311 A list of neutron capture reactions and $t_{1/2}$, $k_{0\text{Au}}$, Q_0 , \bar{E}_r values recommended in the k_0
 312 database [14] and used in this study are reported in Table 3 for reader's convenience.

313 **Table 3** Neutron capture reactions and adopted $t_{1/2}$, $k_{0\text{Au}}$, Q_0 , \bar{E}_r values.

Reaction	$t_{1/2}$ / h	$k_{0\text{Au}}$ / 1	Q_0 / 1	\bar{E}_r / eV
$^{232}\text{Th}(n,\gamma)^{233}\text{Pa}$	647.280(48)	$2.520(13) \times 10^{-2}$	11.50(41)	54.40(49)
$^{50}\text{Cr}(n,\gamma)^{51}\text{Cr}$	664.800(58)	$2.620(13) \times 10^{-3}$	0.53(11)	$753(83) \times 10^1$
$^{130}\text{Ba}(n,\gamma)^{131}\text{Ba}$	276.0(14)	$6.480(13) \times 10^{-5}$	24.8(50)	69.9(35)
$^{123}\text{Sb}(n,\gamma)^{124}\text{Sb}$	1444.80(72)	$1.410(16) \times 10^{-2}$	28.8(11)	28.2(18)
$^{45}\text{Sc}(n,\gamma)^{46}\text{Sc}$	2011.92(48)	1.2200(49)	0.430(86)	$513(87) \times 10^1$
$^{85}\text{Rb}(n,\gamma)^{86}\text{Rb}$	447.12(48)	$7.650(77) \times 10^{-4}$	14.80(37)	839(50)
$^{58}\text{Fe}(n,\gamma)^{59}\text{Fe}$	1068.00(14)	$7.770(39) \times 10^{-5}$	0.975(10)	$64(15) \times 10^1$
$^{64}\text{Zn}(n,\gamma)^{65}\text{Zn}$	5863.2(24)	$5.720(23) \times 10^{-3}$	1.91(10)	$256(26) \times 10^1$
$^{59}\text{Co}(n,\gamma)^{60}\text{Co}$	46207.2(72)	1.3200(53)	1.993(60)	136.0(69)

314 Values and uncertainties assigned to t_i , $t_{d\text{a}}$, $t_{c\text{a}}$, $t_{l\text{a}}$, $t_{d\text{m}}$, $t_{c\text{m}}$, $t_{l\text{m}}$, μ , f , α , m_a , m_m , w_m
 315 and v are given in the section 3. The thermal and epithermal neutron self-shielding of the
 316 lyophilized CSF sample and of the dissolved (and diluted) Co monitor were considered
 317 insignificant. Accordingly, $G_{\text{th m}} = G_{\text{th a}} = G_{\text{e m}} = G_{\text{e a}} = 1.000$ with negligible
 318 uncertainty.

319 *Uncertainty budget*

320 The spreadsheet technique was applied to set up the uncertainty budget of the analyte mass
 321 concentration, ρ_a , via the measurement model (5).

322 The input quantities for ρ_a were $t_i, \mu, t_{1/2 a}, t_{1/2 m}, t_{d a}, t_{c a}, t_{l a}, t_{d m}, t_{c m}, t_{l m}, n_{p a}, n_{p m},$
323 $k_{0 Au}(a), k_{0 Au}(m), G_{th a}, G_{e a}, G_{th m}, G_{e m}, f, \alpha, Q_{0 a}, \bar{E}_{r a}, Q_{0 m}, \bar{E}_{r m}, \varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}, COI_m/COI_a,$
324 m_m, m_a, w_m and v . The intermediate quantities $\lambda_a, \lambda_m, \delta_a, \delta_m, \xi_a, \xi_m, Q_{0 a}(\alpha)$ and $Q_{0 m}(\alpha)$
325 were calculated for information.

326 For simplicity, the $\varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}$ and COI_m/COI_a values and uncertainties were computed
327 separately via the measurement models (7) and (8), respectively. The input quantities for
328 $\varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}$ were $a_1, a_0, a_{-1}, a_{-2}, a_{-3}, E_{\gamma m}, E_{\gamma a}, \Delta d_a, \Delta d_m, \delta\varepsilon_{r a}$ and $\delta\varepsilon_{r m}$ while the input
329 quantities for COI_m/COI_a were $a_1, a_0, a_{-1}, a_{-2}, a_{-3}$ and additional parameters depending
330 on the cascade scheme, e.g. $E_{\gamma}, a_{\gamma}, c_{\gamma}, P/T$ and P_{γ} either for the monitor and for the analyte.
331 The quantities $e_4, e_3, e_2, e_1, e_0, d_1$ and d_0 used to compute $\delta\varepsilon_r$ and the quantities $b_1, b_0,$
332 c_2, c_1 and c_0 used to compute P/T were given for information. The (small) correlation
333 effect due to the shared parameters a_1, a_0, a_{-1}, a_{-2} and a_{-3} was neglected.

334 The formulae were implemented in a MS excel file [17] consisting of nine worksheets, one
335 for each quantified analyte. A single worksheet included four sections. Irradiation time,
336 day and time of the irradiation end, day and time of the γ -counting start, outputs of the
337 Gamma Vision software, target nuclide and produced radionuclide were given in the first
338 section, called “Irradiation and γ -spectrometry”. Values, standard uncertainties and
339 correlation coefficients of the input quantities were added in the main section, called
340 “Uncertainty budget of ρ_a ”, with the exception of the $\varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}$ and COI_m/COI_a ratios,
341 whose data were added and calculated in two sub-sections, called “Uncertainty budget of
342 $\varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}$ ” and “Uncertainty budget of COI_m/COI_a ”, respectively.

343 Values and combined uncertainties of $\rho_a, \varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}$ and COI_m/COI_a were calculated
344 together with sensitivity coefficients of the input quantities and their relative contribution;
345 the matrix formalism was used to propagate the uncertainties via the correlation matrices
346 $R_{\rho_a}, R_{\varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}}$ and R_{COI_m/COI_a} .

347 The analysis quantified $2.32(11) \times 10^{-10}$ g mL⁻¹ of Th, $2.096(99) \times 10^{-9}$ g mL⁻¹ of Cr,
348 $6.89(96) \times 10^{-8}$ g mL⁻¹ of Ba, $4.01(39) \times 10^{-11}$ g mL⁻¹ of Sb, $5.06(15) \times 10^{-11}$ g mL⁻¹ of Sc,

349 $8.00(85) \times 10^{-10}$ g mL⁻¹ of Rb, $3.87(27) \times 10^{-8}$ g mL⁻¹ of Fe, $2.220(77) \times 10^{-8}$ g mL⁻¹ of Zn
 350 and $3.24(31) \times 10^{-11}$ g mL⁻¹ of Co.

351 The uncertainty budgets are given in the developed MS excel file available in the
 352 Supplementary Information; cells dealing with informative or intermediate data were
 353 grayed. In $R_{\varepsilon_{p m}^{\text{geo}}/\varepsilon_{p a}^{\text{geo}}}$ and $R_{\text{COI}_m/\text{COI}_a}$, we set the correlation coefficients of a_1, a_0, a_{-1}, a_{-2}
 354 and a_{-3} according to the data shown in Table 1; in addition, as a first attempt, in $R_{\varepsilon_{p m}^{\text{geo}}/\varepsilon_{p a}^{\text{geo}}}$,
 355 we set to the unity value the correlation between $\delta\varepsilon_{r a}$ and $\delta\varepsilon_{r m}$, and in $R_{\text{COI}_m/\text{COI}_a}$, we set
 356 to the unity value the correlation between P/T_γ values, if existing.

357 A survey of the main contributors to the combined uncertainties is given in Table 4 while
 358 the (complete) Cr budget is shown in the Supplementary Information.

359 **Table 4** Main contributors to the combined uncertainty of the quantified elements. Input
 360 quantities, X_i , are explained in the text. The index I is the relative contribution of X_i

Th		Cr		Ba		Sb		Sc		Rb		Fe		Zn		Co	
X_i	I / %	X_i	I / %	X_i	I / %	X_i	I / %	X_i	I / %	X_i	I / %	X_i	I / %	X_i	I / %	X_i	I / %
$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	26.7	$n_{p a}$	35.3	$Q_{0 a}$	89.3	$n_{p a}$	77.6	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	49.3	$n_{p a}$	83.4	$n_{p a}$	78.0	$\frac{\text{COI}_m}{\text{COI}_a}$	33.1	$n_{p a}$	92.8
$n_{p a}$	25.1	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	27.4	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	3.2	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	8.0	v	16.0	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	3.5	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	7.9	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	32.6	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	4.1
$\frac{\text{COI}_m}{\text{COI}_a}$	16.1	$\frac{\text{COI}_m}{\text{COI}_a}$	17.6	$n_{p a}$	2.9	$Q_{0 a}$	6.6	w_m	10.9	$\frac{\text{COI}_m}{\text{COI}_a}$	3.5	$\frac{\text{COI}_m}{\text{COI}_a}$	6.9	v	12.3		
$Q_{0 a}$	12.0	v	6.5					$Q_{0 a}$	5.8					w_m	8.4		
v	6.4	w_m	4.5					$n_{p a}$	4.1					$Q_{0 a}$	4.1		

361 In summary, the uncertainty of the results was largely due to $\varepsilon_{p m}^{\text{geo}}/\varepsilon_{p a}^{\text{geo}}$, $n_{p a}$ and
 362 $\text{COI}_m/\text{COI}_a$. In a few cases, v , w_m and m_m had an influence while the 20% uncertainty of
 363 the $Q_{0 a}$ recommended in the k_0 database [14] had the overriding effect for the
 364 determination of Ba.

365 It is worth to observe that the contribution to $\varepsilon_{p m}^{\text{geo}}/\varepsilon_{p a}^{\text{geo}}$ due to possible differences in
 366 counting positions of samples could be canceled if the monitor element was embedded in

367 the analyte sample [18, 19]; this was confirmed by setting the correlation coefficient
368 between Δd_a and Δd_m in $R_{\varepsilon_{p m}^{\text{geo}}/\varepsilon_{p a}^{\text{geo}}}$ to the unity value.

369 Besides, the result of Co deserves attention. In this case, i.e. when the analyte corresponds
370 to the monitor element and the same γ -emission is used, the k_0 -NAA turns into the relative-
371 NAA. Accordingly, we set to the unity value the correlation coefficients between $t_{1/2}$, $t_{1/2}$,
372 $k_{0 \text{ Au}}$, Q_0 and \bar{E}_r in R_{ρ_a} and between E_γ , a_γ , c_γ , P/T_γ in $R_{\text{COI}_m/\text{COI}_a}$. As a result, the
373 contributions due to the “intrinsic” uncertainty characteristic of the k_0 -NAA method [8]
374 and due to the $\text{COI}_m/\text{COI}_a$ were reset; moreover, the correlation coefficients of a_1 , a_0 , a_{-1} ,
375 a_{-2} and a_{-3} in $R_{\varepsilon_{p m}^{\text{geo}}/\varepsilon_{p a}^{\text{geo}}}$ made their contribution to $\varepsilon_{p m}^{\text{ext}}/\varepsilon_{p a}^{\text{ext}}$ zero as well.

376 **Conclusions**

377 The spreadsheet approach proved to be suitable to set up the uncertainty budget for the k_0 -
378 standardisation method in NAA when the majority of the recognized sources of error are
379 considered and the measurement model is written to limit the correlations between input
380 quantities. The use of the matrix formalism was straightforward to propagate the
381 uncertainties by taking into account the covariances.

382 A MS excel file was developed and tested for the determination of Th, Cr, Ba, Sb, Sc, Rb,
383 Fe, Zn and Co in a lyophilized CSF sample. The uncertainty budget of each element was
384 compiled once the estimates, the uncertainties and the correlation coefficients associated
385 with the input quantities were specified. The value and combined uncertainty of the result
386 were calculated and the most overriding contributors were pointed out.

387 It was shown that when the monitor element corresponded to the analyte element and the
388 same γ -emission was used, the worksheet set up the uncertainty budget for the relative-
389 NAA method; this makes the proposed approach applicable either in the relative- and k_0 -
390 NAA.

391 The MS excel file is open and free available to users. The implemented measurement model
392 allows a broad application, e.g. in case of different sample material, monitor element,

393 neutron irradiation and γ -spectrometry conditions. The extension to other elements is
394 possible by a simple duplication of the existing worksheets; only the modification of the
395 formulae adopted to compute the COI_m/COI_a ratio might be required for other decay
396 schemes.

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Supplementary information441 *Developed worksheet file*

442 See the MS excel file “uncertainty_k0_spreadsheet.xlsx”

443 *Uncertainty budget of Cr*

444 The (complete) uncertainty budget of the Cr determination is here reported. According to
 445 Table 1, the most overriding contributors to the combined uncertainty were n_{p_a} (35.3%),
 446 $\varepsilon_{p_m}^{\text{geo}}/\varepsilon_{p_a}^{\text{geo}}$ (27.4%) and $\text{COI}_m/\text{COI}_a$ (17.6%). The remaining 19.7% was due to v , w_m ,
 447 $Q_{0_a}, m_m, k_{0_{\text{Au}}(a)}, k_{0_{\text{Au}}(m)}, Q_{0_m}, n_{p_m}, \alpha$ and f , in decreasing order of importance. As
 448 regards to $\varepsilon_{p_m}^{\text{geo}}/\varepsilon_{p_a}^{\text{geo}}$ (see Table 2), the main contributors were a_1, a_{-1}, a_{-2} (44.0%), Δd_a
 449 (25.6%) and Δd_m (31.5%), while the uncertainty of $\text{COI}_m/\text{COI}_a$ (see Table 3) was due to
 450 $P/T_{\gamma 2m}$ (96.1%).

451 The a_0 value is not affecting $\varepsilon_{p_m}^{\text{geo}}/\varepsilon_{p_a}^{\text{geo}}$. In fact, a_0 in equation (6) models a constant
 452 multiplying factor that is deleted from the detection efficiency ratio. In addition, since we
 453 considered $\Delta d_a = \Delta d_m = 0$ mm, the contribution of $\delta\varepsilon_{r_a}$ and $\delta\varepsilon_{r_m}$ was reset.

454 **Table 1** Uncertainty budget of the mass concentration of Cr in
 455 the lyophilized CSF sample. Quantities are explained in the text.
 456 The column Index gives the relative contribution of the input
 457 quantity, X_i , to the output quantity, Y . Values of the sensitivity
 458 coefficient, c_i , and Index are omitted for those quantities that are
 459 not actual inputs of the measurement model.

Quantity X_i	Unit [X_i]	Value x_i	Std. Uncertainty $u(x_i)$	Sens. Coeff. c_i	Index I / %
t_i	s	2.1600×10^4	1.7×10^1	3.0×10^{-16}	0.0
μ	1	4.45×10^{-2}	5×10^{-4}	-1.0×10^{-10}	0.0
$t_{1/2 a}$	s	2.39328×10^6	2.1×10^2	1.1×10^{-16}	0.0
λ_a	s ⁻¹	2.89622×10^{-7}	2.5×10^{-11}		
$t_{1/2 m}$	s	1.66346×10^8	2.6×10^4	-1.2×10^{-17}	0.0
λ_m	s ⁻¹	4.16690×10^{-9}	6.5×10^{-13}		
$t_{d a}$	s	2.404405×10^6	3.5×10^1	6.1×10^{-16}	0.0

$t_{c a}$	s	1.29262800×10^6	2.9×10^{-1}	3.6×10^{-16}	0.0
$t_{l a}$	s	1.26426800×10^6	2.9×10^{-1}	-1.7×10^{-15}	0.0
$t_{d m}$	s	3.722775×10^6	3.5×10^1	-8.7×10^{-18}	0.0
$t_{c m}$	s	7.9700×10^2	2.9×10^{-1}	-1.1×10^{-13}	0.0
$t_{l m}$	s	7.400×10^2	2.9×10^{-1}	2.9×10^{-12}	0.0
δ_a	1	1.022	0.000		
δ_m	1	1.077	0.001		
ξ_a	1	1.00098	1×10^{-5}		
ξ_m	1	1.00319	4×10^{-5}		
$n_{p a}$	1	5.26×10^4	1.5×10^3	4.0×10^{-14}	35.3
$n_{p m}$	1	1.3749×10^5	4.4×10^2	-1.5×10^{-14}	0.5
$k_{0 Au(a)}$	1	2.620×10^{-3}	1.3×10^{-5}	-8.0×10^{-7}	1.1
$k_{0 Au(m)}$	1	1.3200	5.3×10^{-3}	1.6×10^{-9}	0.7
$G_{th a}$	1	1.000	0.000	-2.0×10^{-9}	0.0
$G_{e a}$	1	1.000	0.000	-7.7×10^{-11}	0.0
$G_{th m}$	1	1.000	0.000	1.8×10^{-9}	0.0
$G_{e m}$	1	1.000	0.000	2.7×10^{-10}	0.0
f	1	1.560×10^1	3.3×10^{-1}	-1.2×10^{-11}	0.2
α	1	-3.60×10^{-2}	6.4×10^{-3}	-9.0×10^{-10}	0.3
$Q_{0 a}$	1	5.3×10^{-1}	1.1×10^{-1}	-1.8×10^{-10}	3.6
$\bar{E}_{r a}$	eV	7.53×10^3	8.3×10^2	-8.7×10^{-17}	0.0
$Q_{0 a}(\alpha)$	1	5.9×10^{-1}	1.5×10^{-1}		
$Q_{0 m}$	1	1.993	6.0×10^{-2}	1.4×10^{-10}	0.7
$\bar{E}_{r m}$	eV	1.360×10^2	6.9	5.8×10^{-14}	0.0
$Q_{0 m}(\alpha)$	1	2.319	9.5×10^{-2}		
$\varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}$	1	3.507×10^{-1}	8.7×10^{-3}	6.0×10^{-9}	27.4
COI_m/COI_a	1	8.57×10^{-1}	1.7×10^{-2}	2.4×10^{-9}	17.6
m_m	g	8.47×10^{-3}	5×10^{-5}	2.5×10^{-7}	1.6
m_a	g	2.4000×10^{-1}	5×10^{-5}	-8.7×10^{-9}	0.0
w_m	g g ⁻¹	4.597×10^{-3}	4.6×10^{-5}	4.6×10^{-7}	4.5
v	mg L ⁻¹	99.2	1.2	-2.1×10^{-11}	6.6
Y	[Y]	y	$u_c(y)$		
ρ_a	g mL ⁻¹	2.096×10^{-9}	9.9×10^{-11}		

460
461

Table 2. Uncertainty budget of the $\varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}$ ratio given in Table 1.

Quantity X_i	Unit [X_i]	Value x_i	Std. Uncertainty $u(x_i)$	Sens. Coeff. c_i	Index I / %
a_1	MeV ⁻¹	-4.72×10^{-1}	4.3×10^{-2}	3.0×10^{-1}	74.1

a_0	1	-3.229	5.7×10^{-2}	0.0	0.0
a_{-1}	MeV	4.03×10^{-1}	2.0×10^{-2}	-8.0×10^{-1}	-43.1
a_{-2}	MeV ²	3.20×10^{-2}	2.2×10^{-3}	-3.2	13.0
a_{-3}	MeV ³	5.73×10^{-4}	7.5×10^{-5}	-1.0×10^1	-1.1
$E_{\gamma m}$	MeV	1.17320	1.2×10^{-4}	-2.5×10^{-1}	0.0
$E_{\gamma a}$	MeV	3.2010×10^{-1}	1.2×10^{-4}	9.2×10^{-1}	0.0
Δd_a	mm	0.00	0.29	1.5×10^{-2}	25.6
Δd_m	mm	0.00	0.29	-1.7×10^{-2}	31.5
e_4	keV ⁻⁴	-7.10×10^{-11}	0.00×10^{-11}		
e_3	keV ⁻³	5.19×10^{-8}	0.00×10^{-8}		
e_2	keV ⁻²	-1.43×10^{-5}	0.00×10^{-5}		
e_1	keV ⁻¹	1.78×10^{-3}	0.00×10^{-3}		
e_0	1	-4.46×10^{-2}	0.00×10^{-2}		
d_1	keV ⁻¹	5.56×10^{-6}	0.00×10^{-6}		
d_0	1	4.17×10^{-2}	0.00×10^{-2}		
$\delta \varepsilon_{ra}$	mm ⁻¹	4.3×10^{-2}	5×10^{-3}	0.0	0.0
$\delta \varepsilon_{rm}$	mm ⁻¹	4.8×10^{-2}	6×10^{-3}	0.0	0.0
Y	[Y]	y	$u_c(y)$		
$\varepsilon_{pm}^{\text{geo}}/\varepsilon_{pa}^{\text{geo}}$	1	3.507×10^{-1}	8.7×10^{-3}		

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Table 3 Uncertainty budget of the $\text{COI}_m/\text{COI}_a$ ratio given in Table 1. (*) Notation reported in [4] and adopted for the cascade scheme.

Quantity X_i	Unit [X_i]	Value x_i	Std. Uncertainty $u(x_i)$	Sens. Coeff. c_i	Index I / %
a_1	MeV ⁻¹	-4.72×10^{-1}	4.3×10^{-2}	-1.9×10^{-1}	5.9
a_0	1	-3.229	5.7×10^{-2}	-1.4×10^{-1}	-4.9
a_{-1}	MeV	4.03×10^{-1}	2.0×10^{-2}	-1.1×10^{-1}	1.0
a_{-2}	MeV ²	3.20×10^{-2}	2.2×10^{-3}	-8.0×10^{-2}	-0.1
a_{-3}	MeV ³	5.73×10^{-4}	7.5×10^{-5}	-6.0×10^{-2}	0.0
b_1	1	-0.571	0.000		
b_0	1	1.079	0.000		
c_2	1	-1.625	0.000		
c_1	1	6.678	0.000		
c_0	1	-7.006	0.000		
$E_{\gamma 2m}$	keV	1.3325×10^3	1.2×10^{-1}	9.6×10^{-5}	0.0
$a_{\gamma 2m}$	1	1.000	0.012	-1.4×10^{-1}	0.9
$c_{\gamma 2m}$	1	1.000	0.012	-1.4×10^{-1}	0.9
$P/T_{\gamma 2m}$	1	0.197	0.023	7.3×10^{-1}	96.1

Y	$[Y]$	y	$u_c(y)$		
$\text{COI}_m/\text{COI}_a$	1	8.57×10^{-1}	1.7×10^{-2}		

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466 This section will not appear in the printed version of your paper but it will contain a link;
467 the webpage containing the electronic supplementary information will appear when one
468 clicks on the hyperlink. Here you can list the details of your research which would be too
469 long for the main text, *e.g.* a larger number of spectra *etc.* Start with 1 for Figure and Table
470 numbers in this section.

Irradiation and γ -spectrometry

end irradiation 9/12/2017 2.46 PM
irradiation time / s 21600

library CSF.Lib
calib OR50_source2016_geom_cont_12052017.Clb
sm type CSF.Lib (ROI32 Analysis)

Nuclide	Channel	Energy	Background
233Pa		1246.2	311.9
Co60		4691.96	1173.2
			1461015
			5220

	target	product
analite, a	^{232}Th	^{233}Pa
monitor, m	^{59}Co	^{60}Co

Uncertainty budget of ρ_a

Input Quantity	Quantity	Unit	Value
X_i	X_i	$[X_i]$	x_i
t_i		s	21600
μ		1	0.0445
$t_{1/2 a}$		s	2330208
	λ_a	s^{-1}	3.0E-07
$t_{1/2 m}$		s	1.7E+08
	λ_m	s^{-1}	4.2E-09
$t_{d a}$		s	2404405
$t_{c a}$		s	1292628
$t_{i a}$		s	1264268
$t_{d m}$		s	3722775
$t_{c m}$		s	797.0
$t_{i m}$		s	740.0
	δ_a	1	1.022
	δ_m	1	1.077
	ξ_a	1	1.001
	ξ_m	1	1.003
$n_{p a}$		1	101680
$n_{p m}$		1	137487
$k_{0 Au(a)}$		1	0.02520
$k_{0 Au(m)}$		1	1.3200
$G_{th a}$		1	1

$G_{e a}$		1	1
$G_{th m}$		1	1
$G_{e m}$		1	1
f		1	15.60
α		1	-0.0360
$Q_{0 a}$		1	11.50
$E_{r a}$		eV	54.40
	$Q_{0 a}(\alpha)$	1	13.24
$Q_{0 m}$		1	1.993
$E_{r m}$		eV	136.0
	$Q_{0 m}(\alpha)$	1	2.319
$\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$		1	0.3431
COI_m / COI_a		1	0.862
m_m		g	0.00847
m_a		g	0.24000
w_m		$g g^{-1}$	0.004597
ν		$mg L^{-1}$	99.2
Y		[Y]	y
ρ_a		$g mL^{-1}$	2.32E-10

Uncertainty budget of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

Input Quantity	Quantity	Unit	Value
X_i	X_i	[X_i]	x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
$a_{.1}$		Mev	0.403
$a_{.2}$		Mev2	-0.0320
$a_{.3}$		Mev3	0.000573
$E_{\gamma m}$		MeV	1.17320
$E_{\gamma a}$		MeV	0.31190
Δd_a		mm	0
Δd_m		mm	0
	e_4	keV-4	-7.1E-11
	e_3	keV-3	5.2E-08
	e_2	keV-2	-1.4E-05
	e_1	keV-1	1.8E-03
	e_0		1 -4.5E-02
	d_1	keV-1	5.6E-06

	d_0		1	4.2E-02
$\delta\epsilon_{ra}$		mm^{-1}		0.043
$\delta\epsilon_{rm}$		mm^{-1}		0.048
Y		[Y]	y	
	$\epsilon_{pm}^{\text{geo}} / \epsilon_{pa}^{\text{geo}}$		1	0.343

Uncertainty budget of $\text{COI}_m / \text{COI}_a$

Input Quantity	Quantity X_i	Unit [X_i]	Value x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
a_{-1}		Mev	0.403
a_{-2}		Mev2	-0.0320
a_{-3}		Mev3	0.000573
	b_1		1 -0.571
	b_0		1 1.079
	c_2		1 -1.625
	c_1		1 6.678
	c_0		1 -7.006
$E_{\gamma 2m}$		keV	1332.50
$a_{\gamma 2m}$			1 1.000
$c_{\gamma 2m}$			1 1.000
$P/T_{\gamma 2m}$			1 0.197
$E_{\gamma 6a}$		keV	86.60
$P_{\gamma 6a}$			1 2.05%
$P/T_{\gamma 6a}$			1 0.680
$a_{\gamma 9a}$			1 0.980
$c_{\gamma 9a}$			1 0.550
$P_{\gamma 9a}$			1 38.60%
	Y	[Y]	y
	$\text{COI}_m / \text{COI}_a$		1 0.862

Net area	Cnts/s	Uncert %	FWHM	source file	start counting
101680	0.08	2.4	1.269	OR50_20171025_CSF_s	10/10/2017
137487	185.919	0.32	1.798	OR50_20170925_Co_sa	10/25/2017

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance γ $u_y^2(x_i)$	Index	Input for sensit coeff $x_i+u(x_i)$ $\gamma(x_i+u(x_i))$	
17	0.1%	3.4E-17	3.5E-31	0.0%	2.2E+04	2.3E-10
0.0005	1.1%	-1.1E-11	3.3E-29	0.0%	4.5E-02	2.3E-10
173	0.0%	1.0E-17	3.1E-30	0.0%	2.3E+06	2.3E-10
2.2E-11	0.0%					
2.6E+04	0.0%	-1.4E-18	1.3E-27	0.0%	1.7E+08	2.3E-10
6.5E-13	0.0%					
35	0.0%	6.9E-17	5.7E-30	0.0%	2.4E+06	2.3E-10
0.3	0.0%	4.0E-17	1.3E-34	0.0%	1.3E+06	2.3E-10
0.3	0.0%	-1.9E-16	3.1E-33	0.0%	1.3E+06	2.3E-10
35	0.0%	-9.7E-19	1.1E-33	0.0%	3.7E+06	2.3E-10
0.3	0.0%	-1.2E-14	1.2E-29	0.0%	8.0E+02	2.3E-10
0.3	0.0%	3.3E-13	8.9E-27	0.0%	7.4E+02	2.3E-10
0.000	0.0%					
0.001	0.1%					
0.000	0.0%					
0.000	0.0%					
2440	2.4%	2.3E-15	3.1E-23	25.1%	1.0E+05	2.4E-10
440	0.3%	-1.7E-15	5.5E-25	0.4%	1.4E+05	2.3E-10
0.00013	0.5%	-9.2E-09	1.3E-24	1.1%	2.5E-02	2.3E-10
0.0053	0.4%	1.8E-10	8.6E-25	0.7%	1.3E+00	2.3E-10
0	0.0%	-1.3E-10	0.0E+00	0.0%	1.0E+00	2.3E-10

	0.0000	0.0%					
	0.005	11.5%	0.0E+00	0.0E+00	0.0%	4.8E-02	3.4E-01
	0.006	11.5%	0.0E+00	0.0E+00	0.0%	5.4E-02	3.4E-01
$u_c(y)$	$u_{c_r}(y)$				Σ		
	0.008	2.5%			100.0%		

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance γ $u^2_{\gamma}(x_i)$	Index	Input for sensit coeff	
					$x_i+u(x_i)$	$\gamma(x_i+u(x_i))$
0.043	9.2%	-0.1908	1.7E-05	6.3%	-4.3E-01	8.5E-01
0.057	1.8%	-0.1385	-1.4E-05	-5.2%	-3.2E+00	8.5E-01
0.020	4.8%	-0.0496	1.4E-06	0.5%	4.2E-01	8.6E-01
0.0022	6.9%	0.5942	1.7E-06	0.6%	-3.0E-02	8.6E-01
0.000075	13.1%	7.6348	-6.7E-07	-0.2%	6.5E-04	8.6E-01
0	0.0%					
0	0.0%					
0	0.0%					
0	0.0%					
0	0.0%					
0.12	0.0%	0.0001	1.2E-10	0.0%	1.3E+03	8.6E-01
0.012	1.2%	-0.1434	2.7E-06	1.0%	1.0E+00	8.6E-01
0.012	1.2%	-0.1434	2.7E-06	1.0%	1.0E+00	8.6E-01
0.023	11.5%	0.7385	2.7E-04	99.4%	2.2E-01	8.8E-01
0.12	0.1%	0.0001	6.1E-11	0.0%	8.7E+01	8.6E-01
0.01%	0.6%	0.2432	7.9E-10	0.0%	2.1E-02	8.6E-01
0.079	11.5%	-0.0074	-9.5E-06	-3.5%	7.6E-01	8.6E-01
0.012	1.2%	0.0051	3.5E-09	0.0%	9.9E-01	8.6E-01
0.012	2.1%	0.0091	1.1E-08	0.0%	5.6E-01	8.6E-01
0.12%	0.3%	-0.0129	2.2E-10	0.0%	3.9E-01	8.6E-01

$u_c(y)$	$u_r(y)$			Σ	
	0.017	1.9%		100.0%	

	t_c / s	t_i / s	$t_{dead\ r} / \%$	t_d / s	$t_c / t_{1/2}$	$t_d / t_{1/2}$
10:39 AM	1292628	1264268	2.2%	2404405	0.55	1.0
4:52 PM	797	740	7.2%	3722775	0.00	0.0

Correlation matrix of ρ_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		t_i	μ	$t_{1/2\ a}$	$t_{1/2\ m}$
2.2E+04	2.3E-10	t_i	1	0	0	0
4.4E-02	2.3E-10	μ	0	1	0	0
2.3E+06	2.3E-10	$t_{1/2\ a}$	0	0	1	0
		$t_{1/2\ m}$	0	0	0	1
1.7E+08	2.3E-10	$t_{d\ a}$	0	0	0	0
		$t_{c\ a}$	0	0	0	0
2.4E+06	2.3E-10	$t_{i\ a}$	0	0	0	0
1.3E+06	2.3E-10	$t_{d\ m}$	0	0	0	0
1.3E+06	2.3E-10	$t_{c\ m}$	0	0	0	0
3.7E+06	2.3E-10	$t_{i\ m}$	0	0	0	0
8.0E+02	2.3E-10	$n_{p\ a}$	0	0	0	0
7.4E+02	2.3E-10	$n_{p\ m}$	0	0	0	0
		$k_{0\ Au}(a)$	0	0	0	0
		$k_{0\ Au}(m)$	0	0	0	0
		$G_{th\ a}$	0	0	0	0
		$G_{e\ a}$	0	0	0	0
9.9E+04	2.3E-10	$G_{th\ m}$	0	0	0	0
1.4E+05	2.3E-10	$G_{e\ m}$	0	0	0	0
2.5E-02	2.3E-10	f	0	0	0	0
1.3E+00	2.3E-10	α	0	0	0	0
1.0E+00	2.3E-10	$Q_{0\ a}$	0	0	0	0

1.0E+00	2.3E-10	E_{ra}	0	0	0	0
1.0E+00	2.3E-10	Q_{0m}	0	0	0	0
1.0E+00	2.3E-10	E_{rm}	0	0	0	0
1.5E+01	2.3E-10	$\varepsilon_{pm}^{geo} / \varepsilon_{pa}^i$	0	0	0	0
-4.2E-02	2.3E-10	COI_m / COI_a	0	0	0	0
1.1E+01	2.4E-10	m_m	0	0	0	0
5.4E+01	2.3E-10	m_a	0	0	0	0
		w_m	0	0	0	0
1.9E+00	2.3E-10	v	0	0	0	0
1.3E+02	2.3E-10					
3.3E-01	2.3E-10					
8.5E-01	2.3E-10					
8.4E-03	2.3E-10					
2.4E-01	2.3E-10					
4.6E-03	2.3E-10					
9.8E+01	2.3E-10					

Correlation matrix of $\varepsilon_{pm}^{geo} / \varepsilon_{pa}^{geo}$

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	3.3E-01	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	3.4E-01	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	3.6E-01	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	3.5E-01	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	3.4E-01	a_{-3}	0.748	-0.848	0.957	-0.993
1.2E+00	3.4E-01	$E_{\gamma m}$	0	0	0	0
3.1E-01	3.4E-01	$E_{\gamma a}$	0	0	0	0
-2.9E-01	3.4E-01	Δd_a	0	0	0	0
-2.9E-01	3.5E-01	Δd_m	0	0	0	0
		$\delta \varepsilon_{ra}$	0	0	0	0
		$\delta \varepsilon_{rm}$	0	0	0	0

3.8E-02 3.4E-01
 4.3E-02 3.4E-01

Correlation matrix of COI_m / COI_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	8.7E-01	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	8.7E-01	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	8.6E-01	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	8.6E-01	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	8.6E-01	a_{-3}	0.748	-0.848	0.957	-0.993
		$E_{\gamma 2 m}$	0	0	0	0
		$a_{\gamma 2 m}$	0	0	0	0
		$C_{\gamma 2 m}$	0	0	0	0
		$P/T_{\gamma 2 m}$	0	0	0	0
		$E_{\gamma 6 a}$	0	0	0	0
1.3E+03	8.6E-01	$P_{\gamma 6 a}$	0	0	0	0
9.9E-01	8.6E-01	$P/T_{\gamma 6 a}$	0	0	0	0
9.9E-01	8.6E-01	$a_{\gamma 9 a}$	0	0	0	0
1.7E-01	8.4E-01	$C_{\gamma 9 a}$	0	0	0	0
8.6E+01	8.6E-01	$P_{\gamma 9 a}$	0	0	0	0
2.0E-02	8.6E-01					
6.0E-01	8.6E-01					
9.7E-01	8.6E-01					
5.4E-01	8.6E-01					
3.8E-01	8.6E-01					

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$	Δd_a	Δd_m	$\delta \varepsilon_{ra}$	$\delta \varepsilon_{rm}$	c_i
0.748	0	0	0	0	0	0	3.0E-01
-0.848	0	0	0	0	0	0	0.0E+00
0.957	0	0	0	0	0	0	-8.1E-01
-0.993	0	0	0	0	0	0	-3.3E+00
1.000	0	0	0	0	0	0	-1.1E+01
0	1	0	0	0	0	0	-2.5E-01
0	0	1	0	0	0	0	9.2E-01
0	0	0	1	0	0	0	1.5E-02
0	0	0	0	1	0	0	-1.7E-02
0	0	0	0	0	1	1	0.0E+00
0	0	0	0	0	0	1	0.0E+00

0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Covariance matrix of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

	a_1	a_0	a_{-1}	a_{-2}	a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$
a_1	1.9E-03	-2.4E-03	7.5E-04	-7.7E-05	2.4E-06	0.0E+00	0.0E+00
a_0	-2.4E-03	3.2E-03	-1.1E-03	1.1E-04	-3.6E-06	0.0E+00	0.0E+00
a_{-1}	7.5E-04	-1.1E-03	3.8E-04	-4.3E-05	1.4E-06	0.0E+00	0.0E+00
a_{-2}	-7.7E-05	1.1E-04	-4.3E-05	4.9E-06	-1.7E-07	0.0E+00	0.0E+00
a_{-3}	2.4E-06	-3.6E-06	1.4E-06	-1.7E-07	5.7E-09	0.0E+00	0.0E+00
$E_{\gamma m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08	0.0E+00
$E_{\gamma a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08
Δd_a	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
Δd_m	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
c_i	3.0E-01	0.0E+00	-8.1E-01	-3.3E+00	-1.1E+01	-2.5E-01	9.2E-01

Covariance matrix of COI_m/COI_a

$C_{\gamma 9 a}$	$P_{\gamma 9 a}$	c_i		a_1	a_0	a_{-1}
0	0	-1.9E-01	a_1	1.9E-03	-2.4E-03	7.5E-04
0	0	-1.4E-01	a_0	-2.4E-03	3.2E-03	-1.1E-03
0	0	-5.0E-02	a_{-1}	7.5E-04	-1.1E-03	3.8E-04
0	0	5.9E-01	a_{-2}	-7.7E-05	1.1E-04	-4.3E-05
0	0	7.6E+00	a_{-3}	2.4E-06	-3.6E-06	1.4E-06
0	0	9.7E-05	$E_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
0	0	-1.4E-01	$a_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
0	0	-1.4E-01	$c_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
0	0	7.4E-01	$P/T_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
0	0	6.8E-05	$E_{\gamma 6 a}$	0.0E+00	0.0E+00	0.0E+00
0	0	2.4E-01	$P_{\gamma 6 a}$	0.0E+00	0.0E+00	0.0E+00
0	0	-7.4E-03	$P/T_{\gamma 6 a}$	0.0E+00	0.0E+00	0.0E+00
0	0	5.1E-03	$a_{\gamma 9 a}$	0.0E+00	0.0E+00	0.0E+00
1	0	9.1E-03	$c_{\gamma 9 a}$	0.0E+00	0.0E+00	0.0E+00
0	1	-1.3E-02	$P_{\gamma 9 a}$	0.0E+00	0.0E+00	0.0E+00
			c_i	-1.9E-01	-1.4E-01	-5.0E-02

0	0	0	0	0	0	0
1	0	0	0	0	0	0
0	1	0	0	0	0	0
0	0	1	0	0	0	0
0	0	0	1	0	0	0
0	0	0	0	1	0	0
0	0	0	0	0	1	0
0	0	0	0	0	0	1
0	0	0	0	0	0	0

Δd_a	Δd_m	$\delta \varepsilon_{r_a}$	$\delta \varepsilon_{r_m}$
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
8.3E-02	0.0E+00	0.0E+00	0.0E+00
0.0E+00	8.3E-02	0.0E+00	0.0E+00
0.0E+00	0.0E+00	2.5E-05	2.8E-05
0.0E+00	0.0E+00	2.8E-05	3.1E-05
1.5E-02	-1.7E-02	0.0E+00	0.0E+00

a_{-2}	a_{-3}	$E_{\gamma 2 m}$	$a_{\gamma 2 m}$	$C_{\gamma 2 m}$	$P/T_{\gamma 2 m}$	$E_{\gamma 6 a}$
-7.7E-05	2.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
1.1E-04	-3.6E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-4.3E-05	1.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
4.9E-06	-1.7E-07	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-1.7E-07	5.7E-09	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	1.3E-02	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	5.2E-04	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-02
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.8E-03	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
5.9E-01	7.6E+00	9.7E-05	-1.4E-01	-1.4E-01	7.4E-01	6.8E-05

Covariance matrix of ρ_a

ρ	c_i	t_i	μ
0	3.4E-17	t_i	3.0E+02
0	-1.1E-11	μ	0.0E+00
0	1.0E-17	$t_{1/2 a}$	0.0E+00
0	-1.4E-18	$t_{1/2 m}$	0.0E+00
0	6.9E-17	$t_{d a}$	0.0E+00
0	4.0E-17	$t_{c a}$	0.0E+00
0	-1.9E-16	$t_{i a}$	0.0E+00
0	-9.7E-19	$t_{d m}$	0.0E+00
0	-1.2E-14	$t_{c m}$	0.0E+00
0	3.3E-13	$t_{i m}$	0.0E+00
0	2.3E-15	$n_{p a}$	0.0E+00
0	-1.7E-15	$n_{p m}$	0.0E+00
0	-9.2E-09	$k_{0 Au(a)}$	0.0E+00
0	1.8E-10	$k_{0 Au(m)}$	0.0E+00
0	-1.3E-10	$G_{th a}$	0.0E+00
0	-1.1E-10	$G_{e a}$	0.0E+00
0	2.0E-10	$G_{th m}$	0.0E+00
0	3.0E-11	$G_{e m}$	0.0E+00
0	4.9E-12	f	0.0E+00
0	2.9E-10	α	0.0E+00
0	-9.3E-12	$Q_{0 a}$	0.0E+00

0	-6.8E-14	E_{r_a}	0.0E+00	0.0E+00
0	1.5E-11	Q_{0_m}	0.0E+00	0.0E+00
0	6.4E-15	E_{r_m}	0.0E+00	0.0E+00
0	6.8E-10	$\varepsilon_{p_m}^{geo} / \varepsilon_{p_a}^{geo}$	0.0E+00	0.0E+00
0	2.7E-10	COI_m / COI_a	0.0E+00	0.0E+00
0	2.7E-08	m_m	0.0E+00	0.0E+00
0	-9.7E-10	m_a	0.0E+00	0.0E+00
0	5.0E-08	w_m	0.0E+00	0.0E+00
1	-2.3E-12	ν	0.0E+00	0.0E+00
		c_i	3.4E-17	-1.1E-11

$P_{\gamma 6 a}$	$P/T_{\gamma 6 a}$	$a_{\gamma 9 a}$	$C_{\gamma 9 a}$	$P_{\gamma 9 a}$	
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	1.8E-03	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
1.3E-08	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	6.2E-03	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-06
2.4E-01	-7.4E-03	5.1E-03	9.1E-03		-1.3E-02

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
1.0E-17	-1.4E-18	6.9E-17	4.0E-17	-1.9E-16	-9.7E-19

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-1.2E-14	3.3E-13	2.3E-15	-1.7E-15	-9.2E-09	1.8E-10

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-1.3E-10	-1.1E-10	2.0E-10	3.0E-11	4.9E-12

0.0E+00	0.0E+00	2.4E-01	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	3.6E-03	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	4.8E+01	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	7.2E-05
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
2.9E-10	-9.3E-12	-6.8E-14	1.5E-11	6.4E-15	6.8E-10

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
2.7E-04	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	2.5E-09	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	2.5E-09	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	2.1E-09	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.4E+00
2.7E-10	2.7E-08	-9.7E-10	5.0E-08	-2.3E-12

Irradiation and γ -spectrometry

end irradiation 9/12/2017 2.46 PM
 irradiation time / s 21600

library CSF.Lib
 calib OR50_source2016_geom_cont_12052017.Clb
 sm type CSF.Lib (ROI32 Analysis)

Nuclide	Channel	Energy	Background
51Cr		1279.1	320.1
Co60		4691.96	1173.2
			1066118
			5220

	target	product
analite, a	^{50}Cr	^{51}Cr
monitor, m	^{59}Co	^{60}Co

Uncertainty budget of ρ_a

Input Quantity	Quantity	Unit	Value
X_i	X_i	$[X_i]$	x_i
t_i		s	21600
μ		1	0.0445
$t_{1/2 a}$		s	2393280
	λ_a	s^{-1}	2.89622E-07
$t_{1/2 m}$		s	166345920
	λ_m	s^{-1}	4.16690E-09
$t_{d a}$		s	2.404405E+06
$t_{c a}$		s	1.29262800E+06
$t_{i a}$		s	1.26426800E+06
$t_{d m}$		s	3.722775E+06
$t_{c m}$		s	7.9700E+02
$t_{i m}$		s	7.4000E+02
	δ_a	1	1.022
	δ_m	1	1.077
	ξ_a	1	1.00098
	ξ_m	1	1.00319
$n_{p a}$		1	5.26E+04
$n_{p m}$		1	1.3749E+05
$k_{0 Au(a)}$		1	2.620E-03
$k_{0 Au(m)}$		1	1.3200
$G_{th a}$		1	1

$G_{e a}$		1	1
$G_{th m}$		1	1
$G_{e m}$		1	1
f		1	15.60
α		1	-0.0360
$Q_{0 a}$		1	0.53
$E_{r a}$		eV	7530
	$Q_{0 a}(\alpha)$	1	0.59
$Q_{0 m}$		1	1.993
$E_{r m}$		eV	136.0
	$Q_{0 m}(\alpha)$	1	2.319
$\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$		1	0.3507
COI_m / COI_a		1	0.857
m_m		g	0.00847
m_a		g	0.24000
w_m		$g g^{-1}$	0.004597
ν		$mg L^{-1}$	99.2
Y		[Y]	y
ρ_a		$g mL^{-1}$	2.096E-09

Uncertainty budget of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

Input Quantity	Quantity	Unit	Value
X_i	X_i	[X_i]	x_i
a_1		Mev-1	-0.472
a_0			1
a_{-1}		Mev	0.403
a_{-2}		Mev2	-0.0320
a_{-3}		Mev3	0.000573
$E_{\gamma m}$		MeV	1.17320
$E_{\gamma a}$		MeV	0.32010
Δd_a		mm	0.00
Δd_m		mm	0.00
	e_4	keV-4	-7.10E-11
	e_3	keV-3	5.19E-08
	e_2	keV-2	-1.43E-05
	e_1	keV-1	1.78E-03
	e_0		1
	d_1	keV-1	-4.46E-02
			5.56E-06

	d_0		1	4.17E-02
$\delta\epsilon_{ra}$		mm^{-1}		0.043
$\delta\epsilon_{rm}$		mm^{-1}		0.048
Y		[Y]	y	
	$\epsilon_{pm}^{\text{geo}} / \epsilon_{pa}^{\text{geo}}$		1	0.3507

Uncertainty budget of $\text{COI}_m / \text{COI}_a$

Input Quantity	Quantity X_i	Unit [X_i]	Value x_i	
a_1		Mev-1	-0.472	
a_0			1	
a_{-1}		Mev	0.403	
a_{-2}		Mev2	-0.0320	
a_{-3}		Mev3	0.000573	
	b_1		1	
	b_0		1	
	c_2		1	
	c_1		1	
	c_0		1	
$E_{\gamma 2m}$		keV	1332.50	
$a_{\gamma 2m}$			1	
$c_{\gamma 2m}$			1	
$P/T_{\gamma 2m}$			1	
	Y	[Y]	y	
	$\text{COI}_m / \text{COI}_a$		1	
				0.857

Net area	Cnts/s	Uncert %	FWHM	source file	start counting
52632	0.042	2.81	1.277	OR50_20171025_CSF_si	10/10/2017
137487	185.919	0.32	1.798	OR50_20170925_Co_sa	10/25/2017

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance y $u^2_y(x_i)$	Index	Input for sensit coeff $x_i+u(x_i)$ $y(x_i+u(x_i))$	
17	0.1%	3.0E-16	2.7E-29	0.0%	2.2E+04	2.1E-09
0.0005	1.1%	-1.0E-10	2.7E-27	0.0%	4.5E-02	2.1E-09
207	0.0%	1.1E-16	5.2E-28	0.0%	2.4E+06	2.1E-09
2.5E-11	0.0%					
25920	0.0%	-1.2E-17	1.0E-25	0.0%	1.7E+08	2.1E-09
6.5E-13	0.0%					
3.5E+01	0.0%	6.1E-16	4.4E-28	0.0%	2.4E+06	2.1E-09
2.9E-01	0.0%	3.6E-16	1.1E-32	0.0%	1.3E+06	2.1E-09
2.9E-01	0.0%	-1.7E-15	2.5E-31	0.0%	1.3E+06	2.1E-09
3.5.E+01	0.0%	-8.7E-18	9.2E-32	0.0%	3.7E+06	2.1E-09
2.9E-01	0.0%	-1.1E-13	9.8E-28	0.0%	8.0E+02	2.1E-09
2.9E-01	0.0%	2.9E-12	7.2E-25	0.0%	7.4E+02	2.1E-09
0.000	0.0%					
0.001	0.1%					
0.00001	0.0%					
0.00004	0.0%					
1.5E+03	2.8%	4.0E-14	3.5E-21	35.3%	5.4E+04	2.2E-09
4.4E+02	0.3%	-1.5E-14	4.5E-23	0.5%	1.4E+05	2.1E-09
1.3E-05	0.5%	-8.0E-07	1.1E-22	1.1%	2.6E-03	2.1E-09
0.0053	0.4%	1.6E-09	7.0E-23	0.7%	1.3E+00	2.1E-09
0	0.0%	-2.0E-09	0.0E+00	0.0%	1.0E+00	2.1E-09

	0.0000	0.0%					
	0.005	11.5%	0.0E+00	0.0E+00	0.0%	4.8E-02	3.5E-01
	0.006	11.5%	0.0E+00	0.0E+00	0.0%	5.4E-02	3.5E-01
$u_c(y)$	$u_{c,r}(y)$				Σ		
	0.0087	2.5%			100.0%		

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance y $u^2_y(x_i)$	Index	Input for sensit coeff	
					$x_i+u(x_i)$	$y(x_i+u(x_i))$
0.043	9.2%	-1.9E-01	1.7E-05	5.9%	-4.3E-01	8.5E-01
0.057	1.8%	-1.4E-01	-1.4E-05	-4.9%	-3.2E+00	8.5E-01
0.020	4.8%	-1.1E-01	3.0E-06	1.0%	4.2E-01	8.6E-01
0.0022	6.9%	-8.0E-02	-2.2E-07	-0.1%	-3.0E-02	8.6E-01
0.000075	13.1%	-6.0E-02	5.0E-09	0.0%	6.5E-04	8.6E-01
0	0.0%					
0	0.0%					
0	0.0%					
0	0.0%					
0	0.0%					
0.12	0.0%	9.6E-05	1.2E-10	0.0%	1.3E+03	8.6E-01
0.012	1.2%	-1.4E-01	2.7E-06	0.9%	1.0E+00	8.6E-01
0.012	1.2%	-1.4E-01	2.7E-06	0.9%	1.0E+00	8.6E-01
0.023	11.5%	7.3E-01	2.8E-04	96.2%	2.2E-01	8.7E-01
$u_c(y)$	$u_r(y)$					
	0.017	2.0%				
					Σ	
					100.0%	

	t_c / s	t_i / s	$t_{dead\ r} / \%$	t_d / s	$t_c / t_{1/2}$	$t_d / t_{1/2}$
10:39 AM	1292628	1264268	2.2%	2404405	0.54	1.0
4:52 PM	797	740	7.2%	3722775	0.00	0.0

Correlation matrix of ρ_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		t_i	μ	$t_{1/2\ a}$	$t_{1/2\ m}$
2.2E+04	2.1E-09	t_i		1	0	0
4.4E-02	2.1E-09	μ		0	1	0
2.4E+06	2.1E-09	$t_{1/2\ a}$		0	0	1
		$t_{1/2\ m}$		0	0	0
1.7E+08	2.1E-09	$t_{d\ a}$		0	0	0
		$t_{c\ a}$		0	0	0
2.4E+06	2.1E-09	$t_{i\ a}$		0	0	0
1.3E+06	2.1E-09	$t_{d\ m}$		0	0	0
1.3E+06	2.1E-09	$t_{c\ m}$		0	0	0
3.7E+06	2.1E-09	$t_{i\ m}$		0	0	0
8.0E+02	2.1E-09	$n_{p\ a}$		0	0	0
7.4E+02	2.1E-09	$n_{p\ m}$		0	0	0
		$k_{0\ Au}(a)$		0	0	0
		$k_{0\ Au}(m)$		0	0	0
		$G_{th\ a}$		0	0	0
		$G_{e\ a}$		0	0	0
5.1E+04	2.0E-09	$G_{th\ m}$		0	0	0
1.4E+05	2.1E-09	$G_{e\ m}$		0	0	0
2.6E-03	2.1E-09	f		0	0	0
1.3E+00	2.1E-09	α		0	0	0
1.0E+00	2.1E-09	$Q_{0\ a}$		0	0	0

1.0E+00	2.1E-09	E_{ra}	0	0	0	0
1.0E+00	2.1E-09	Q_{0m}	0	0	0	0
1.0E+00	2.1E-09	E_{rm}	0	0	0	0
1.5E+01	2.1E-09	$\varepsilon_{pm}^{geo} / \varepsilon_{pa}^i$	0	0	0	0
-4.2E-02	2.1E-09	COI_m / COI_a	0	0	0	0
4.2E-01	2.1E-09	m_m	0	0	0	0
6.7E+03	2.1E-09	m_a	0	0	0	0
		w_m	0	0	0	0
1.9E+00	2.1E-09	v	0	0	0	0
1.3E+02	2.1E-09					
3.4E-01	2.0E-09					
8.4E-01	2.1E-09					
8.4E-03	2.1E-09					
2.4E-01	2.1E-09					
4.6E-03	2.1E-09					
9.8E+01	2.1E-09					

Correlation matrix of $\varepsilon_{pm}^{geo} / \varepsilon_{pa}^{geo}$

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	3.4E-01	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	3.5E-01	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	3.7E-01	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	3.6E-01	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	3.5E-01	a_{-3}	0.748	-0.848	0.957	-0.993
1.2E+00	3.5E-01	$E_{\gamma m}$	0	0	0	0
3.2E-01	3.5E-01	$E_{\gamma a}$	0	0	0	0
-2.9E-01	3.5E-01	Δd_a	0	0	0	0
-2.9E-01	3.6E-01	Δd_m	0	0	0	0
		$\delta \varepsilon_{ra}$	0	0	0	0
		$\delta \varepsilon_{rm}$	0	0	0	0

3.8E-02 3.5E-01
 4.3E-02 3.5E-01

Correlation matrix of COI_m / COI_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	8.7E-01	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	8.7E-01	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	8.6E-01	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	8.6E-01	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	8.6E-01	a_{-3}	0.748	-0.848	0.957	-0.993
		$E_{\gamma^2 m}$	0	0	0	0
		$a_{\gamma^2 m}$	0	0	0	0
		$C_{\gamma^2 m}$	0	0	0	0
		$P/T_{\gamma^2 m}$	0	0	0	0
1.3E+03	8.6E-01					
9.9E-01	8.6E-01					
9.9E-01	8.6E-01					
1.7E-01	8.4E-01					

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$	Δd_a	Δd_m	$\delta \varepsilon_{ra}$	$\delta \varepsilon_{rm}$	c_i
0.748	0	0	0	0	0	0	3.0E-01
-0.848	0	0	0	0	0	0	0.0E+00
0.957	0	0	0	0	0	0	-8.0E-01
-0.993	0	0	0	0	0	0	-3.2E+00
1.000	0	0	0	0	0	0	-1.0E+01
0	1	0	0	0	0	0	-2.5E-01
0	0	1	0	0	0	0	9.2E-01
0	0	0	1	0	0	0	1.5E-02
0	0	0	0	1	0	0	-1.7E-02
0	0	0	0	0	1	1	0.0E+00
0	0	0	0	0	1	1	0.0E+00

Covariance

a_{-3}	$E_{\gamma 2 m}$	$a_{\gamma 2 m}$	$c_{\gamma 2 m}$	$P/T_{\gamma 2 m}$	c_i	
0.748	0	0	0	0	-1.9E-01	a_1
-0.848	0	0	0	0	-1.4E-01	a_0
0.957	0	0	0	0	-1.1E-01	a_{-1}
-0.993	0	0	0	0	-8.0E-02	a_{-2}
1.000	0	0	0	0	-6.0E-02	a_{-3}
0	1	0	0	0	9.6E-05	$E_{\gamma 2 m}$
0	0	1	0	0	-1.4E-01	$a_{\gamma 2 m}$
0	0	0	1	0	-1.4E-01	$c_{\gamma 2 m}$
0	0	0	0	1	7.3E-01	$P/T_{\gamma 2 m}$

c_i

0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Covariance matrix of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

	a_1	a_0	a_{-1}	a_{-2}	a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$
a_1	1.9E-03	-2.4E-03	7.5E-04	-7.7E-05	2.4E-06	0.0E+00	0.0E+00
a_0	-2.4E-03	3.2E-03	-1.1E-03	1.1E-04	-3.6E-06	0.0E+00	0.0E+00
a_{-1}	7.5E-04	-1.1E-03	3.8E-04	-4.3E-05	1.4E-06	0.0E+00	0.0E+00
a_{-2}	-7.7E-05	1.1E-04	-4.3E-05	4.9E-06	-1.7E-07	0.0E+00	0.0E+00
a_{-3}	2.4E-06	-3.6E-06	1.4E-06	-1.7E-07	5.7E-09	0.0E+00	0.0E+00
$E_{\gamma m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08	0.0E+00
$E_{\gamma a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08
Δd_a	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
Δd_m	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
c_i	3.0E-01	0.0E+00	-8.0E-01	-3.2E+00	-1.0E+01	-2.5E-01	9.2E-01

matrix of COI_m/COI_a

a_1	a_0	a_{-1}	a_{-2}	a_{-3}	$E_{\gamma 2 m}$	$a_{\gamma 2 m}$	$c_{\gamma 2 m}$	$P/T_{\gamma 2 m}$
1.9E-03	-2.4E-03	7.5E-04	-7.7E-05	2.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-2.4E-03	3.2E-03	-1.1E-03	1.1E-04	-3.6E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00
7.5E-04	-1.1E-03	3.8E-04	-4.3E-05	1.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-7.7E-05	1.1E-04	-4.3E-05	4.9E-06	-1.7E-07	0.0E+00	0.0E+00	0.0E+00	0.0E+00
2.4E-06	-3.6E-06	1.4E-06	-1.7E-07	5.7E-09	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-02	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	5.2E-04
-1.9E-01	-1.4E-01	-1.1E-01	-8.0E-02	-6.0E-02	9.6E-05	-1.4E-01	-1.4E-01	7.3E-01

0	0	0	0	0	0	0
1	0	0	0	0	0	0
0	1	0	0	0	0	0
0	0	1	0	0	0	0
0	0	0	1	0	0	0
0	0	0	0	1	0	0
0	0	0	0	0	1	0
0	0	0	0	0	0	1
0	0	0	0	0	0	0

Δd_a	Δd_m	$\delta \varepsilon_{r_a}$	$\delta \varepsilon_{r_m}$
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
8.3E-02	0.0E+00	0.0E+00	0.0E+00
0.0E+00	8.3E-02	0.0E+00	0.0E+00
0.0E+00	0.0E+00	2.5E-05	2.8E-05
0.0E+00	0.0E+00	2.8E-05	3.1E-05
1.5E-02	-1.7E-02	0.0E+00	0.0E+00

Covariance matrix of ρ_a

u	c_i	t_i	μ
0	3.0E-16	t_i	3.0E+02
0	-1.0E-10	μ	0.0E+00
0	1.1E-16	$t_{1/2 a}$	0.0E+00
0	-1.2E-17	$t_{1/2 m}$	0.0E+00
0	6.1E-16	$t_{d a}$	0.0E+00
0	3.6E-16	$t_{c a}$	0.0E+00
0	-1.7E-15	$t_{i a}$	0.0E+00
0	-8.7E-18	$t_{d m}$	0.0E+00
0	-1.1E-13	$t_{c m}$	0.0E+00
0	2.9E-12	$t_{i m}$	0.0E+00
0	4.0E-14	$n_{p a}$	0.0E+00
0	-1.5E-14	$n_{p m}$	0.0E+00
0	-8.0E-07	$k_{0 Au(a)}$	0.0E+00
0	1.6E-09	$k_{0 Au(m)}$	0.0E+00
0	-2.0E-09	$G_{th a}$	0.0E+00
0	-7.7E-11	$G_{e a}$	0.0E+00
0	1.8E-09	$G_{th m}$	0.0E+00
0	2.7E-10	$G_{e m}$	0.0E+00
0	-1.2E-11	f	0.0E+00
0	-9.0E-10	α	0.0E+00
0	-1.8E-10	$Q_{0 a}$	0.0E+00

0	-8.7E-17	E_{r_a}	0.0E+00	0.0E+00
0	1.4E-10	Q_{0_m}	0.0E+00	0.0E+00
0	5.8E-14	E_{r_m}	0.0E+00	0.0E+00
0	6.0E-09	$\varepsilon_{p_m}^{geo} / \varepsilon_{p_a}^{geo}$	0.0E+00	0.0E+00
0	2.4E-09	COI_m / COI_a	0.0E+00	0.0E+00
0	2.5E-07	m_m	0.0E+00	0.0E+00
0	-8.7E-09	m_a	0.0E+00	0.0E+00
0	4.6E-07	w_m	0.0E+00	0.0E+00
1	-2.1E-11	ν	0.0E+00	0.0E+00
		c_i	3.0E-16	-1.0E-10

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
1.1E-16	-1.2E-17	6.1E-16	3.6E-16	-1.7E-15	-8.7E-18

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-1.1E-13	2.9E-12	4.0E-14	-1.5E-14	-8.0E-07	1.6E-09

$G_{th a}$	$G_{e a}$	$G_{th m}$	$G_{e m}$	f	
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.1E-01
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-2.0E-09	-7.7E-11	1.8E-09	2.7E-10	-1.2E-11

α	Q_{0a}	E_{ra}	Q_{0m}	E_{rm}	$\varepsilon_{pm}^{geo} / \varepsilon_{pa}^{geo}$
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
4.1E-05	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	1.1E-02	0.0E+00	0.0E+00	0.0E+00	0.0E+00

0.0E+00	0.0E+00	6.9E+05	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	3.6E-03	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	4.8E+01	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	7.6E-05
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-9.0E-10	-1.8E-10	-8.7E-17	1.4E-10	5.8E-14	6.0E-09

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
2.9E-04	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	2.5E-09	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	2.5E-09	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	2.1E-09	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.4E+00
2.4E-09	2.5E-07	-8.7E-09	4.6E-07	-2.1E-11

Irradiation and γ -spectrometry

end irradiation 9/12/2017 2.46 PM
 irradiation time / s 21600

library CSF.Lib
 calib OR50_source2016_geom_cont_12052017.Clb
 sm type CSF.Lib (ROI32 Analysis)

Nuclide	Channel	Energy	Background
131Ba		1983.94	496.3
Co60		4691.96	1173.2

	target	product
analite, a	^{130}Ba	^{131}Ba
monitor, m	^{59}Co	^{60}Co

Uncertainty budget of ρ_a

Input Quantity	Quantity	Unit	Value
X_i	X_i	$[X_i]$	x_i
t_i		s	21600
μ		1	0.0445
$t_{1/2 a}$		s	993600
	λ_a	s^{-1}	7.0E-07
$t_{1/2 m}$		s	1.7E+08
	λ_m	s^{-1}	4.2E-09
$t_{d a}$		s	2404405
$t_{c a}$		s	1292628
$t_{i a}$		s	1264268
$t_{d m}$		s	3722775
$t_{c m}$		s	797
$t_{i m}$		s	740
	δ_a	1	1.022
	δ_m	1	1.077
	ξ_a	1	1.00098
	ξ_m	1	1.00319
$n_{p a}$		1	50777
$n_{p m}$		1	137487
$k_{0 Au(a)}$		1	0.00006480
$k_{0 Au(m)}$		1	1.3200
$G_{th a}$		1	1

$G_{e a}$		1	1
$G_{th m}$		1	1
$G_{e m}$		1	1
f		1	15.60
α		1	-0.0360
$Q_{0 a}$		1	24.8
$E_{r a}$		eV	69.9
	$Q_{0 a}(\alpha)$	1	28.85
$Q_{0 m}$		1	1.993
$E_{r m}$		eV	136.0
	$Q_{0 m}(\alpha)$	1	2.319
$\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$		1	0.5033
COI_m / COI_a		1	0.981
m_m		g	0.00847
m_a		g	0.24000
w_m		$g g^{-1}$	0.004597
ν		$mg L^{-1}$	99.2
Y		[Y]	y
ρ_a		$g mL^{-1}$	6.89E-08

Uncertainty budget of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

Input Quantity	Quantity	Unit	Value
X_i	X_i	[X_i]	x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
$a_{.1}$		Mev	0.403
$a_{.2}$		Mev2	-0.0320
$a_{.3}$		Mev3	0.000573
$E_{\gamma m}$		MeV	1.17320
$E_{\gamma a}$		MeV	0.49630
Δd_a		mm	0
Δd_m		mm	0
	e_4	keV-4	-7.1E-11
	e_3	keV-3	5.2E-08
	e_2	keV-2	-1.4E-05
	e_1	keV-1	1.8E-03
	e_0		1 -4.5E-02
	d_1	keV-1	5.6E-06

	d_0		1	4.2E-02
$\delta\epsilon_{ra}$		mm^{-1}		0.044
$\delta\epsilon_{rm}$		mm^{-1}		0.048
Y		[Y]	y	
$\epsilon_{pm}^{\text{geo}} / \epsilon_{pa}^{\text{geo}}$		1		0.503

Uncertainty budget of $\text{COI}_m / \text{COI}_a$

Input Quantity	Quantity X_i	Unit [X_i]	Value x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
a_{-1}		Mev	0.403
a_{-2}		Mev2	-0.0320
a_{-3}		Mev3	0.000573
	b_1		1 -0.571
	b_0		1 1.079
	c_2		1 -1.625
	c_1		1 6.678
	c_0		1 -7.006
$E_{\gamma 2m}$		keV	1332.5
$a_{\gamma 2m}$			1 1.000
$c_{\gamma 2m}$			1 1.000
$P/T_{\gamma 2m}$			1 0.197
$E_{\gamma 29a}$		keV	123.80
$a_{\gamma 29a}$			1 1.000
$c_{\gamma 29a}$			1 0.550
$P/T_{\gamma 29a}$			1 0.712
	Y	[Y]	y
	$\text{COI}_m / \text{COI}_a$		1 0.981

Net area	Cnts/s	Uncert %	FWHM	source file	start counting
50777	0.04	2.37	1.368	OR50_20171025_CSF_si	10/10/2017
137487	185.919	0.32	1.798	OR50_20170925_Co_sa	10/25/2017

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance y $u^2_y(x_i)$	Index	Input for sensit coeff $x_i+u(x_i)$ $y(x_i+u(x_i))$	
17	0.1%	2.4E-14	1.7E-25	0.0%	2.2E+04	6.9E-08
0.0005	1.1%	-3.4E-09	2.9E-24	0.0%	4.5E-02	6.9E-08
5184	0.5%	-7.4E-14	1.5E-19	0.2%	1.0E+06	6.8E-08
3.6E-09	0.5%					
2.6E+04	0.0%	-4.1E-16	1.1E-22	0.0%	1.7E+08	6.9E-08
6.5E-13	0.0%					
35	0.0%	4.8E-14	2.8E-24	0.0%	2.4E+06	6.9E-08
0.3	0.0%	2.3E-14	4.3E-29	0.0%	1.3E+06	6.9E-08
0.3	0.0%	-5.7E-14	2.7E-28	0.0%	1.3E+06	6.9E-08
35	0.0%	-2.9E-16	9.9E-29	0.0%	3.7E+06	6.9E-08
0.3	0.0%	-3.6E-12	1.1E-24	0.0%	8.0E+02	6.9E-08
0.3	0.0%	9.7E-11	7.8E-22	0.0%	7.4E+02	6.9E-08
0.000	0.0%					
0.001	0.1%					
0.00001	0.0%					
0.00004	0.0%					
1203	2.4%	1.4E-12	2.7E-18	2.9%	5.2E+04	7.1E-08
440	0.3%	-5.0E-13	4.9E-20	0.1%	1.4E+05	6.9E-08
0.00000013	0.2%	-1.1E-03	1.9E-20	0.0%	6.5E-05	6.9E-08
0.0053	0.4%	5.2E-08	7.6E-20	0.1%	1.3E+00	6.9E-08
0	0.0%	-2.4E-08	0.0E+00	0.0%	1.0E+00	6.9E-08

	0.0000	0.0%					
	0.005	11.5%	0.0E+00	0.0E+00	0.0%	5.0E-02	5.0E-01
	0.006	11.5%	0.0E+00	0.0E+00	0.0%	5.4E-02	5.0E-01
$u_c(y)$	$u_{c,r}(y)$				Σ		
	0.013	2.5%			100.0%		

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance y $u^2_y(x_i)$	Index	Input for sensit coeff	
					$x_i+u(x_i)$	$y(x_i+u(x_i))$
0.043	9.2%	-0.2000	1.7E-05	7.1%	-4.3E-01	9.7E-01
0.057	1.8%	-0.0216	-1.9E-06	-0.8%	-3.2E+00	9.8E-01
0.020	4.8%	1.0307	-2.3E-05	-9.6%	4.2E-01	1.0E+00
0.0022	6.9%	9.2132	2.0E-05	8.3%	-3.0E-02	1.0E+00
0.000075	13.1%	74.6117	-5.0E-06	-2.1%	6.5E-04	9.9E-01
0	0.0%					
0	0.0%					
0	0.0%					
0	0.0%					
0	0.0%					
0.1	0.0%	0.0001	1.6E-10	0.0%	1.3E+03	9.8E-01
0.012	1.2%	-0.1632	3.6E-06	1.5%	1.0E+00	9.8E-01
0.012	1.2%	-0.1632	3.6E-06	1.5%	1.0E+00	9.8E-01
0.023	11.5%	0.8402	2.8E-04	116.9%	2.2E-01	1.0E+00
0.12	0.1%	-0.0001	4.8E-11	0.0%	1.2E+02	9.8E-01
0.012	1.2%	0.1416	2.7E-06	1.1%	1.0E+00	9.8E-01
0.012	2.1%	0.2575	8.8E-06	3.7%	5.6E-01	9.8E-01
0.023	3.2%	-0.1991	-6.6E-05	-27.7%	7.4E-01	9.8E-01
$u_c(y)$	$u_r(y)$				Σ	
	0.015	1.6%			100.0%	

	t_c / s	t_i / s	$t_{dead\ r} / \%$	t_d / s	$t_c / t_{1/2}$	$t_d / t_{1/2}$
10:39 AM	1292628	1264268	2.2%	2404405	1.30	2.4
4:52 PM	797	740	7.2%	3722775	0.00	0.0

Correlation matrix of ρ_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		t_i	μ	$t_{1/2\ a}$	$t_{1/2\ m}$
2.2E+04	6.9E-08	t_i		1	0	0
4.4E-02	6.9E-08	μ		0	1	0
9.9E+05	6.9E-08	$t_{1/2\ a}$		0	0	1
		$t_{1/2\ m}$		0	0	0
1.7E+08	6.9E-08	$t_{d\ a}$		0	0	0
		$t_{c\ a}$		0	0	0
2.4E+06	6.9E-08	$t_{i\ a}$		0	0	0
1.3E+06	6.9E-08	$t_{d\ m}$		0	0	0
1.3E+06	6.9E-08	$t_{c\ m}$		0	0	0
3.7E+06	6.9E-08	$t_{i\ m}$		0	0	0
8.0E+02	6.9E-08	$n_{p\ a}$		0	0	0
7.4E+02	6.9E-08	$n_{p\ m}$		0	0	0
		$k_{0\ Au}(a)$		0	0	0
		$k_{0\ Au}(m)$		0	0	0
		$G_{th\ a}$		0	0	0
		$G_{e\ a}$		0	0	0
5.0E+04	6.7E-08	$G_{th\ m}$		0	0	0
1.4E+05	6.9E-08	$G_{e\ m}$		0	0	0
6.5E-05	6.9E-08	f		0	0	0
1.3E+00	6.9E-08	α		0	0	0
1.0E+00	6.9E-08	$Q_{0\ a}$		0	0	0

1.0E+00	6.9E-08	E_{ra}	0	0	0	0
1.0E+00	6.9E-08	Q_{0m}	0	0	0	0
1.0E+00	6.9E-08	E_{rm}	0	0	0	0
1.5E+01	6.8E-08	$\varepsilon_{pm}^{geo} / \varepsilon_{pa}^i$	0	0	0	0
-4.2E-02	6.8E-08	COI_m / COI_a	0	0	0	0
2.0E+01	7.9E-08	m_m	0	0	0	0
6.6E+01	6.9E-08	m_a	0	0	0	0
		w_m	0	0	0	0
1.9E+00	6.9E-08	v	0	0	0	0
1.3E+02	6.9E-08					
4.9E-01	6.7E-08					
9.7E-01	6.8E-08					
8.4E-03	6.8E-08					
2.4E-01	6.9E-08					
4.6E-03	6.8E-08					
9.8E+01	7.0E-08					

Correlation matrix of $\varepsilon_{pm}^{geo} / \varepsilon_{pa}^{geo}$

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	4.9E-01	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	5.0E-01	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	5.1E-01	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	5.1E-01	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	5.0E-01	a_{-3}	0.748	-0.848	0.957	-0.993
1.2E+00	5.0E-01	$E_{\gamma m}$	0	0	0	0
5.0E-01	5.0E-01	$E_{\gamma a}$	0	0	0	0
-2.9E-01	5.0E-01	Δd_a	0	0	0	0
-2.9E-01	5.1E-01	Δd_m	0	0	0	0
		$\delta \varepsilon_{ra}$	0	0	0	0
		$\delta \varepsilon_{rm}$	0	0	0	0

3.9E-02 5.0E-01
 4.3E-02 5.0E-01

Correlation matrix of COI_m / COI_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	9.9E-01	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	9.8E-01	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	9.6E-01	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	9.6E-01	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	9.8E-01	a_{-3}	0.748	-0.848	0.957	-0.993
		$E_{\gamma 2 m}$	0	0	0	0
		$a_{\gamma 2 m}$	0	0	0	0
		$C_{\gamma 2 m}$	0	0	0	0
		$P/T_{\gamma 2 m}$	0	0	0	0
		$E_{\gamma 29 a}$	0	0	0	0
1.3E+03	9.8E-01	$a_{\gamma 29 a}$	0	0	0	0
9.9E-01	9.8E-01	$C_{\gamma 29 a}$	0	0	0	0
9.9E-01	9.8E-01	$P/T_{\gamma 29 a}$	0	0	0	0
1.7E-01	9.6E-01					
1.2E+02	9.8E-01					
9.9E-01	9.8E-01					
5.4E-01	9.8E-01					
6.9E-01	9.9E-01					

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$	Δd_a	Δd_m	$\delta \varepsilon_{ra}$	$\delta \varepsilon_{rm}$	c_i
0.748	0	0	0	0	0	0	3.4E-01
-0.848	0	0	0	0	0	0	0.0E+00
0.957	0	0	0	0	0	0	-5.9E-01
-0.993	0	0	0	0	0	0	-1.7E+00
1.000	0	0	0	0	0	0	-3.8E+00
0	1	0	0	0	0	0	-3.7E-01
0	0	1	0	0	0	0	8.1E-01
0	0	0	1	0	0	0	2.2E-02
0	0	0	0	1	0	0	-2.4E-02
0	0	0	0	0	1	1	0.0E+00
0	0	0	0	0	1	1	0.0E+00

a_{-3}	$E_{\gamma 2 m}$	$a_{\gamma 2 m}$	$c_{\gamma 2 m}$	$P/T_{\gamma 2 m}$	$E_{\gamma 29 a}$	$a_{\gamma 29 a}$	$c_{\gamma 29 a}$	$P/T_{\gamma 29 a}$	
0.748	0	0	0	0	0	0	0	0	0
-0.848	0	0	0	0	0	0	0	0	0
0.957	0	0	0	0	0	0	0	0	0
-0.993	0	0	0	0	0	0	0	0	0
1.000	0	0	0	0	0	0	0	0	0
0	1	0	0	0	0	0	0	0	0
0	0	1	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0	0	0
0	0	0	0	1	0	0	0	0	1
0	0	0	0	0	1	0	0	0	0
0	0	0	0	0	0	1	0	0	0
0	0	0	0	0	0	0	1	0	0
0	0	0	0	0	0	0	0	1	0
0	0	0	0	0	1	0	0	0	1

0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Covariance matrix of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

	a_1	a_0	a_{-1}	a_{-2}	a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$
a_1	1.9E-03	-2.4E-03	7.5E-04	-7.7E-05	2.4E-06	0.0E+00	0.0E+00
a_0	-2.4E-03	3.2E-03	-1.1E-03	1.1E-04	-3.6E-06	0.0E+00	0.0E+00
a_{-1}	7.5E-04	-1.1E-03	3.8E-04	-4.3E-05	1.4E-06	0.0E+00	0.0E+00
a_{-2}	-7.7E-05	1.1E-04	-4.3E-05	4.9E-06	-1.7E-07	0.0E+00	0.0E+00
a_{-3}	2.4E-06	-3.6E-06	1.4E-06	-1.7E-07	5.7E-09	0.0E+00	0.0E+00
$E_{\gamma m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08	0.0E+00
$E_{\gamma a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08
Δd_a	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
Δd_m	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
c_i	3.4E-01	0.0E+00	-5.9E-01	-1.7E+00	-3.8E+00	-3.7E-01	8.1E-01

Covariance matrix of COI_m/COI_a

c_i		a₁	a₀	a₋₁
-2.0E-01	a ₁	1.9E-03	-2.4E-03	7.5E-04
-2.2E-02	a ₀	-2.4E-03	3.2E-03	-1.1E-03
1.0E+00	a ₋₁	7.5E-04	-1.1E-03	3.8E-04
9.2E+00	a ₋₂	-7.7E-05	1.1E-04	-4.3E-05
7.5E+01	a ₋₃	2.4E-06	-3.6E-06	1.4E-06
1.1E-04	E _{γ2 m}	0.0E+00	0.0E+00	0.0E+00
-1.6E-01	a _{γ2 m}	0.0E+00	0.0E+00	0.0E+00
-1.6E-01	c _{γ2 m}	0.0E+00	0.0E+00	0.0E+00
8.4E-01	P/T _{γ2 m}	0.0E+00	0.0E+00	0.0E+00
-6.0E-05	E _{γ29 a}	0.0E+00	0.0E+00	0.0E+00
1.4E-01	a _{γ29 a}	0.0E+00	0.0E+00	0.0E+00
2.6E-01	c _{γ29 a}	0.0E+00	0.0E+00	0.0E+00
-2.0E-01	P/T _{γ29 a}	0.0E+00	0.0E+00	0.0E+00
	c_i	-2.0E-01	-2.2E-02	1.0E+00

0	0	0	0	0	0	0
1	0	0	0	0	0	0
0	1	0	0	0	0	0
0	0	1	0	0	0	0
0	0	0	1	0	0	0
0	0	0	0	1	0	0
0	0	0	0	0	1	0
0	0	0	0	0	0	1
0	0	0	0	0	0	0

Δd_a	Δd_m	$\delta \varepsilon_{r_a}$	$\delta \varepsilon_{r_m}$
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
8.3E-02	0.0E+00	0.0E+00	0.0E+00
0.0E+00	8.3E-02	0.0E+00	0.0E+00
0.0E+00	0.0E+00	2.6E-05	2.9E-05
0.0E+00	0.0E+00	2.9E-05	3.1E-05
2.2E-02	-2.4E-02	0.0E+00	0.0E+00

a_{-2}	a_{-3}	$E_{\gamma 2 m}$	$a_{\gamma 2 m}$	$C_{\gamma 2 m}$	$P/T_{\gamma 2 m}$	$E_{\gamma 29 a}$
-7.7E-05	2.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
1.1E-04	-3.6E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-4.3E-05	1.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
4.9E-06	-1.7E-07	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-1.7E-07	5.7E-09	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	1.3E-02	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	5.2E-04	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-02
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	5.2E-04	0.0E+00
9.2E+00	7.5E+01	1.1E-04	-1.6E-01	-1.6E-01	8.4E-01	-6.0E-05

Covariance matrix of ρ_a

ν	c_i	t_i	μ
0	2.4E-14	t_i	3.0E+02
0	-3.4E-09	μ	0.0E+00
0	-7.4E-14	$t_{1/2 a}$	0.0E+00
0	-4.1E-16	$t_{1/2 m}$	0.0E+00
0	4.8E-14	$t_{d a}$	0.0E+00
0	2.3E-14	$t_{c a}$	0.0E+00
0	-5.7E-14	$t_{i a}$	0.0E+00
0	-2.9E-16	$t_{d m}$	0.0E+00
0	-3.6E-12	$t_{c m}$	0.0E+00
0	9.7E-11	$t_{i m}$	0.0E+00
0	1.4E-12	$n_{p a}$	0.0E+00
0	-5.0E-13	$n_{p m}$	0.0E+00
0	-1.1E-03	$k_{0 Au(a)}$	0.0E+00
0	5.2E-08	$k_{0 Au(m)}$	0.0E+00
0	-2.4E-08	$G_{th a}$	0.0E+00
0	-4.5E-08	$G_{e a}$	0.0E+00
0	6.0E-08	$G_{th m}$	0.0E+00
0	8.9E-09	$G_{e m}$	0.0E+00
0	2.3E-09	f	0.0E+00
0	1.5E-07	α	0.0E+00
0	-1.8E-09	$Q_{0 a}$	0.0E+00

0	-2.3E-11	E_{r_a}	0.0E+00	0.0E+00
0	4.6E-09	Q_{0_m}	0.0E+00	0.0E+00
0	1.9E-12	E_{r_m}	0.0E+00	0.0E+00
0	1.4E-07	$\varepsilon_{p_m}^{geo} / \varepsilon_{p_a}^{geo}$	0.0E+00	0.0E+00
0	7.0E-08	COI_m / COI_a	0.0E+00	0.0E+00
0	8.1E-06	m_m	0.0E+00	0.0E+00
0	-2.9E-07	m_a	0.0E+00	0.0E+00
0	1.5E-05	w_m	0.0E+00	0.0E+00
1	-6.9E-10	ν	0.0E+00	0.0E+00
		c_i	2.4E-14	-3.4E-09

$a_{\gamma 29 a}$	$c_{\gamma 29 a}$	$P/T_{\gamma 29 a}$
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	5.2E-04
0.0E+00	0.0E+00	0.0E+00
1.3E-04	0.0E+00	0.0E+00
0.0E+00	1.3E-04	0.0E+00
0.0E+00	0.0E+00	5.2E-04
1.4E-01	2.6E-01	-2.0E-01

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-7.4E-14	-4.1E-16	4.8E-14	2.3E-14	-5.7E-14	-2.9E-16

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-3.6E-12	9.7E-11	1.4E-12	-5.0E-13	-1.1E-03	5.2E-08

$G_{th a}$	$G_{e a}$	$G_{th m}$	$G_{e m}$	f	
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.1E-01
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-2.4E-08	-4.5E-08	6.0E-08	8.9E-09	2.3E-09

0.0E+00	0.0E+00	1.2E+01	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	3.6E-03	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	4.8E+01	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.6E-04
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
1.5E-07	-1.8E-09	-2.3E-11	4.6E-09	1.9E-12	1.4E-07

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
2.4E-04	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	2.5E-09	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	2.5E-09	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	2.1E-09	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.4E+00
7.0E-08	8.1E-06	-2.9E-07	1.5E-05	-6.9E-10

Irradiation and γ -spectrometry

end irradiation 9/12/2017 2.46 PM
 irradiation time / s 21600

library CSF.Lib
 calib OR50_source2016_geom_cont_12052017.Clb
 sm type CSF.Lib (ROI32 Analysis)

Nuclide	Channel	Energy	Background
124Sb		6765.27	1691
Co60		4691.96	1173.2

	target	product
analite, a	^{123}Sb	^{124}Sb
monitor, m	^{59}Co	^{60}Co

Uncertainty budget of ρ_a

Input Quantity	Quantity	Unit	Value
X_i	X_i	$[X_i]$	x_i
t_i		s	21600
μ		1	0.0445
$t_{1/2 a}$		s	5201280
	λ_a	s^{-1}	1.3E-07
$t_{1/2 m}$		s	1.7E+08
	λ_m	s^{-1}	4.2E-09
$t_{d a}$		s	2404405
$t_{c a}$		s	1292628
$t_{i a}$		s	1264268
$t_{d m}$		s	3722775
$t_{c m}$		s	797
$t_{i m}$		s	740
	δ_a	1	1.022
	δ_m	1	1.077
	ξ_a	1	1.00098
	ξ_m	1	1.00319
$n_{p a}$		1	2474
$n_{p m}$		1	137487
$k_{0 Au(a)}$		1	0.01410
$k_{0 Au(m)}$		1	1.3200
$G_{th a}$		1	1

$G_{e a}$		1	1
$G_{th m}$		1	1
$G_{e m}$		1	1
f		1	15.60
α		1	-0.0360
$Q_{0 a}$		1	28.8
$E_{r a}$		eV	28.2
	$Q_{0 a}(\alpha)$	1	32.45
$Q_{0 m}$		1	1.993
$E_{r m}$		eV	136.0
	$Q_{0 m}(\alpha)$	1	2.319
$\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$		1	1.4022
COI_m / COI_a		1	1.030
m_m		g	0.00847
m_a		g	0.24000
w_m		$g g^{-1}$	0.004597
ν		$mg L^{-1}$	99.2
Y		[Y]	y
ρ_a		$g mL^{-1}$	4.01E-11

Uncertainty budget of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

Input Quantity	Quantity	Unit	Value
X_i	X_i	[X_i]	x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
$a_{.1}$		Mev	0.403
$a_{.2}$		Mev2	-0.0320
$a_{.3}$		Mev3	0.000573
$E_{\gamma m}$		MeV	1.17320
$E_{\gamma a}$		MeV	1.69100
Δd_a		mm	0
Δd_m		mm	0
	e_4	keV-4	-7.1E-11
	e_3	keV-3	5.2E-08
	e_2	keV-2	-1.4E-05
	e_1	keV-1	1.8E-03
	e_0		1 -4.5E-02
	d_1	keV-1	5.6E-06

	d_0		1	4.2E-02
$\delta\epsilon_{ra}$		mm^{-1}		0.051
$\delta\epsilon_{rm}$		mm^{-1}		0.048
Y		[Y]	y	
$\epsilon_{pm}^{\text{geo}} / \epsilon_{pa}^{\text{geo}}$		1		1.402

Uncertainty budget of $\text{COI}_m / \text{COI}_a$

Input Quantity	Quantity X_i	Unit [X_i]	Value x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
a_{-1}		Mev	0.403
a_{-2}		Mev2	-0.0320
a_{-3}		Mev3	0.000573
	b_1		1 -0.571
	b_0		1 1.079
	c_2		1 -1.625
	c_1		1 6.678
	c_0		1 -7.006
$E_{\gamma 2m}$		keV	1332.5
$a_{\gamma 2m}$			1 1.000
$c_{\gamma 2m}$			1 1.000
$P/T_{\gamma 2m}$			1 0.197
$E_{\gamma 12a}$		keV	1691.00
$P_{\gamma 12a}$			1 47.60%
$E_{\gamma 24a}$		keV	602.70
$a_{\gamma 24a}$			1 1.000
$c_{\gamma 24a}$			1 1.000
$P/T_{\gamma 24a}$			1 0.310
$E_{\gamma 13a}$		keV	1045.10
$P_{\gamma 13a}$			1 1.82%
$E_{\gamma 23a}$		keV	645.90
$a_{\gamma 23a}$			1 1.000
$c_{\gamma 23a}$			1 1.000
$E_{\gamma 14a}$		keV	962.20
$P_{\gamma 14a}$			1 1.88%
$E_{\gamma 22a}$		keV	722.80
$a_{\gamma 22a}$			1 0.890

$C_{\gamma 22 a}$

1

1.000

Y

[Y]

y

COI_m / COI_a

1

1.030

Net area	Cnts/s	Uncert %	FWHM	source file	start counting
2474	0.002	8.61	1.924	OR50_20171025_CSF_si	10/10/2017
137487	185.919	0.32	1.798	OR50_20170925_Co_sa	10/25/2017

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance y $u^2_y(x_i)$	Index	Input for sensit coeff $x_i+u(x_i)$ $y(x_i+u(x_i))$	
17	0.1%	2.6E-18	2.0E-33	0.0%	2.2E+04	4.0E-11
0.0005	1.1%	-2.0E-12	9.9E-31	0.0%	4.5E-02	4.0E-11
2592	0.0%	4.6E-18	1.4E-28	0.0%	5.2E+06	4.0E-11
6.6E-11	0.0%					
2.6E+04	0.0%	-2.4E-19	3.8E-29	0.0%	1.7E+08	4.0E-11
6.5E-13	0.0%					
35	0.0%	5.3E-18	3.4E-32	0.0%	2.4E+06	4.0E-11
0.3	0.0%	3.9E-18	1.3E-36	0.0%	1.3E+06	4.0E-11
0.3	0.0%	-3.3E-17	9.1E-35	0.0%	1.3E+06	4.0E-11
35	0.0%	-1.7E-19	3.4E-35	0.0%	3.7E+06	4.0E-11
0.3	0.0%	-2.1E-15	3.6E-31	0.0%	8.0E+02	4.0E-11
0.3	0.0%	5.6E-14	2.7E-28	0.0%	7.4E+02	4.0E-11
0.000	0.0%					
0.001	0.1%					
0.00001	0.0%					
0.00004	0.0%					
213	8.6%	1.6E-14	1.2E-23	77.6%	2.7E+03	4.4E-11
440	0.3%	-2.9E-16	1.6E-26	0.1%	1.4E+05	4.0E-11
0.00016	1.1%	-2.8E-09	1.9E-25	1.3%	1.4E-02	4.0E-11
0.0053	0.4%	3.0E-11	2.6E-26	0.2%	1.3E+00	4.0E-11
0	0.0%	-1.3E-11	0.0E+00	0.0%	1.0E+00	4.0E-11

	0.0000	0.0%					
	0.006	11.5%	0.0E+00	0.0E+00	0.0%	5.7E-02	1.4E+00
	0.006	11.5%	0.0E+00	0.0E+00	0.0%	5.4E-02	1.4E+00
$u_c(y)$	$u_{c,r}(y)$			Σ			
	0.039	2.8%			100.0%		

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance y $u^2_y(x_i)$	Index	Input for sensit coeff $x_i+u(x_i)$ $y(x_i+u(x_i))$	
0.043	9.2%	-0.0990	1.5E-05	24.5%	-4.3E-01	1.0E+00
0.057	1.8%	0.0377	6.8E-06	11.2%	-3.2E+00	1.0E+00
0.020	4.8%	0.2171	-1.1E-05	-18.2%	4.2E-01	1.0E+00
0.0022	6.9%	0.4785	2.3E-06	3.9%	-3.0E-02	1.0E+00
0.000075	13.1%	0.8856	-1.3E-07	-0.2%	6.5E-04	1.0E+00
0	0.0%					
0	0.0%					
0	0.0%					
0	0.0%					
0	0.0%					
0.1	0.0%	0.0001	1.8E-10	0.0%	1.3E+03	1.0E+00
0.012	1.2%	-0.1714	3.9E-06	6.5%	1.0E+00	1.0E+00
0.012	1.2%	-0.1714	3.9E-06	6.5%	1.0E+00	1.0E+00
0.023	11.5%	0.8823	-1.1E-04	-173.7%	2.2E-01	1.0E+00
0.12	0.0%	0.0000	1.6E-13	0.0%	1.7E+03	1.0E+00
0.12%	0.2%	0.0122	2.0E-10	0.0%	4.8E-01	1.0E+00
0.12	0.0%	-0.0003	1.0E-09	0.0%	6.0E+02	1.0E+00
0.012	1.2%	0.2148	6.2E-06	10.2%	1.0E+00	1.0E+00
0.012	1.2%	0.2148	6.2E-06	10.2%	1.0E+00	1.0E+00
0.036	11.5%	-0.7075	1.3E-04	219.2%	3.5E-01	1.0E+00
0.12	0.0%	0.0000	7.7E-14	0.0%	1.0E+03	1.0E+00
0.12%	6.3%	-0.1683	3.8E-08	0.1%	1.9E-02	1.0E+00
0.12	0.0%	0.0000	1.8E-13	0.0%	6.5E+02	1.0E+00
0.012	1.2%	-0.0031	1.3E-09	0.0%	1.0E+00	1.0E+00
0.012	1.2%	-0.0031	1.3E-09	0.0%	1.0E+00	1.0E+00
0.12	0.0%	0.0000	7.1E-14	0.0%	9.6E+02	1.0E+00
0.12%	6.1%	-0.1467	2.9E-08	0.0%	2.0E-02	1.0E+00
0.12	0.0%	0.0000	1.2E-13	0.0%	7.2E+02	1.0E+00
0.012	1.3%	-0.0031	1.3E-09	0.0%	9.0E-01	1.0E+00

	0.012	1.2%	-0.0028	1.0E-09	0.0%	1.0E+00	1.0E+00
$u_c(y)$	$u_r(y)$				Σ		
	0.008	0.8%			100.0%		

	t_c / s	t_i / s	$t_{dead\ r} / \%$	t_d / s	$t_c / t_{1/2}$	$t_d / t_{1/2}$
10:39 AM	1292628	1264268	2.2%	2404405	0.25	0.5
4:52 PM	797	740	7.2%	3722775	0.00	0.0

Correlation matrix of ρ_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		t_i	μ	$t_{1/2\ a}$	$t_{1/2\ m}$
2.2E+04	4.0E-11	t_i	1	0	0	0
4.4E-02	4.0E-11	μ	0	1	0	0
5.2E+06	4.0E-11	$t_{1/2\ a}$	0	0	1	0
		$t_{1/2\ m}$	0	0	0	1
1.7E+08	4.0E-11	$t_{d\ a}$	0	0	0	0
		$t_{c\ a}$	0	0	0	0
2.4E+06	4.0E-11	$t_{i\ a}$	0	0	0	0
1.3E+06	4.0E-11	$t_{d\ m}$	0	0	0	0
1.3E+06	4.0E-11	$t_{c\ m}$	0	0	0	0
3.7E+06	4.0E-11	$t_{i\ m}$	0	0	0	0
8.0E+02	4.0E-11	$n_{p\ a}$	0	0	0	0
7.4E+02	4.0E-11	$n_{p\ m}$	0	0	0	0
		$k_{0\ Au}(a)$	0	0	0	0
		$k_{0\ Au}(m)$	0	0	0	0
		$G_{th\ a}$	0	0	0	0
		$G_{e\ a}$	0	0	0	0
2.3E+03	3.7E-11	$G_{th\ m}$	0	0	0	0
1.4E+05	4.0E-11	$G_{e\ m}$	0	0	0	0
1.4E-02	4.1E-11	f	0	0	0	0
1.3E+00	4.0E-11	α	0	0	0	0
1.0E+00	4.0E-11	$Q_{0\ a}$	0	0	0	0

1.0E+00	4.0E-11	E_{ra}	0	0	0	0
1.0E+00	4.0E-11	Q_{0m}	0	0	0	0
1.0E+00	4.0E-11	E_{rm}	0	0	0	0
1.5E+01	4.0E-11	$\varepsilon_{pm}^{geo} / \varepsilon_{pa}^i$	0	0	0	0
-4.2E-02	4.0E-11	COI_m / COI_a	0	0	0	0
2.8E+01	4.1E-11	m_m	0	0	0	0
2.6E+01	4.0E-11	m_a	0	0	0	0
		w_m	0	0	0	0
1.9E+00	4.0E-11	v	0	0	0	0
1.3E+02	4.0E-11					
1.4E+00	3.9E-11					
1.0E+00	4.0E-11					
8.4E-03	4.0E-11					
2.4E-01	4.0E-11					
4.6E-03	4.0E-11					
9.8E+01	4.1E-11					

Correlation matrix of $\varepsilon_{pm}^{geo} / \varepsilon_{pa}^{geo}$

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	1.4E+00	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	1.4E+00	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	1.4E+00	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	1.4E+00	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	1.4E+00	a_{-3}	0.748	-0.848	0.957	-0.993
1.2E+00	1.4E+00	$E_{\gamma m}$	0	0	0	0
1.7E+00	1.4E+00	$E_{\gamma a}$	0	0	0	0
-2.9E-01	1.4E+00	Δd_a	0	0	0	0
-2.9E-01	1.4E+00	Δd_m	0	0	0	0
		$\delta \varepsilon_{ra}$	0	0	0	0
		$\delta \varepsilon_{rm}$	0	0	0	0

4.5E-02 1.4E+00
 4.3E-02 1.4E+00

Correlation matrix of COI_m / COI_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	1.0E+00	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	1.0E+00	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	1.0E+00	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	1.0E+00	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	1.0E+00	a_{-3}	0.748	-0.848	0.957	-0.993
		$E_{\gamma 2 m}$	0	0	0	0
		$a_{\gamma 2 m}$	0	0	0	0
		$C_{\gamma 2 m}$	0	0	0	0
		$P/T_{\gamma 2 m}$	0	0	0	0
		$E_{\gamma 12 a}$	0	0	0	0
1.3E+03	1.0E+00	$P_{\gamma 12 a}$	0	0	0	0
9.9E-01	1.0E+00	$E_{\gamma 24 a}$	0	0	0	0
9.9E-01	1.0E+00	$a_{\gamma 24 a}$	0	0	0	0
1.7E-01	1.0E+00	$C_{\gamma 24 a}$	0	0	0	0
1.7E+03	1.0E+00	$P/T_{\gamma 24 a}$	0	0	0	0
4.7E-01	1.0E+00	$E_{\gamma 13 a}$	0	0	0	0
6.0E+02	1.0E+00	$P_{\gamma 13 a}$	0	0	0	0
9.9E-01	1.0E+00	$E_{\gamma 23 a}$	0	0	0	0
9.9E-01	1.0E+00	$a_{\gamma 23 a}$	0	0	0	0
2.7E-01	1.1E+00	$C_{\gamma 23 a}$	0	0	0	0
1.0E+03	1.0E+00	$E_{\gamma 14 a}$	0	0	0	0
1.7E-02	1.0E+00	$P_{\gamma 14 a}$	0	0	0	0
6.5E+02	1.0E+00	$E_{\gamma 22 a}$	0	0	0	0
9.9E-01	1.0E+00	$a_{\gamma 22 a}$	0	0	0	0
9.9E-01	1.0E+00	$C_{\gamma 22 a}$	0	0	0	0
9.6E+02	1.0E+00					
1.8E-02	1.0E+00					
7.2E+02	1.0E+00					
8.8E-01	1.0E+00					

9.9E-01 1.0E+00

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$	Δd_a	Δd_m	$\delta \varepsilon_{ra}$	$\delta \varepsilon_{rm}$	c_i
0.748	0	0	0	0	0	0	-7.3E-01
-0.848	0	0	0	0	0	0	0.0E+00
0.957	0	0	0	0	0	0	3.7E-01
-0.993	0	0	0	0	0	0	5.3E-01
1.000	0	0	0	0	0	0	5.8E-01
0	1	0	0	0	0	0	-1.0E+00
0	0	1	0	0	0	0	8.4E-01
0	0	0	1	0	0	0	7.2E-02
0	0	0	0	1	0	0	-6.8E-02
0	0	0	0	0	1	1	0.0E+00
0	0	0	0	0	0	1	0.0E+00

$k_{0\text{Au}}(m)$	$G_{\text{th}a}$	$G_{e a}$	$G_{\text{th}m}$	$G_{e m}$	f	α	Q_{0a}	$E_{r a}$	Q_{0m}	
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0	0	0
0	1	0	0	0	0	0	0	0	0	0
0	0	1	0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0	0	0	0
0	0	0	0	1	0	0	0	0	0	0
0	0	0	0	0	1	0	0	0	0	0
0	0	0	0	0	0	1	0	0	0	0
0	0	0	0	0	0	0	1	0	0	0
0	0	0	0	0	0	0	0	1	0	0

0	0	0	0	0	0	0	0	1	0
0	0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

Covariance matrix of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

	a_1	a_0	a_{-1}	a_{-2}	a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$	Δd_a
a_1	1.9E-03	-2.4E-03	7.5E-04	-7.7E-05	2.4E-06	0.0E+00	0.0E+00	0.0E+00
a_0	-2.4E-03	3.2E-03	-1.1E-03	1.1E-04	-3.6E-06	0.0E+00	0.0E+00	0.0E+00
a_{-1}	7.5E-04	-1.1E-03	3.8E-04	-4.3E-05	1.4E-06	0.0E+00	0.0E+00	0.0E+00
a_{-2}	-7.7E-05	1.1E-04	-4.3E-05	4.9E-06	-1.7E-07	0.0E+00	0.0E+00	0.0E+00
a_{-3}	2.4E-06	-3.6E-06	1.4E-06	-1.7E-07	5.7E-09	0.0E+00	0.0E+00	0.0E+00
$E_{\gamma m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08	0.0E+00	0.0E+00
$E_{\gamma a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08	0.0E+00
Δd_a	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	8.3E-02
Δd_m	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta\varepsilon_{r a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta\varepsilon_{r m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
c_i	-7.3E-01	0.0E+00	3.7E-01	5.3E-01	5.8E-01	-1.0E+00	8.4E-01	7.2E-02

0	0	0	0	0	0	0
0	0	0	0	0	0	0
1	0	0	0	0	0	0
0	1	0	0	0	0	0
0	0	1	0	0	0	0
0	0	0	1	0	0	0
0	0	0	0	1	0	0
0	0	0	0	0	1	0
0	0	0	0	0	0	1

Δd_m	$\delta \varepsilon_{ra}$	$\delta \varepsilon_{rm}$
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
8.3E-02	0.0E+00	0.0E+00
0.0E+00	3.5E-05	3.3E-05
0.0E+00	3.3E-05	3.1E-05
-6.8E-02	0.0E+00	0.0E+00

Covariance matrix of COI_m/COI_a

a _{γ22 a}	c _{γ22 a}	c _i		a ₁	a ₀
0	0	-9.9E-02	a ₁	1.9E-03	-2.4E-03
0	0	3.8E-02	a ₀	-2.4E-03	3.2E-03
0	0	2.2E-01	a ₋₁	7.5E-04	-1.1E-03
0	0	4.8E-01	a ₋₂	-7.7E-05	1.1E-04
0	0	8.9E-01	a ₋₃	2.4E-06	-3.6E-06
0	0	1.2E-04	E _{γ2 m}	0.0E+00	0.0E+00
0	0	-1.7E-01	a _{γ2 m}	0.0E+00	0.0E+00
0	0	-1.7E-01	c _{γ2 m}	0.0E+00	0.0E+00
0	0	8.8E-01	P/T _{γ2 m}	0.0E+00	0.0E+00
0	0	-3.5E-06	E _{γ12 a}	0.0E+00	0.0E+00
0	0	1.2E-02	P _{γ12 a}	0.0E+00	0.0E+00
0	0	-2.8E-04	E _{γ24 a}	0.0E+00	0.0E+00
0	0	2.1E-01	a _{γ24 a}	0.0E+00	0.0E+00
0	0	2.1E-01	c _{γ24 a}	0.0E+00	0.0E+00
0	0	-7.1E-01	P/T _{γ24 a}	0.0E+00	0.0E+00
0	0	2.4E-06	E _{γ13 a}	0.0E+00	0.0E+00
0	0	-1.7E-01	P _{γ13 a}	0.0E+00	0.0E+00
0	0	3.7E-06	E _{γ23 a}	0.0E+00	0.0E+00
0	0	-3.1E-03	a _{γ23 a}	0.0E+00	0.0E+00
0	0	-3.1E-03	c _{γ23 a}	0.0E+00	0.0E+00
0	0	2.3E-06	E _{γ14 a}	0.0E+00	0.0E+00
0	0	-1.5E-01	P _{γ14 a}	0.0E+00	0.0E+00
0	0	3.0E-06	E _{γ22 a}	0.0E+00	0.0E+00
1	0	-3.1E-03	a _{γ22 a}	0.0E+00	0.0E+00
0	1	-2.8E-03	c _{γ22 a}	0.0E+00	0.0E+00
			c _i	-9.9E-02	3.8E-02

-3.4E-14	E_{r_a}	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
2.7E-12	Q_{0_m}	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
1.1E-15	E_{r_m}	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
2.9E-11	$\varepsilon_{p_m}^{geo} / \varepsilon_{p_a}^{geo}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
3.9E-11	COI_m / COI_a	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
4.7E-09	m_m	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-1.7E-10	m_a	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
8.7E-09	w_m	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-4.0E-13	v	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
	c_i	2.6E-18	-2.0E-12	4.6E-18	-2.4E-19	5.3E-18	3.9E-18

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-3.3E-17	-1.7E-19	-2.1E-15	5.6E-14	1.6E-14	-2.9E-16	-2.8E-09	3.0E-11	-1.3E-11	-2.7E-11

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	3.3E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	3.6E-03	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	4.8E+01	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.5E-03
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
3.5E-11	5.2E-12	1.4E-12	6.8E-11	-9.4E-13	-3.4E-14	2.7E-12	1.1E-15	2.9E-11

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
6.1E-05	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	2.5E-09	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	2.5E-09	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	2.1E-09	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.4E+00
3.9E-11	4.7E-09	-1.7E-10	8.7E-09	-4.0E-13

Irradiation and γ -spectrometry

end irradiation 9/12/2017 2.46 PM
 irradiation time / s 21600

library CSF.Lib
 calib OR50_source2016_geom_cont_12052017.Clb
 sm type CSF.Lib (ROI32 Analysis)

Nuclide	Channel	Energy	Background
46Sc		3555.94	889.3
Co60		4691.96	1173.2

	target	product
analite, a	^{45}Sc	^{46}Sc
monitor, m	^{59}Co	^{60}Co

Uncertainty budget of ρ_a

Input Quantity	Quantity	Unit	Value
X_i	X_i	$[X_i]$	x_i
t_i		s	21600
μ		1	0.0445
$t_{1/2 a}$		s	7242912
	λ_a	s^{-1}	9.6E-08
$t_{1/2 m}$		s	1.7E+08
	λ_m	s^{-1}	4.2E-09
$t_{d a}$		s	2404405
$t_{c a}$		s	1292628
$t_{i a}$		s	1264268
$t_{d m}$		s	3722775
$t_{c m}$		s	797
$t_{i m}$		s	740
	δ_a	1	1.022
	δ_m	1	1.077
	ξ_a	1	1.00098
	ξ_m	1	1.00319
$n_{p a}$		1	130702
$n_{p m}$		1	137487
$k_{0 Au(a)}$		1	1.2200
$k_{0 Au(m)}$		1	1.3200
$G_{th a}$		1	1

$G_{e a}$		1	1
$G_{th m}$		1	1
$G_{e m}$		1	1
f		1	15.60
α		1	-0.0360
$Q_{0 a}$		1	0.430
$E_{r a}$		eV	5130
	$Q_{0 a}(\alpha)$	1	0.45
$Q_{0 m}$		1	1.993
$E_{r m}$		eV	136.0
	$Q_{0 m}(\alpha)$	1	2.319
$\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$		1	0.7968
COI_m / COI_a		1	1.009
m_m		g	0.00847
m_a		g	0.24000
w_m		$g g^{-1}$	0.004597
ν		$mg L^{-1}$	99.2
Y		[Y]	y
ρ_a		$g mL^{-1}$	5.06E-11

Uncertainty budget of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

Input Quantity	Quantity	Unit	Value
X_i	X_i	[X_i]	x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
$a_{.1}$		Mev	0.403
$a_{.2}$		Mev2	-0.0320
$a_{.3}$		Mev3	0.000573
$E_{\gamma m}$		MeV	1.17320
$E_{\gamma a}$		MeV	0.88930
Δd_a		mm	0
Δd_m		mm	0
	e_4	keV-4	-7.1E-11
	e_3	keV-3	5.2E-08
	e_2	keV-2	-1.4E-05
	e_1	keV-1	1.8E-03
	e_0		1 -4.5E-02
	d_1	keV-1	5.6E-06

	d_0		1	4.2E-02
$\delta\epsilon_{ra}$		mm^{-1}		0.047
$\delta\epsilon_{rm}$		mm^{-1}		0.048
Y		[Y]	y	
	$\epsilon_{pm}^{\text{geo}} / \epsilon_{pa}^{\text{geo}}$		1	0.797

Uncertainty budget of $\text{COI}_m / \text{COI}_a$

Input Quantity	Quantity X_i	Unit [X_i]	Value x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
a_{-1}		Mev	0.403
a_{-2}		Mev2	-0.0320
a_{-3}		Mev3	0.000573
	b_1		1 -0.571
	b_0		1 1.079
	c_2		1 -1.625
	c_1		1 6.678
	c_0		1 -7.006
$E_{\gamma 2m}$		keV	1332.5
$a_{\gamma 2m}$			1 1.000
$c_{\gamma 2m}$			1 1.000
$P/T_{\gamma 2m}$			1 0.197
$E_{\gamma 1a}$		keV	1120.5
$P_{\gamma 1a}$			1 99.99%
$P/T_{\gamma 1a}$			1 0.217
$a_{\gamma 2a}$			1 1.000
$c_{\gamma 2a}$			1 1.000
$P_{\gamma 2a}$			1 99.98%
	Y	[Y]	y
	$\text{COI}_m / \text{COI}_a$		1 1.009

Net area	Cnts/s	Uncert %	FWHM	source file	start counting
130702	0.103	0.61	1.615	OR50_20171025_CSF_si	10/10/2017
137487	185.919	0.32	1.798	OR50_20170925_Co_sa	10/25/2017

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance y $u^2_y(x_i)$	Index	Input for sensit coeff $x_i+u(x_i)$ $y(x_i+u(x_i))$	
17	0.1%	2.3E-18	1.6E-33	0.0%	2.2E+04	5.1E-11
0.0005	1.1%	-2.5E-12	1.6E-30	0.0%	4.5E-02	5.1E-11
1728	0.0%	5.0E-18	7.3E-29	0.0%	7.2E+06	5.1E-11
2.3E-11	0.0%					
2.6E+04	0.0%	-3.0E-19	6.0E-29	0.0%	1.7E+08	5.1E-11
6.5E-13	0.0%					
35	0.0%	4.8E-18	2.8E-32	0.0%	2.4E+06	5.1E-11
0.3	0.0%	4.1E-18	1.4E-36	0.0%	1.3E+06	5.1E-11
0.3	0.0%	-4.2E-17	1.5E-34	0.0%	1.3E+06	5.1E-11
35	0.0%	-2.1E-19	5.3E-35	0.0%	3.7E+06	5.1E-11
0.3	0.0%	-2.6E-15	5.7E-31	0.0%	8.0E+02	5.1E-11
0.3	0.0%	7.1E-14	4.2E-28	0.0%	7.4E+02	5.1E-11
0.000	0.0%					
0.001	0.1%					
0.00001	0.0%					
0.00004	0.0%					
797	0.6%	3.9E-16	9.5E-26	4.1%	1.3E+05	5.1E-11
440	0.3%	-3.7E-16	2.6E-26	1.1%	1.4E+05	5.0E-11
0.0049	0.4%	-4.2E-11	4.1E-26	1.7%	1.2E+00	5.0E-11
0.0053	0.4%	3.8E-11	4.1E-26	1.7%	1.3E+00	5.1E-11
0	0.0%	-4.9E-11	0.0E+00	0.0%	1.0E+00	5.1E-11

	0.0000	0.0%					
	0.005	11.5%	0.0E+00	0.0E+00	0.0%	5.2E-02	8.0E-01
	0.006	11.5%	0.0E+00	0.0E+00	0.0%	5.4E-02	8.0E-01
$u_c(y)$	$u_{c,r}(y)$				Σ		
	0.017	2.1%			100.0%		

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance y $u^2_y(x_i)$	Index	Input for sensit coeff $x_i+u(x_i)$ $y(x_i+u(x_i))$	
0.043	9.2%	-0.0240	1.2E-06	6.2%	-4.3E-01	1.0E+00
0.057	1.8%	0.0104	6.4E-07	3.3%	-3.2E+00	1.0E+00
0.020	4.8%	0.0331	-6.1E-07	-3.2%	4.2E-01	1.0E+00
0.0022	6.9%	0.0474	8.8E-08	0.5%	-3.0E-02	1.0E+00
0.000075	13.1%	0.0557	-3.2E-09	0.0%	6.5E-04	1.0E+00
0	0.0%					
0	0.0%					
0	0.0%					
0	0.0%					
0	0.0%					
0.1	0.0%	0.0001	1.7E-10	0.0%	1.3E+03	1.0E+00
0.012	1.2%	-0.1678	3.8E-06	19.7%	1.0E+00	1.0E+00
0.012	1.2%	-0.1678	3.8E-06	19.7%	1.0E+00	1.0E+00
0.023	11.5%	0.8639	-2.6E-05	-136.3%	2.2E-01	1.0E+00
0.12	0.0%	-0.0001	2.4E-10	0.0%	1.1E+03	1.0E+00
0.01%	0.0%	0.1782	4.2E-10	0.0%	1.0E+00	1.0E+00
0.025	11.5%	-0.8352	2.8E-05	145.4%	2.4E-01	9.9E-01
0.012	1.2%	0.1782	4.2E-06	22.2%	1.0E+00	1.0E+00
0.012	1.2%	0.1782	4.2E-06	22.2%	1.0E+00	1.0E+00
0.12%	0.1%	-0.1782	4.2E-08	0.2%	1.0E+00	1.0E+00

$u_c(y)$	$u_r(y)$			Σ	
	0.004	0.4%		100.0%	

	t_c / s	t_i / s	$t_{dead\ r} / \%$	t_d / s	$t_c / t_{1/2}$	$t_d / t_{1/2}$
10:39 AM	1292628	1264268	2.2%	2404405	0.18	0.3
4:52 PM	797	740	7.2%	3722775	0.00	0.0

Correlation matrix of ρ_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		t_i	μ	$t_{1/2\ a}$	$t_{1/2\ m}$
2.2E+04	5.1E-11	t_i	1	0	0	0
4.4E-02	5.1E-11	μ	0	1	0	0
7.2E+06	5.1E-11	$t_{1/2\ a}$	0	0	1	0
		$t_{1/2\ m}$	0	0	0	1
1.7E+08	5.1E-11	$t_{d\ a}$	0	0	0	0
		$t_{c\ a}$	0	0	0	0
2.4E+06	5.1E-11	$t_{i\ a}$	0	0	0	0
1.3E+06	5.1E-11	$t_{d\ m}$	0	0	0	0
1.3E+06	5.1E-11	$t_{c\ m}$	0	0	0	0
3.7E+06	5.1E-11	$t_{i\ m}$	0	0	0	0
8.0E+02	5.1E-11	$n_{p\ a}$	0	0	0	0
7.4E+02	5.1E-11	$n_{p\ m}$	0	0	0	0
		$k_{0\ Au}(a)$	0	0	0	0
		$k_{0\ Au}(m)$	0	0	0	0
		$G_{th\ a}$	0	0	0	0
		$G_{e\ a}$	0	0	0	0
1.3E+05	5.0E-11	$G_{th\ m}$	0	0	0	0
1.4E+05	5.1E-11	$G_{e\ m}$	0	0	0	0
1.2E+00	5.1E-11	f	0	0	0	0
1.3E+00	5.0E-11	α	0	0	0	0
1.0E+00	5.1E-11	$Q_{0\ a}$	0	0	0	0

1.0E+00	5.1E-11	E_{ra}	0	0	0	0
1.0E+00	5.1E-11	Q_{0m}	0	0	0	0
1.0E+00	5.1E-11	E_{rm}	0	0	0	0
1.5E+01	5.1E-11	$\varepsilon_{pm}^{geo} / \varepsilon_{pa}^i$	0	0	0	0
-4.2E-02	5.1E-11	COI_m / COI_a	0	0	0	0
3.4E-01	5.1E-11	m_m	0	0	0	0
4.3E+03	5.1E-11	m_a	0	0	0	0
		w_m	0	0	0	0
1.9E+00	5.0E-11	v	0	0	0	0
1.3E+02	5.1E-11					
7.8E-01	5.0E-11					
1.0E+00	5.0E-11					
8.4E-03	5.0E-11					
2.4E-01	5.1E-11					
4.6E-03	5.0E-11					
9.8E+01	5.1E-11					

Correlation matrix of $\varepsilon_{pm}^{geo} / \varepsilon_{pa}^{geo}$

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	7.9E-01	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	8.0E-01	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	8.0E-01	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	8.0E-01	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	8.0E-01	a_{-3}	0.748	-0.848	0.957	-0.993
1.2E+00	8.0E-01	$E_{\gamma m}$	0	0	0	0
8.9E-01	8.0E-01	$E_{\gamma a}$	0	0	0	0
-2.9E-01	7.9E-01	Δd_a	0	0	0	0
-2.9E-01	8.1E-01	Δd_m	0	0	0	0
		$\delta \varepsilon_{ra}$	0	0	0	0
		$\delta \varepsilon_{rm}$	0	0	0	0

4.1E-02 8.0E-01
 4.3E-02 8.0E-01

Correlation matrix of COI_m / COI_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	1.0E+00	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	1.0E+00	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	1.0E+00	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	1.0E+00	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	1.0E+00	a_{-3}	0.748	-0.848	0.957	-0.993
		$E_{\gamma 2 m}$	0	0	0	0
		$a_{\gamma 2 m}$	0	0	0	0
		$C_{\gamma 2 m}$	0	0	0	0
		$P/T_{\gamma 2 m}$	0	0	0	0
		$E_{\gamma 1 a}$	0	0	0	0
1.3E+03	1.0E+00	$P_{\gamma 1 a}$	0	0	0	0
9.9E-01	1.0E+00	$P/T_{\gamma 1 a}$	0	0	0	0
9.9E-01	1.0E+00	$a_{\gamma 2 a}$	0	0	0	0
1.7E-01	9.9E-01	$C_{\gamma 2 a}$	0	0	0	0
1.1E+03	1.0E+00	$P_{\gamma 2 a}$	0	0	0	0
1.0E+00	1.0E+00					
1.9E-01	1.0E+00					
9.9E-01	1.0E+00					
9.9E-01	1.0E+00					
1.0E+00	1.0E+00					

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$	Δd_a	Δd_m	$\delta \varepsilon_{ra}$	$\delta \varepsilon_{rm}$	c_i
0.748	0	0	0	0	0	0	2.3E-01
-0.848	0	0	0	0	0	0	0.0E+00
0.957	0	0	0	0	0	0	-2.2E-01
-0.993	0	0	0	0	0	0	-4.3E-01
1.000	0	0	0	0	0	0	-6.4E-01
0	1	0	0	0	0	0	-5.8E-01
0	0	1	0	0	0	0	7.1E-01
0	0	0	1	0	0	0	3.7E-02
0	0	0	0	1	0	0	-3.8E-02
0	0	0	0	0	1	1	0.0E+00
0	0	0	0	0	1	1	0.0E+00

0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Covariance matrix of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

	a_1	a_0	a_{-1}	a_{-2}	a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$
a_1	1.9E-03	-2.4E-03	7.5E-04	-7.7E-05	2.4E-06	0.0E+00	0.0E+00
a_0	-2.4E-03	3.2E-03	-1.1E-03	1.1E-04	-3.6E-06	0.0E+00	0.0E+00
a_{-1}	7.5E-04	-1.1E-03	3.8E-04	-4.3E-05	1.4E-06	0.0E+00	0.0E+00
a_{-2}	-7.7E-05	1.1E-04	-4.3E-05	4.9E-06	-1.7E-07	0.0E+00	0.0E+00
a_{-3}	2.4E-06	-3.6E-06	1.4E-06	-1.7E-07	5.7E-09	0.0E+00	0.0E+00
$E_{\gamma m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08	0.0E+00
$E_{\gamma a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08
Δd_a	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
Δd_m	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
c_i	2.3E-01	0.0E+00	-2.2E-01	-4.3E-01	-6.4E-01	-5.8E-01	7.1E-01

Covariance matrix of COI_m/COI_a

$C_{\gamma 2 a}$	$P_{\gamma 2 a}$	c_i		a_1	a_0	a_{-1}
0	0	-2.4E-02	a_1	1.9E-03	-2.4E-03	7.5E-04
0	0	1.0E-02	a_0	-2.4E-03	3.2E-03	-1.1E-03
0	0	3.3E-02	a_{-1}	7.5E-04	-1.1E-03	3.8E-04
0	0	4.7E-02	a_{-2}	-7.7E-05	1.1E-04	-4.3E-05
0	0	5.6E-02	a_{-3}	2.4E-06	-3.6E-06	1.4E-06
0	0	1.1E-04	$E_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
0	0	-1.7E-01	$a_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
0	0	-1.7E-01	$c_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
0	0	8.6E-01	$P/T_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
0	0	-1.3E-04	$E_{\gamma 1 a}$	0.0E+00	0.0E+00	0.0E+00
0	0	1.8E-01	$P_{\gamma 1 a}$	0.0E+00	0.0E+00	0.0E+00
0	0	-8.4E-01	$P/T_{\gamma 1 a}$	0.0E+00	0.0E+00	0.0E+00
0	0	1.8E-01	$a_{\gamma 2 a}$	0.0E+00	0.0E+00	0.0E+00
1	0	1.8E-01	$c_{\gamma 2 a}$	0.0E+00	0.0E+00	0.0E+00
0	1	-1.8E-01	$P_{\gamma 2 a}$	0.0E+00	0.0E+00	0.0E+00
			c_i	-2.4E-02	1.0E-02	3.3E-02

0	0	0	0	0	0	0
1	0	0	0	0	0	0
0	1	0	0	0	0	0
0	0	1	0	0	0	0
0	0	0	1	0	0	0
0	0	0	0	1	0	0
0	0	0	0	0	1	0
0	0	0	0	0	0	1
0	0	0	0	0	0	0

Δd_a	Δd_m	$\delta \varepsilon_{r_a}$	$\delta \varepsilon_{r_m}$
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
8.3E-02	0.0E+00	0.0E+00	0.0E+00
0.0E+00	8.3E-02	0.0E+00	0.0E+00
0.0E+00	0.0E+00	2.9E-05	3.0E-05
0.0E+00	0.0E+00	3.0E-05	3.1E-05
3.7E-02	-3.8E-02	0.0E+00	0.0E+00

a_{-2}	a_{-3}	$E_{\gamma 2 m}$	$a_{\gamma 2 m}$	$C_{\gamma 2 m}$	$P/T_{\gamma 2 m}$	$E_{\gamma 1 a}$
-7.7E-05	2.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
1.1E-04	-3.6E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-4.3E-05	1.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
4.9E-06	-1.7E-07	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-1.7E-07	5.7E-09	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	1.3E-02	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	5.2E-04	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-02
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	5.7E-04	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
4.7E-02	5.6E-02	1.1E-04	-1.7E-01	-1.7E-01	8.6E-01	-1.3E-04

Covariance matrix of ρ_a

ν	c_i	t_i	μ
0	2.3E-18	t_i	3.0E+02
0	-2.5E-12	μ	0.0E+00
0	5.0E-18	$t_{1/2 a}$	0.0E+00
0	-3.0E-19	$t_{1/2 m}$	0.0E+00
0	4.8E-18	$t_{d a}$	0.0E+00
0	4.1E-18	$t_{c a}$	0.0E+00
0	-4.2E-17	$t_{i a}$	0.0E+00
0	-2.1E-19	$t_{d m}$	0.0E+00
0	-2.6E-15	$t_{c m}$	0.0E+00
0	7.1E-14	$t_{i m}$	0.0E+00
0	3.9E-16	$n_{p a}$	0.0E+00
0	-3.7E-16	$n_{p m}$	0.0E+00
0	-4.2E-11	$k_{0 Au(a)}$	0.0E+00
0	3.8E-11	$k_{0 Au(m)}$	0.0E+00
0	-4.9E-11	$G_{th a}$	0.0E+00
0	-1.4E-12	$G_{e a}$	0.0E+00
0	4.4E-11	$G_{th m}$	0.0E+00
0	6.6E-12	$G_{e m}$	0.0E+00
0	-3.3E-13	f	0.0E+00
0	-2.6E-11	α	0.0E+00
0	-4.3E-12	$Q_{0 a}$	0.0E+00

0	-3.0E-20	E_{r_a}	0.0E+00	0.0E+00
0	3.4E-12	Q_{0_m}	0.0E+00	0.0E+00
0	1.4E-15	E_{r_m}	0.0E+00	0.0E+00
0	6.4E-11	$\varepsilon_{p_m}^{geo} / \varepsilon_{p_a}^{geo}$	0.0E+00	0.0E+00
0	5.0E-11	COI_m / COI_a	0.0E+00	0.0E+00
0	6.0E-09	m_m	0.0E+00	0.0E+00
0	-2.1E-10	m_a	0.0E+00	0.0E+00
0	1.1E-08	w_m	0.0E+00	0.0E+00
1	-5.1E-13	ν	0.0E+00	0.0E+00
		c_i	2.3E-18	-2.5E-12

$P_{\gamma 1 a}$	$P/T_{\gamma 1 a}$	$a_{\gamma 2 a}$	$C_{\gamma 2 a}$	$P_{\gamma 2 a}$	
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	5.7E-04	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
1.3E-08	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	6.3E-04	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-06
1.8E-01	-8.4E-01	1.8E-01	1.8E-01	1.8E-01	-1.8E-01

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
5.0E-18	-3.0E-19	4.8E-18	4.1E-18	-4.2E-17	-2.1E-19

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-2.6E-15	7.1E-14	3.9E-16	-3.7E-16	-4.2E-11	3.8E-11

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-4.9E-11	-1.4E-12	4.4E-11	6.6E-12	-3.3E-13

0.0E+00	0.0E+00	7.6E+05	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	3.6E-03	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	4.8E+01	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	2.9E-04
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-2.6E-11	-4.3E-12	-3.0E-20	3.4E-12	1.4E-15	6.4E-11

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
1.9E-05	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	2.5E-09	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	2.5E-09	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	2.1E-09	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.4E+00
5.0E-11	6.0E-09	-2.1E-10	1.1E-08	-5.1E-13

Irradiation and γ -spectrometry

end irradiation 9/12/2017 2.46 PM
 irradiation time / s 21600

library CSF.Lib
 calib OR50_source2016_geom_cont_12052017.Clb
 sm type CSF.Lib (ROI32 Analysis)

Nuclide	Channel	Energy	Background
86Rb		4307.77	1077
Co60		4691.96	1173.2

	target	product
analite, a	^{85}Rb	^{86}Rb
monitor, m	^{59}Co	^{60}Co

Uncertainty budget of ρ_a

Input Quantity	Quantity	Unit	Value
X_i	X_i	$[X_i]$	x_i
t_i		s	21600
μ		1	0.0445
$t_{1/2 a}$		s	1609632
	λ_a	s^{-1}	4.3E-07
$t_{1/2 m}$		s	1.7E+08
	λ_m	s^{-1}	4.2E-09
$t_{d a}$		s	2404405
$t_{c a}$		s	1292628
$t_{i a}$		s	1264268
$t_{d m}$		s	3722775
$t_{c m}$		s	797
$t_{i m}$		s	740
	δ_a	1	1.022
	δ_m	1	1.077
	ξ_a	1	1.00098
	ξ_m	1	1.00319
$n_{p a}$		1	4559
$n_{p m}$		1	137487
$k_{0 Au(a)}$		1	0.0007650
$k_{0 Au(m)}$		1	1.3200
$G_{th a}$		1	1

$G_{e a}$		1	1
$G_{th m}$		1	1
$G_{e m}$		1	1
f		1	15.60
α		1	-0.0360
$Q_{0 a}$		1	14.80
$E_{r a}$		eV	839
	$Q_{0 a}(\alpha)$	1	18.76
$Q_{0 m}$		1	1.993
$E_{r m}$		eV	136.0
	$Q_{0 m}(\alpha)$	1	2.319
$\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$		1	0.9306
COI_m / COI_a		1	0.857
m_m		g	0.00847
m_a		g	0.24000
w_m		$g g^{-1}$	0.004597
ν		$mg L^{-1}$	99.2
Y		[Y]	y
ρ_a		$g mL^{-1}$	8.00E-10

Uncertainty budget of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

Input Quantity	Quantity	Unit	Value
X_i	X_i	[X_i]	x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
$a_{.1}$		Mev	0.403
$a_{.2}$		Mev2	-0.0320
$a_{.3}$		Mev3	0.000573
$E_{\gamma m}$		MeV	1.17320
$E_{\gamma a}$		MeV	1.07700
Δd_a		mm	0
Δd_m		mm	0
	e_4	keV-4	-7.1E-11
	e_3	keV-3	5.2E-08
	e_2	keV-2	-1.4E-05
	e_1	keV-1	1.8E-03
	e_0		1 -4.5E-02
	d_1	keV-1	5.6E-06

	d_0		1	4.2E-02
$\delta\epsilon_{ra}$		mm^{-1}		0.048
$\delta\epsilon_{rm}$		mm^{-1}		0.048
Y		[Y]	y	
$\epsilon_{pm}^{\text{geo}} / \epsilon_{pa}^{\text{geo}}$		1		0.931

Uncertainty budget of $\text{COI}_m / \text{COI}_a$

Input Quantity	Quantity X_i	Unit [X_i]	Value x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
a_{-1}		Mev	0.403
a_2		Mev2	-0.0320
a_3		Mev3	0.000573
	b_1		1 -0.571
	b_0		1 1.079
	c_2		1 -1.625
	c_1		1 6.678
	c_0		1 -7.006
$E_{\gamma 2m}$		keV	1332.5
$a_{\gamma 2m}$			1 1.000
$c_{\gamma 2m}$			1 1.000
$P/T_{\gamma 2m}$			1 0.197
	Y	[Y]	y
	$\text{COI}_m / \text{COI}_a$		1 0.857

Net area	Cnts/s	Uncert %	FWHM	source file	start counting
4559	0.004	9.68	1.958	OR50_20171025_CSF_si	10/10/2017
137487	185.919	0.32	1.798	OR50_20170925_Co_sa	10/25/2017

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance y $u^2_y(x_i)$	Index	Input for sensit coeff $x_i+u(x_i)$ $y(x_i+u(x_i))$	
17	0.1%	1.7E-16	8.7E-30	0.0%	2.2E+04	8.0E-10
0.0005	1.1%	-4.0E-11	3.9E-28	0.0%	4.5E-02	8.0E-10
1728	0.1%	-1.5E-16	6.3E-26	0.0%	1.6E+06	8.0E-10
4.6E-10	0.1%					
2.6E+04	0.0%	-4.7E-18	1.5E-26	0.0%	1.7E+08	8.0E-10
6.5E-13	0.0%					
35	0.0%	3.4E-16	1.4E-28	0.0%	2.4E+06	8.0E-10
0.3	0.0%	1.8E-16	2.8E-33	0.0%	1.3E+06	8.0E-10
0.3	0.0%	-6.6E-16	3.6E-32	0.0%	1.3E+06	8.0E-10
35	0.0%	-3.3E-18	1.3E-32	0.0%	3.7E+06	8.0E-10
0.3	0.0%	-4.1E-14	1.4E-28	0.0%	8.0E+02	8.0E-10
0.3	0.0%	1.1E-12	1.1E-25	0.0%	7.4E+02	8.0E-10
0.000	0.0%					
0.001	0.1%					
0.00001	0.0%					
0.00004	0.0%					
441	9.7%	1.8E-13	6.0E-21	83.4%	5.0E+03	8.8E-10
440	0.3%	-5.8E-15	6.5E-24	0.1%	1.4E+05	8.0E-10
0.0000077	1.0%	-1.0E-06	6.4E-23	0.9%	7.7E-04	7.9E-10
0.0053	0.4%	6.1E-10	1.0E-23	0.1%	1.3E+00	8.0E-10
0	0.0%	-3.6E-10	0.0E+00	0.0%	1.0E+00	8.0E-10

	0.0000	0.0%					
	0.006	11.5%	0.0E+00	0.0E+00	0.0%	5.3E-02	9.3E-01
	0.006	11.5%	0.0E+00	0.0E+00	0.0%	5.4E-02	9.3E-01
$u_c(y)$	$u_{c,r}(y)$				Σ		
	0.018	2.0%			100.0%		

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance y $u^2_y(x_i)$	Index	Input for sensit coeff	
					$x_i+u(x_i)$	$y(x_i+u(x_i))$
0.043	9.2%	-0.1901	1.7E-05	5.9%	-4.3E-01	8.5E-01
0.057	1.8%	-0.1427	-1.4E-05	-4.9%	-3.2E+00	8.5E-01
0.020	4.8%	-0.1070	3.0E-06	1.0%	4.2E-01	8.6E-01
0.0022	6.9%	-0.0803	-2.2E-07	-0.1%	-3.0E-02	8.6E-01
0.000075	13.1%	-0.0603	5.0E-09	0.0%	6.5E-04	8.6E-01
0	0.0%					
0	0.0%					
0	0.0%					
0	0.0%					
0	0.0%					
0.1	0.0%	0.0001	1.2E-10	0.0%	1.3E+03	8.6E-01
0.012	1.2%	-0.1426	2.7E-06	0.9%	1.0E+00	8.6E-01
0.012	1.2%	-0.1426	2.7E-06	0.9%	1.0E+00	8.6E-01
0.023	11.5%	0.7343	2.8E-04	96.2%	2.2E-01	8.7E-01
$u_c(y)$	$u_r(y)$					
	0.017	2.0%				
					Σ	
					100.0%	

	t_c / s	t_i / s	$t_{dead\ r} / \%$	t_d / s	$t_c / t_{1/2}$	$t_d / t_{1/2}$
10:39 AM	1292628	1264268	2.2%	2404405	0.80	1.5
4:52 PM	797	740	7.2%	3722775	0.00	0.0

Covariance matrix of ρ_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		t_i	μ	$t_{1/2\ a}$	$t_{1/2\ m}$
2.2E+04	8.0E-10	t_i	1	0	0	0
4.4E-02	8.0E-10	μ	0	1	0	0
1.6E+06	8.0E-10	$t_{1/2\ a}$	0	0	1	0
		$t_{1/2\ m}$	0	0	0	1
1.7E+08	8.0E-10	$t_{d\ a}$	0	0	0	0
		$t_{c\ a}$	0	0	0	0
2.4E+06	8.0E-10	$t_{i\ a}$	0	0	0	0
1.3E+06	8.0E-10	$t_{d\ m}$	0	0	0	0
1.3E+06	8.0E-10	$t_{c\ m}$	0	0	0	0
3.7E+06	8.0E-10	$t_{i\ m}$	0	0	0	0
8.0E+02	8.0E-10	$n_{p\ a}$	0	0	0	0
7.4E+02	8.0E-10	$n_{p\ m}$	0	0	0	0
		$k_{0\ Au}(a)$	0	0	0	0
		$k_{0\ Au}(m)$	0	0	0	0
		$G_{th\ a}$	0	0	0	0
		$G_{e\ a}$	0	0	0	0
4.1E+03	7.2E-10	$G_{th\ m}$	0	0	0	0
1.4E+05	8.0E-10	$G_{e\ m}$	0	0	0	0
7.6E-04	8.1E-10	f	0	0	0	0
1.3E+00	8.0E-10	α	0	0	0	0
1.0E+00	8.0E-10	$Q_{0\ a}$	0	0	0	0

1.0E+00	8.0E-10	E_{ra}	0	0	0	0
1.0E+00	8.0E-10	Q_{0m}	0	0	0	0
1.0E+00	8.0E-10	E_{rm}	0	0	0	0
1.5E+01	7.9E-10	$\varepsilon_{pm}^{geo} / \varepsilon_{pa}^i$	0	0	0	0
-4.2E-02	7.8E-10	COI_m / COI_a	0	0	0	0
1.4E+01	8.1E-10	m_m	0	0	0	0
7.9E+02	8.0E-10	m_a	0	0	0	0
		w_m	0	0	0	0
1.9E+00	8.0E-10	v	0	0	0	0
1.3E+02	8.0E-10					
9.1E-01	7.8E-10					
8.4E-01	7.8E-10					
8.4E-03	7.9E-10					
2.4E-01	8.0E-10					
4.6E-03	7.9E-10					
9.8E+01	8.1E-10					

Correlation matrix of $\varepsilon_{pm}^{geo} / \varepsilon_{pa}^{geo}$

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	9.3E-01	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	9.3E-01	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	9.3E-01	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	9.3E-01	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	9.3E-01	a_{-3}	0.748	-0.848	0.957	-0.993
1.2E+00	9.3E-01	$E_{\gamma m}$	0	0	0	0
1.1E+00	9.3E-01	$E_{\gamma a}$	0	0	0	0
-2.9E-01	9.2E-01	Δd_a	0	0	0	0
-2.9E-01	9.4E-01	Δd_m	0	0	0	0
		$\delta \varepsilon_{ra}$	0	0	0	0
		$\delta \varepsilon_{rm}$	0	0	0	0

4.2E-02 9.3E-01
 4.3E-02 9.3E-01

Correlation matrix of COI_m / COI_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	8.7E-01	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	8.7E-01	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	8.6E-01	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	8.6E-01	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	8.6E-01	a_{-3}	0.748	-0.848	0.957	-0.993
		$E_{\gamma 2 m}$	0	0	0	0
		$a_{\gamma 2 m}$	0	0	0	0
		$C_{\gamma 2 m}$	0	0	0	0
		$P/T_{\gamma 2 m}$	0	0	0	0
1.3E+03	8.6E-01					
9.9E-01	8.6E-01					
9.9E-01	8.6E-01					
1.7E-01	8.4E-01					

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$	Δd_a	Δd_m	$\delta \varepsilon_{ra}$	$\delta \varepsilon_{rm}$	c_i
0.748	0	0	0	0	0	0	9.0E-02
-0.848	0	0	0	0	0	0	0.0E+00
0.957	0	0	0	0	0	0	-7.1E-02
-0.993	0	0	0	0	0	0	-1.3E-01
1.000	0	0	0	0	0	0	-1.7E-01
0	1	0	0	0	0	0	-6.8E-01
0	0	1	0	0	0	0	7.2E-01
0	0	0	1	0	0	0	4.4E-02
0	0	0	0	1	0	0	-4.5E-02
0	0	0	0	0	1	1	0.0E+00
0	0	0	0	0	0	1	0.0E+00

Covariance

a_{-3}	$E_{\gamma 2 m}$	$a_{\gamma 2 m}$	$c_{\gamma 2 m}$	$P/T_{\gamma 2 m}$	c_i	
0.748	0	0	0	0	-1.9E-01	a_1
-0.848	0	0	0	0	-1.4E-01	a_0
0.957	0	0	0	0	-1.1E-01	a_{-1}
-0.993	0	0	0	0	-8.0E-02	a_{-2}
1.000	0	0	0	0	-6.0E-02	a_{-3}
0	1	0	0	0	9.6E-05	$E_{\gamma 2 m}$
0	0	1	0	0	-1.4E-01	$a_{\gamma 2 m}$
0	0	0	1	0	-1.4E-01	$c_{\gamma 2 m}$
0	0	0	0	1	7.3E-01	$P/T_{\gamma 2 m}$

c_i

0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Covariance matrix of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

	a_1	a_0	a_{-1}	a_{-2}	a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$
a_1	1.9E-03	-2.4E-03	7.5E-04	-7.7E-05	2.4E-06	0.0E+00	0.0E+00
a_0	-2.4E-03	3.2E-03	-1.1E-03	1.1E-04	-3.6E-06	0.0E+00	0.0E+00
a_{-1}	7.5E-04	-1.1E-03	3.8E-04	-4.3E-05	1.4E-06	0.0E+00	0.0E+00
a_{-2}	-7.7E-05	1.1E-04	-4.3E-05	4.9E-06	-1.7E-07	0.0E+00	0.0E+00
a_{-3}	2.4E-06	-3.6E-06	1.4E-06	-1.7E-07	5.7E-09	0.0E+00	0.0E+00
$E_{\gamma m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08	0.0E+00
$E_{\gamma a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08
Δd_a	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
Δd_m	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
c_i	9.0E-02	0.0E+00	-7.1E-02	-1.3E-01	-1.7E-01	-6.8E-01	7.2E-01

matrix of COI_m/COI_a

a_1	a_0	a_{-1}	a_{-2}	a_{-3}	$E_{\gamma 2 m}$	$a_{\gamma 2 m}$	$c_{\gamma 2 m}$	$P/T_{\gamma 2 m}$
1.9E-03	-2.4E-03	7.5E-04	-7.7E-05	2.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-2.4E-03	3.2E-03	-1.1E-03	1.1E-04	-3.6E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00
7.5E-04	-1.1E-03	3.8E-04	-4.3E-05	1.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-7.7E-05	1.1E-04	-4.3E-05	4.9E-06	-1.7E-07	0.0E+00	0.0E+00	0.0E+00	0.0E+00
2.4E-06	-3.6E-06	1.4E-06	-1.7E-07	5.7E-09	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-02	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	5.2E-04
-1.9E-01	-1.4E-01	-1.1E-01	-8.0E-02	-6.0E-02	9.6E-05	-1.4E-01	-1.4E-01	7.3E-01

0	0	0	0	0	0	0
1	0	0	0	0	0	0
0	1	0	0	0	0	0
0	0	1	0	0	0	0
0	0	0	1	0	0	0
0	0	0	0	1	0	0
0	0	0	0	0	1	0
0	0	0	0	0	0	1
0	0	0	0	0	0	0

Δd_a	Δd_m	$\delta \varepsilon_{r_a}$	$\delta \varepsilon_{r_m}$
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
8.3E-02	0.0E+00	0.0E+00	0.0E+00
0.0E+00	8.3E-02	0.0E+00	0.0E+00
0.0E+00	0.0E+00	3.0E-05	3.1E-05
0.0E+00	0.0E+00	3.1E-05	3.1E-05
4.4E-02	-4.5E-02	0.0E+00	0.0E+00

Covariance matrix of ρ_a

ρ	c_i	t_i	μ
0	1.7E-16	t_i	3.0E+02
0	-4.0E-11	μ	0.0E+00
0	-1.5E-16	$t_{1/2 a}$	0.0E+00
0	-4.7E-18	$t_{1/2 m}$	0.0E+00
0	3.4E-16	$t_{d a}$	0.0E+00
0	1.8E-16	$t_{c a}$	0.0E+00
0	-6.6E-16	$t_{i a}$	0.0E+00
0	-3.3E-18	$t_{d m}$	0.0E+00
0	-4.1E-14	$t_{c m}$	0.0E+00
0	1.1E-12	$t_{i m}$	0.0E+00
0	1.8E-13	$n_{p a}$	0.0E+00
0	-5.8E-15	$n_{p m}$	0.0E+00
0	-1.0E-06	$k_{0 Au(a)}$	0.0E+00
0	6.1E-10	$k_{0 Au(m)}$	0.0E+00
0	-3.6E-10	$G_{th a}$	0.0E+00
0	-4.4E-10	$G_{e a}$	0.0E+00
0	7.0E-10	$G_{th m}$	0.0E+00
0	1.0E-10	$G_{e m}$	0.0E+00
0	2.1E-11	f	0.0E+00
0	2.4E-09	α	0.0E+00
0	-3.0E-11	$Q_{0 a}$	0.0E+00

0	-1.8E-14	E_{r_a}	0.0E+00	0.0E+00
0	5.3E-11	Q_{0_m}	0.0E+00	0.0E+00
0	2.2E-14	E_{r_m}	0.0E+00	0.0E+00
0	8.6E-10	$\varepsilon_{p_m}^{geo} / \varepsilon_{p_a}^{geo}$	0.0E+00	0.0E+00
0	9.3E-10	COI_m / COI_a	0.0E+00	0.0E+00
0	9.4E-08	m_m	0.0E+00	0.0E+00
0	-3.3E-09	m_a	0.0E+00	0.0E+00
0	1.7E-07	w_m	0.0E+00	0.0E+00
1	-8.1E-12	ν	0.0E+00	0.0E+00
		c_i	1.7E-16	-4.0E-11

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-1.5E-16	-4.7E-18	3.4E-16	1.8E-16	-6.6E-16	-3.3E-18

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-4.1E-14	1.1E-12	1.8E-13	-5.8E-15	-1.0E-06	6.1E-10

$G_{th a}$	$G_{e a}$	$G_{th m}$	$G_{e m}$	f	
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.1E-01
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-3.6E-10	-4.4E-10	7.0E-10	1.0E-10	2.1E-11

α	Q_{0a}	E_{ra}	Q_{0m}	E_{rm}	$\varepsilon_{pm}^{geo} / \varepsilon_{pa}^{geo}$
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
4.1E-05	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	1.4E-01	0.0E+00	0.0E+00	0.0E+00	0.0E+00

0.0E+00	0.0E+00	2.5E+03	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	3.6E-03	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	4.8E+01	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	3.4E-04
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
2.4E-09	-3.0E-11	-1.8E-14	5.3E-11	2.2E-14	8.6E-10

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
2.9E-04	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	2.5E-09	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	2.5E-09	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	2.1E-09	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.4E+00
9.3E-10	9.4E-08	-3.3E-09	1.7E-07	-8.1E-12

Irradiation and γ -spectrometry

end irradiation 9/12/2017 2.46 PM
 irradiation time / s 21600

library CSF.Lib
 calib OR50_source2016_geom_cont_12052017.Clb
 sm type CSF.Lib (ROI32 Analysis)

Nuclide	Channel	Energy	Background
59Fe		4396.05	1099.3
Co60		4691.96	1173.2

	target	product
analite, a	^{58}Fe	^{59}Fe
monitor, m	^{59}Co	^{60}Co

Uncertainty budget of ρ_a

Input Quantity	Quantity	Unit	Value
X_i	X_i	$[X_i]$	x_i
t_i		s	21600
μ		1	0.0445
$t_{1/2 a}$		s	3844800
	λ_a	s^{-1}	1.8E-07
$t_{1/2 m}$		s	1.7E+08
	λ_m	s^{-1}	4.2E-09
$t_{d a}$		s	2404405
$t_{c a}$		s	1292628
$t_{i a}$		s	1264268
$t_{d m}$		s	3722775
$t_{c m}$		s	797
$t_{i m}$		s	740
	δ_a	1	1.022
	δ_m	1	1.077
	ξ_a	1	1.00098
	ξ_m	1	1.00319
$n_{p a}$		1	9456
$n_{p m}$		1	137487
$k_{0 Au(a)}$		1	0.00007770
$k_{0 Au(m)}$		1	1.3200
$G_{th a}$		1	1

$G_{e a}$		1	1
$G_{th m}$		1	1
$G_{e m}$		1	1
f		1	15.60
α		1	-0.0360
$Q_{0 a}$		1	0.975
$E_{r a}$		eV	637
	$Q_{0 a}(\alpha)$	1	1.14
$Q_{0 m}$		1	1.993
$E_{r m}$		eV	136.0
	$Q_{0 m}(\alpha)$	1	2.319
$\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$		1	0.9466
COI_m / COI_a		1	0.868
m_m		g	0.00847
m_a		g	0.24000
w_m		$g g^{-1}$	0.004597
ν		$mg L^{-1}$	99.2
Y		[Y]	y
ρ_a		$g mL^{-1}$	3.87E-08

Uncertainty budget of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

Input Quantity	Quantity	Unit	Value
X_i	X_i	[X_i]	x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
$a_{.1}$		Mev	0.403
$a_{.2}$		Mev2	-0.0320
$a_{.3}$		Mev3	0.000573
$E_{\gamma m}$		MeV	1.17320
$E_{\gamma a}$		MeV	1.09930
Δd_a		mm	0
Δd_m		mm	0
	e_4	keV-4	-7.1E-11
	e_3	keV-3	5.2E-08
	e_2	keV-2	-1.4E-05
	e_1	keV-1	1.8E-03
	e_0		1 -4.5E-02
	d_1	keV-1	5.6E-06

	d_0		1	4.2E-02
$\delta\epsilon_{ra}$		mm^{-1}		0.048
$\delta\epsilon_{rm}$		mm^{-1}		0.048
Y		[Y]	y	
	$\epsilon_{pm}^{\text{geo}} / \epsilon_{pa}^{\text{geo}}$		1	0.947

Uncertainty budget of $\text{COI}_m / \text{COI}_a$

Input Quantity	Quantity X_i	Unit [X_i]	Value x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
a_{-1}		Mev	0.403
a_{-2}		Mev2	-0.0320
a_{-3}		Mev3	0.000573
	b_1		1 -0.571
	b_0		1 1.079
	c_2		1 -1.625
	c_1		1 6.678
	c_0		1 -7.006
$E_{\gamma 2m}$		keV	1332.5
$a_{\gamma 2m}$			1 1.000
$c_{\gamma 2m}$			1 1.000
$P/T_{\gamma 2m}$			1 0.197
$E_{\gamma 4a}$		keV	192.3
$P_{\gamma 4a}$			1 2.95%
$P/T_{\gamma 4a}$			1 0.595
$a_{\gamma 5a}$			1 1.000
$c_{\gamma 5a}$			1 1.000
$P_{\gamma 5a}$			1 56.1%
	Y	[Y]	y
	$\text{COI}_m / \text{COI}_a$		1 0.868

Net area	Cnts/s	Uncert %	FWHM	source file	start counting
9456	0.007	6.2	1.895	OR50_20171025_CSF_si	10/10/2017
137487	185.919	0.32	1.798	OR50_20170925_Co_sa	10/25/2017

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance y $u^2_y(x_i)$	Index	Input for sensit coeff $x_i+u(x_i)$ $y(x_i+u(x_i))$	
17	0.1%	3.4E-15	3.5E-27	0.0%	2.2E+04	3.9E-08
0.0005	1.1%	-1.9E-09	9.2E-25	0.0%	4.5E-02	3.9E-08
518	0.0%	4.6E-15	5.6E-24	0.0%	3.8E+06	3.9E-08
2.4E-11	0.0%					
2.6E+04	0.0%	-2.3E-16	3.5E-23	0.0%	1.7E+08	3.9E-08
6.5E-13	0.0%					
35	0.0%	7.0E-15	5.8E-26	0.0%	2.4E+06	3.9E-08
0.3	0.0%	4.7E-15	1.8E-30	0.0%	1.3E+06	3.9E-08
0.3	0.0%	-3.2E-14	8.5E-29	0.0%	1.3E+06	3.9E-08
35	0.0%	-1.6E-16	3.1E-29	0.0%	3.7E+06	3.9E-08
0.3	0.0%	-2.0E-12	3.4E-25	0.0%	8.0E+02	3.9E-08
0.3	0.0%	5.4E-11	2.5E-22	0.0%	7.4E+02	3.9E-08
0.000	0.0%					
0.001	0.1%					
0.00001	0.0%					
0.00004	0.0%					
586	6.2%	4.1E-12	5.8E-18	78.0%	1.0E+04	4.1E-08
440	0.3%	-2.8E-13	1.5E-20	0.2%	1.4E+05	3.9E-08
0.00000039	0.5%	-5.0E-04	3.7E-20	0.5%	7.8E-05	3.9E-08
0.0053	0.4%	2.9E-08	2.4E-20	0.3%	1.3E+00	3.9E-08
0	0.0%	-3.6E-08	0.0E+00	0.0%	1.0E+00	3.9E-08

	0.0000	0.0%					
	0.006	11.5%	0.0E+00	0.0E+00	0.0%	5.3E-02	9.5E-01
	0.006	11.5%	0.0E+00	0.0E+00	0.0%	5.4E-02	9.5E-01
$u_c(y)$	$u_{c,r}(y)$				Σ		
	0.019	2.0%			100.0%		

Std unc	Rel std unc	Sensit coeff	Variance y	Index	Input for sensit coeff	
$u(x_i)$	$u_r(x_i)$	c_i	$u^2_{y}(x_i)$		$x_i+u(x_i)$	$y(x_i+u(x_i))$
0.043	9.2%	-0.1904	1.7E-05	6.6%	-4.3E-01	8.6E-01
0.057	1.8%	-0.1339	-1.3E-05	-5.2%	-3.2E+00	8.6E-01
0.020	4.8%	-0.0539	1.5E-06	0.6%	4.2E-01	8.7E-01
0.0022	6.9%	0.2016	5.3E-07	0.2%	-3.0E-02	8.7E-01
0.000075	13.1%	1.4091	-1.1E-07	0.0%	6.5E-04	8.7E-01
0	0.0%					
0	0.0%					
0	0.0%					
0	0.0%					
0	0.0%					
0.1	0.0%	0.0001	1.3E-10	0.0%	1.3E+03	8.7E-01
0.012	1.2%	-0.1443	2.8E-06	1.1%	1.0E+00	8.7E-01
0.012	1.2%	-0.1443	2.8E-06	1.1%	1.0E+00	8.7E-01
0.023	11.5%	0.7431	2.6E-04	103.1%	2.2E-01	8.8E-01
0.12	0.1%	0.0000	1.9E-11	0.0%	1.9E+02	8.7E-01
0.01%	0.4%	0.3544	1.7E-09	0.0%	3.0E-02	8.7E-01
0.069	11.5%	-0.0178	-1.9E-05	-7.5%	6.6E-01	8.7E-01
0.012	1.2%	0.0105	1.5E-08	0.0%	1.0E+00	8.7E-01
0.012	1.2%	0.0105	1.5E-08	0.0%	1.0E+00	8.7E-01
0.12%	0.2%	-0.0186	4.6E-10	0.0%	5.6E-01	8.7E-01

$u_c(y)$	$u_r(y)$			Σ		
	0.016	1.8%		100.0%		

	t_c / s	t_i / s	$t_{dead r} / \%$	t_d / s	$t_c / t_{1/2}$	$t_d / t_{1/2}$
10:39 AM	1292628	1264268	2.2%	2404405	0.34	0.6
4:52 PM	797	740	7.2%	3722775	0.00	0.0

Correlation matrix of ρ_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		t_i	μ	$t_{1/2 a}$	$t_{1/2 m}$
2.2E+04	3.9E-08	t_i	1	0	0	0
4.4E-02	3.9E-08	μ	0	1	0	0
3.8E+06	3.9E-08	$t_{1/2 a}$	0	0	1	0
		$t_{1/2 m}$	0	0	0	1
1.7E+08	3.9E-08	$t_{d a}$	0	0	0	0
		$t_{c a}$	0	0	0	0
2.4E+06	3.9E-08	$t_{i a}$	0	0	0	0
1.3E+06	3.9E-08	$t_{d m}$	0	0	0	0
1.3E+06	3.9E-08	$t_{c m}$	0	0	0	0
3.7E+06	3.9E-08	$t_{i m}$	0	0	0	0
8.0E+02	3.9E-08	$n_{p a}$	0	0	0	0
7.4E+02	3.9E-08	$n_{p m}$	0	0	0	0
		$k_{0 Au(a)}$	0	0	0	0
		$k_{0 Au(m)}$	0	0	0	0
		$G_{th a}$	0	0	0	0
		$G_{e a}$	0	0	0	0
8.9E+03	3.6E-08	$G_{th m}$	0	0	0	0
1.4E+05	3.9E-08	$G_{e m}$	0	0	0	0
7.7E-05	3.9E-08	f	0	0	0	0
1.3E+00	3.9E-08	α	0	0	0	0
1.0E+00	3.9E-08	$Q_{0 a}$	0	0	0	0

1.0E+00	3.9E-08	E_{ra}	0	0	0	0
1.0E+00	3.9E-08	Q_{0m}	0	0	0	0
1.0E+00	3.9E-08	E_{rm}	0	0	0	0
1.5E+01	3.9E-08	$\varepsilon_{pm}^{geo} / \varepsilon_{pa}^i$	0	0	0	0
-4.2E-02	3.9E-08	COI_m / COI_a	0	0	0	0
9.7E-01	3.9E-08	m_m	0	0	0	0
4.8E+02	3.9E-08	m_a	0	0	0	0
		w_m	0	0	0	0
1.9E+00	3.9E-08	v	0	0	0	0
1.3E+02	3.9E-08					
9.3E-01	3.8E-08					
8.5E-01	3.8E-08					
8.4E-03	3.8E-08					
2.4E-01	3.9E-08					
4.6E-03	3.8E-08					
9.8E+01	3.9E-08					

Correlation matrix of $\varepsilon_{pm}^{geo} / \varepsilon_{pa}^{geo}$

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	9.4E-01	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	9.5E-01	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	9.5E-01	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	9.5E-01	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	9.5E-01	a_{-3}	0.748	-0.848	0.957	-0.993
1.2E+00	9.5E-01	$E_{\gamma m}$	0	0	0	0
1.1E+00	9.5E-01	$E_{\gamma a}$	0	0	0	0
-2.9E-01	9.3E-01	Δd_a	0	0	0	0
-2.9E-01	9.6E-01	Δd_m	0	0	0	0
		$\delta \varepsilon_{ra}$	0	0	0	0
		$\delta \varepsilon_{rm}$	0	0	0	0

4.2E-02 9.5E-01
 4.3E-02 9.5E-01

Correlation matrix of COI_m / COI_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	8.8E-01	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	8.8E-01	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	8.7E-01	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	8.7E-01	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	8.7E-01	a_{-3}	0.748	-0.848	0.957	-0.993
		$E_{\gamma 2 m}$	0	0	0	0
		$a_{\gamma 2 m}$	0	0	0	0
		$C_{\gamma 2 m}$	0	0	0	0
		$P/T_{\gamma 2 m}$	0	0	0	0
		$E_{\gamma 4 a}$	0	0	0	0
1.3E+03	8.7E-01	$P_{\gamma 4 a}$	0	0	0	0
9.9E-01	8.7E-01	$P/T_{\gamma 4 a}$	0	0	0	0
9.9E-01	8.7E-01	$a_{\gamma 5 a}$	0	0	0	0
1.7E-01	8.5E-01	$C_{\gamma 5 a}$	0	0	0	0
1.9E+02	8.7E-01	$P_{\gamma 5 a}$	0	0	0	0
2.9E-02	8.7E-01					
5.3E-01	8.7E-01					
9.9E-01	8.7E-01					
9.9E-01	8.7E-01					
5.6E-01	8.7E-01					

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$	Δd_a	Δd_m	$\delta \varepsilon_{ra}$	$\delta \varepsilon_{rm}$	c_i
0.748	0	0	0	0	0	0	7.0E-02
-0.848	0	0	0	0	0	0	0.0E+00
0.957	0	0	0	0	0	0	-5.4E-02
-0.993	0	0	0	0	0	0	-9.6E-02
1.000	0	0	0	0	0	0	-1.3E-01
0	1	0	0	0	0	0	-6.9E-01
0	0	1	0	0	0	0	7.2E-01
0	0	0	1	0	0	0	4.5E-02
0	0	0	0	1	0	0	-4.6E-02
0	0	0	0	0	1	1	0.0E+00
0	0	0	0	0	1	1	0.0E+00

0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Covariance matrix of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

	a_1	a_0	a_{-1}	a_{-2}	a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$
a_1	1.9E-03	-2.4E-03	7.5E-04	-7.7E-05	2.4E-06	0.0E+00	0.0E+00
a_0	-2.4E-03	3.2E-03	-1.1E-03	1.1E-04	-3.6E-06	0.0E+00	0.0E+00
a_{-1}	7.5E-04	-1.1E-03	3.8E-04	-4.3E-05	1.4E-06	0.0E+00	0.0E+00
a_{-2}	-7.7E-05	1.1E-04	-4.3E-05	4.9E-06	-1.7E-07	0.0E+00	0.0E+00
a_{-3}	2.4E-06	-3.6E-06	1.4E-06	-1.7E-07	5.7E-09	0.0E+00	0.0E+00
$E_{\gamma m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08	0.0E+00
$E_{\gamma a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08
Δd_a	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
Δd_m	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
c_i	7.0E-02	0.0E+00	-5.4E-02	-9.6E-02	-1.3E-01	-6.9E-01	7.2E-01

Covariance matrix of COI_m/COI_a

$C_{\gamma 5 a}$	$P_{\gamma 5 a}$	c_i		a_1	a_0	a_{-1}
0	0	-1.9E-01	a_1	1.9E-03	-2.4E-03	7.5E-04
0	0	-1.3E-01	a_0	-2.4E-03	3.2E-03	-1.1E-03
0	0	-5.4E-02	a_{-1}	7.5E-04	-1.1E-03	3.8E-04
0	0	2.0E-01	a_{-2}	-7.7E-05	1.1E-04	-4.3E-05
0	0	1.4E+00	a_{-3}	2.4E-06	-3.6E-06	1.4E-06
0	0	9.7E-05	$E_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
0	0	-1.4E-01	$a_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
0	0	-1.4E-01	$c_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
0	0	7.4E-01	$P/T_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
0	0	-3.8E-05	$E_{\gamma 4 a}$	0.0E+00	0.0E+00	0.0E+00
0	0	3.5E-01	$P_{\gamma 4 a}$	0.0E+00	0.0E+00	0.0E+00
0	0	-1.8E-02	$P/T_{\gamma 4 a}$	0.0E+00	0.0E+00	0.0E+00
0	0	1.0E-02	$a_{\gamma 5 a}$	0.0E+00	0.0E+00	0.0E+00
1	0	1.0E-02	$c_{\gamma 5 a}$	0.0E+00	0.0E+00	0.0E+00
0	1	-1.9E-02	$P_{\gamma 5 a}$	0.0E+00	0.0E+00	0.0E+00
			c_i	-1.9E-01	-1.3E-01	-5.4E-02

0	0	0	0	0	0	0
1	0	0	0	0	0	0
0	1	0	0	0	0	0
0	0	1	0	0	0	0
0	0	0	1	0	0	0
0	0	0	0	1	0	0
0	0	0	0	0	1	0
0	0	0	0	0	0	1
0	0	0	0	0	0	0

Δd_a	Δd_m	$\delta \varepsilon_{r_a}$	$\delta \varepsilon_{r_m}$
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
8.3E-02	0.0E+00	0.0E+00	0.0E+00
0.0E+00	8.3E-02	0.0E+00	0.0E+00
0.0E+00	0.0E+00	3.0E-05	3.1E-05
0.0E+00	0.0E+00	3.1E-05	3.1E-05
4.5E-02	-4.6E-02	0.0E+00	0.0E+00

a_{-2}	a_{-3}	$E_{\gamma 2 m}$	$a_{\gamma 2 m}$	$C_{\gamma 2 m}$	$P/T_{\gamma 2 m}$	$E_{\gamma 4 a}$
-7.7E-05	2.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
1.1E-04	-3.6E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-4.3E-05	1.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
4.9E-06	-1.7E-07	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-1.7E-07	5.7E-09	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	1.3E-02	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	5.2E-04	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-02
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.6E-03	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
2.0E-01	1.4E+00	9.7E-05	-1.4E-01	-1.4E-01	7.4E-01	-3.8E-05

Covariance matrix of ρ_a

ν	c_i	t_i	μ
0	3.4E-15	t_i	3.0E+02
0	-1.9E-09	μ	0.0E+00
0	4.6E-15	$t_{1/2 a}$	0.0E+00
0	-2.3E-16	$t_{1/2 m}$	0.0E+00
0	7.0E-15	$t_{d a}$	0.0E+00
0	4.7E-15	$t_{c a}$	0.0E+00
0	-3.2E-14	$t_{i a}$	0.0E+00
0	-1.6E-16	$t_{d m}$	0.0E+00
0	-2.0E-12	$t_{c m}$	0.0E+00
0	5.4E-11	$t_{i m}$	0.0E+00
0	4.1E-12	$n_{p a}$	0.0E+00
0	-2.8E-13	$n_{p m}$	0.0E+00
0	-5.0E-04	$k_{0 Au(a)}$	0.0E+00
0	2.9E-08	$k_{0 Au(m)}$	0.0E+00
0	-3.6E-08	$G_{th a}$	0.0E+00
0	-2.6E-09	$G_{e a}$	0.0E+00
0	3.4E-08	$G_{th m}$	0.0E+00
0	5.0E-09	$G_{e m}$	0.0E+00
0	-1.5E-10	f	0.0E+00
0	-9.4E-09	α	0.0E+00
0	-2.9E-09	$Q_{0 a}$	0.0E+00

0	-9.2E-14	E_{r_a}	0.0E+00	0.0E+00
0	2.6E-09	Q_{0_m}	0.0E+00	0.0E+00
0	1.1E-12	E_{r_m}	0.0E+00	0.0E+00
0	4.1E-08	$\varepsilon_{p_m}^{geo} / \varepsilon_{p_a}^{geo}$	0.0E+00	0.0E+00
0	4.5E-08	COI_m / COI_a	0.0E+00	0.0E+00
0	4.6E-06	m_m	0.0E+00	0.0E+00
0	-1.6E-07	m_a	0.0E+00	0.0E+00
0	8.4E-06	w_m	0.0E+00	0.0E+00
1	-3.9E-10	ν	0.0E+00	0.0E+00
		c_i	3.4E-15	-1.9E-09

$P_{\gamma 4 a}$	$P/T_{\gamma 4 a}$	$a_{\gamma 5 a}$	$C_{\gamma 5 a}$	$P_{\gamma 5 a}$	
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	1.6E-03	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
1.3E-08	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	4.7E-03	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-06
3.5E-01	-1.8E-02	1.0E-02	1.0E-02	1.0E-02	-1.9E-02

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
4.6E-15	-2.3E-16	7.0E-15	4.7E-15	-3.2E-14	-1.6E-16

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-2.0E-12	5.4E-11	4.1E-12	-2.8E-13	-5.0E-04	2.9E-08

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-3.6E-08	-2.6E-09	3.4E-08	5.0E-09	-1.5E-10

0.0E+00	0.0E+00	2.3E+04	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	3.6E-03	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	4.8E+01	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	3.5E-04
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-9.4E-09	-2.9E-09	-9.2E-14	2.6E-09	1.1E-12	4.1E-08

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
2.6E-04	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	2.5E-09	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	2.5E-09	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	2.1E-09	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.4E+00
4.5E-08	4.6E-06	-1.6E-07	8.4E-06	-3.9E-10

Irradiation and γ -spectrometry

end irradiation 9/12/2017 2.46 PM
 irradiation time / s 21600

library CSF.Lib
 calib OR50_source2016_geom_cont_12052017.Clb
 sm type CSF.Lib (ROI32 Analysis)

Nuclide	Channel	Energy	Background
65Zn		4460.76	1115.5
Co60		4691.96	1173.2

	target	product
analite, a	^{64}Zn	^{65}Zn
monitor, m	^{59}Co	^{60}Co

Uncertainty budget of ρ_a

Input Quantity	Quantity	Unit	Value
X_i	X_i	$[X_i]$	x_i
t_i		s	21600
μ		1	0.0445
$t_{1/2 a}$		s	21107520
	λ_a	s^{-1}	3.3E-08
$t_{1/2 m}$		s	1.7E+08
	λ_m	s^{-1}	4.2E-09
$t_{d a}$		s	2404405
$t_{c a}$		s	1292628
$t_{i a}$		s	1264268
$t_{d m}$		s	3722775
$t_{c m}$		s	797
$t_{i m}$		s	740
	δ_a	1	1.022
	δ_m	1	1.077
	ξ_a	1	1.00098
	ξ_m	1	1.00319
$n_{p a}$		1	122602
$n_{p m}$		1	137487
$k_{0 Au(a)}$		1	0.005720
$k_{0 Au(m)}$		1	1.3200
$G_{th a}$		1	1

$G_{e a}$		1	1
$G_{th m}$		1	1
$G_{e m}$		1	1
f		1	15.60
α		1	-0.0360
$Q_{0 a}$		1	1.91
$E_{r a}$		eV	2560
	$Q_{0 a}(\alpha)$	1	2.41
$Q_{0 m}$		1	1.993
$E_{r m}$		eV	136.0
	$Q_{0 m}(\alpha)$	1	2.319
$\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$		1	0.9583
COI_m / COI_a		1	0.857
m_m		g	0.00847
m_a		g	0.24000
w_m		$g g^{-1}$	0.004597
ν		$mg L^{-1}$	99.2
Y		[Y]	y
ρ_a		$g mL^{-1}$	2.220E-08

Uncertainty budget of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

Input Quantity	Quantity	Unit	Value
X_i	X_i	[X_i]	x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
$a_{.1}$		Mev	0.403
$a_{.2}$		Mev2	-0.0320
$a_{.3}$		Mev3	0.000573
$E_{\gamma m}$		MeV	1.17320
$E_{\gamma a}$		MeV	1.11550
Δd_a		mm	0
Δd_m		mm	0
	e_4	keV-4	-7.1E-11
	e_3	keV-3	5.2E-08
	e_2	keV-2	-1.4E-05
	e_1	keV-1	1.8E-03
	e_0		1 -4.5E-02
	d_1	keV-1	5.6E-06

	d_0		1	4.2E-02
$\delta\epsilon_{ra}$		mm^{-1}		0.048
$\delta\epsilon_{rm}$		mm^{-1}		0.048
Y		[Y]	y	
$\epsilon_{pm}^{\text{geo}} / \epsilon_{pa}^{\text{geo}}$		1		0.958

Uncertainty budget of $\text{COI}_m / \text{COI}_a$

Input Quantity	Quantity X_i	Unit [X_i]	Value x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
a_{-1}		Mev	0.403
a_2		Mev2	-0.0320
a_3		Mev3	0.000573
	b_1		1 -0.571
	b_0		1 1.079
	c_2		1 -1.625
	c_1		1 6.678
	c_0		1 -7.006
$E_{\gamma 2m}$		keV	1332.5
$a_{\gamma 2m}$			1 1.000
$c_{\gamma 2m}$			1 1.000
$P/T_{\gamma 2m}$			1 0.197
	Y	[Y]	y
	$\text{COI}_m / \text{COI}_a$		1 0.857

Net area	Cnts/s	Uncert %	FWHM	source file	start counting
122602	0.097	0.38	1.771	OR50_20171025_CSF_si	10/10/2017
137487	185.919	0.32	1.798	OR50_20170925_Co_sa	10/25/2017

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance y $u^2_y(x_i)$	Index	Input for sensit coeff $x_i+u(x_i)$ $y(x_i+u(x_i))$	
17	0.1%	3.2E-16	3.0E-29	0.0%	2.2E+04	2.2E-08
0.0005	1.1%	-1.1E-09	3.0E-25	0.0%	4.5E-02	2.2E-08
8640	0.0%	9.5E-16	6.7E-23	0.0%	2.1E+07	2.2E-08
1.3E-11	0.0%					
2.6E+04	0.0%	-1.3E-16	1.2E-23	0.0%	1.7E+08	2.2E-08
6.5E-13	0.0%					
35	0.0%	7.3E-16	6.4E-28	0.0%	2.4E+06	2.2E-08
0.3	0.0%	1.1E-15	1.0E-31	0.0%	1.3E+06	2.2E-08
0.3	0.0%	-1.8E-14	2.8E-29	0.0%	1.3E+06	2.2E-08
35	0.0%	-9.2E-17	1.0E-29	0.0%	3.7E+06	2.2E-08
0.3	0.0%	-1.2E-12	1.1E-25	0.0%	8.0E+02	2.2E-08
0.3	0.0%	3.1E-11	8.1E-23	0.0%	7.4E+02	2.2E-08
0.000	0.0%					
0.001	0.1%					
0.00001	0.0%					
0.00004	0.0%					
466	0.4%	1.8E-13	7.1E-21	1.2%	1.2E+05	2.2E-08
440	0.3%	-1.6E-13	5.0E-21	0.9%	1.4E+05	2.2E-08
0.000023	0.4%	-3.9E-06	7.9E-21	1.3%	5.7E-03	2.2E-08
0.0053	0.4%	1.7E-08	7.9E-21	1.3%	1.3E+00	2.2E-08
0	0.0%	-1.9E-08	0.0E+00	0.0%	1.0E+00	2.2E-08

	0.0000	0.0%					
	0.006	11.5%	0.0E+00	0.0E+00	0.0%	5.3E-02	9.6E-01
	0.006	11.5%	0.0E+00	0.0E+00	0.0%	5.4E-02	9.6E-01
$u_c(y)$	$u_{c,r}(y)$				Σ		
	0.019	2.0%			100.0%		

Std unc	Rel std unc	Sensit coeff	Variance y	Index	Input for sensit coeff		
$u(x_i)$	$u_r(x_i)$	c_i	$u^2_y(x_i)$		$x_i+u(x_i)$	$y(x_i+u(x_i))$	
	0.043	9.2%	-0.1901	1.7E-05	5.9%	-4.3E-01	8.5E-01
	0.057	1.8%	-0.1427	-1.4E-05	-4.9%	-3.2E+00	8.5E-01
	0.020	4.8%	-0.1070	3.0E-06	1.0%	4.2E-01	8.6E-01
	0.0022	6.9%	-0.0803	-2.2E-07	-0.1%	-3.0E-02	8.6E-01
	0.000075	13.1%	-0.0603	5.0E-09	0.0%	6.5E-04	8.6E-01
	0	0.0%					
	0	0.0%					
	0	0.0%					
	0	0.0%					
	0	0.0%					
	0.1	0.0%	0.0001	1.2E-10	0.0%	1.3E+03	8.6E-01
	0.012	1.2%	-0.1426	2.7E-06	0.9%	1.0E+00	8.6E-01
	0.012	1.2%	-0.1426	2.7E-06	0.9%	1.0E+00	8.6E-01
	0.023	11.5%	0.7343	2.8E-04	96.2%	2.2E-01	8.7E-01
$u_c(y)$	$u_r(y)$				Σ		
	0.017	2.0%			100.0%		

	t_c / s	t_i / s	$t_{dead\ r} / \%$	t_d / s	$t_c / t_{1/2}$	$t_d / t_{1/2}$
10:39 AM	1292628	1264268	2.2%	2404405	0.06	0.1
4:52 PM	797	740	7.2%	3722775	0.00	0.0

Correlation matrix of ρ_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		t_i	μ	$t_{1/2\ a}$	$t_{1/2\ m}$
2.2E+04	2.2E-08	t_i		1	0	0
4.4E-02	2.2E-08	μ		0	1	0
2.1E+07	2.2E-08	$t_{1/2\ a}$		0	0	1
		$t_{1/2\ m}$		0	0	0
1.7E+08	2.2E-08	$t_{d\ a}$		0	0	0
		$t_{c\ a}$		0	0	0
2.4E+06	2.2E-08	$t_{i\ a}$		0	0	0
1.3E+06	2.2E-08	$t_{d\ m}$		0	0	0
1.3E+06	2.2E-08	$t_{c\ m}$		0	0	0
3.7E+06	2.2E-08	$t_{i\ m}$		0	0	0
8.0E+02	2.2E-08	$n_{p\ a}$		0	0	0
7.4E+02	2.2E-08	$n_{p\ m}$		0	0	0
		$k_{0\ Au}(a)$		0	0	0
		$k_{0\ Au}(m)$		0	0	0
		$G_{th\ a}$		0	0	0
		$G_{e\ a}$		0	0	0
1.2E+05	2.2E-08	$G_{th\ m}$		0	0	0
1.4E+05	2.2E-08	$G_{e\ m}$		0	0	0
5.7E-03	2.2E-08	f		0	0	0
1.3E+00	2.2E-08	α		0	0	0
1.0E+00	2.2E-08	$Q_{0\ a}$		0	0	0

1.0E+00	2.2E-08	E_{ra}	0	0	0	0
1.0E+00	2.2E-08	Q_{0m}	0	0	0	0
1.0E+00	2.2E-08	E_{rm}	0	0	0	0
1.5E+01	2.2E-08	$\varepsilon_{pm}^{geo} / \varepsilon_{pa}^i$	0	0	0	0
-4.2E-02	2.2E-08	COI_m / COI_a	0	0	0	0
1.8E+00	2.2E-08	m_m	0	0	0	0
2.3E+03	2.2E-08	m_a	0	0	0	0
		w_m	0	0	0	0
1.9E+00	2.2E-08	v	0	0	0	0
1.3E+02	2.2E-08					
9.4E-01	2.2E-08					
8.4E-01	2.2E-08					
8.4E-03	2.2E-08					
2.4E-01	2.2E-08					
4.6E-03	2.2E-08					
9.8E+01	2.2E-08					

Correlation matrix of $\varepsilon_{pm}^{geo} / \varepsilon_{pa}^{geo}$

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	9.6E-01	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	9.6E-01	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	9.6E-01	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	9.6E-01	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	9.6E-01	a_{-3}	0.748	-0.848	0.957	-0.993
1.2E+00	9.6E-01	$E_{\gamma m}$	0	0	0	0
1.1E+00	9.6E-01	$E_{\gamma a}$	0	0	0	0
-2.9E-01	9.5E-01	Δd_a	0	0	0	0
-2.9E-01	9.7E-01	Δd_m	0	0	0	0
		$\delta \varepsilon_{ra}$	0	0	0	0
		$\delta \varepsilon_{rm}$	0	0	0	0

4.2E-02 9.6E-01
 4.3E-02 9.6E-01

Correlation matrix of COI_m / COI_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	8.7E-01	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	8.7E-01	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	8.6E-01	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	8.6E-01	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	8.6E-01	a_{-3}	0.748	-0.848	0.957	-0.993
		$E_{\gamma^2 m}$	0	0	0	0
		$a_{\gamma^2 m}$	0	0	0	0
		$C_{\gamma^2 m}$	0	0	0	0
		$P/T_{\gamma^2 m}$	0	0	0	0
1.3E+03	8.6E-01					
9.9E-01	8.6E-01					
9.9E-01	8.6E-01					
1.7E-01	8.4E-01					

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$	Δd_a	Δd_m	$\delta \varepsilon_{ra}$	$\delta \varepsilon_{rm}$	c_i
0.748	0	0	0	0	0	0	5.5E-02
-0.848	0	0	0	0	0	0	0.0E+00
0.957	0	0	0	0	0	0	-4.2E-02
-0.993	0	0	0	0	0	0	-7.4E-02
1.000	0	0	0	0	0	0	-9.7E-02
0	1	0	0	0	0	0	-7.0E-01
0	0	1	0	0	0	0	7.2E-01
0	0	0	1	0	0	0	4.6E-02
0	0	0	0	1	0	0	-4.6E-02
0	0	0	0	0	1	1	0.0E+00
0	0	0	0	0	0	1	0.0E+00

Covariance

a_{-3}	$E_{\gamma 2 m}$	$a_{\gamma 2 m}$	$c_{\gamma 2 m}$	$P/T_{\gamma 2 m}$	c_i	
0.748	0	0	0	0	-1.9E-01	a_1
-0.848	0	0	0	0	-1.4E-01	a_0
0.957	0	0	0	0	-1.1E-01	a_{-1}
-0.993	0	0	0	0	-8.0E-02	a_{-2}
1.000	0	0	0	0	-6.0E-02	a_{-3}
0	1	0	0	0	9.6E-05	$E_{\gamma 2 m}$
0	0	1	0	0	-1.4E-01	$a_{\gamma 2 m}$
0	0	0	1	0	-1.4E-01	$c_{\gamma 2 m}$
0	0	0	0	1	7.3E-01	$P/T_{\gamma 2 m}$

c_i

0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Covariance matrix of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

	a_1	a_0	a_{-1}	a_{-2}	a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$
a_1	1.9E-03	-2.4E-03	7.5E-04	-7.7E-05	2.4E-06	0.0E+00	0.0E+00
a_0	-2.4E-03	3.2E-03	-1.1E-03	1.1E-04	-3.6E-06	0.0E+00	0.0E+00
a_{-1}	7.5E-04	-1.1E-03	3.8E-04	-4.3E-05	1.4E-06	0.0E+00	0.0E+00
a_{-2}	-7.7E-05	1.1E-04	-4.3E-05	4.9E-06	-1.7E-07	0.0E+00	0.0E+00
a_{-3}	2.4E-06	-3.6E-06	1.4E-06	-1.7E-07	5.7E-09	0.0E+00	0.0E+00
$E_{\gamma m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08	0.0E+00
$E_{\gamma a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08
Δd_a	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
Δd_m	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
c_i	5.5E-02	0.0E+00	-4.2E-02	-7.4E-02	-9.7E-02	-7.0E-01	7.2E-01

matrix of COI_m/COI_a

a_1	a_0	a_{-1}	a_{-2}	a_{-3}	$E_{\gamma 2 m}$	$a_{\gamma 2 m}$	$c_{\gamma 2 m}$	$P/T_{\gamma 2 m}$
1.9E-03	-2.4E-03	7.5E-04	-7.7E-05	2.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-2.4E-03	3.2E-03	-1.1E-03	1.1E-04	-3.6E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00
7.5E-04	-1.1E-03	3.8E-04	-4.3E-05	1.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-7.7E-05	1.1E-04	-4.3E-05	4.9E-06	-1.7E-07	0.0E+00	0.0E+00	0.0E+00	0.0E+00
2.4E-06	-3.6E-06	1.4E-06	-1.7E-07	5.7E-09	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-02	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	5.2E-04
-1.9E-01	-1.4E-01	-1.1E-01	-8.0E-02	-6.0E-02	9.6E-05	-1.4E-01	-1.4E-01	7.3E-01

0	0	0	0	0	0	0
1	0	0	0	0	0	0
0	1	0	0	0	0	0
0	0	1	0	0	0	0
0	0	0	1	0	0	0
0	0	0	0	1	0	0
0	0	0	0	0	1	0
0	0	0	0	0	0	1
0	0	0	0	0	0	0

Δd_a	Δd_m	$\delta \varepsilon_{r_a}$	$\delta \varepsilon_{r_m}$
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
8.3E-02	0.0E+00	0.0E+00	0.0E+00
0.0E+00	8.3E-02	0.0E+00	0.0E+00
0.0E+00	0.0E+00	3.1E-05	3.1E-05
0.0E+00	0.0E+00	3.1E-05	3.1E-05
4.6E-02	-4.6E-02	0.0E+00	0.0E+00

Covariance matrix of ρ_a

ν	c_i	t_i	μ
0	3.2E-16	t_i	3.0E+02
0	-1.1E-09	μ	0.0E+00
0	9.5E-16	$t_{1/2 a}$	0.0E+00
0	-1.3E-16	$t_{1/2 m}$	0.0E+00
0	7.3E-16	$t_{d a}$	0.0E+00
0	1.1E-15	$t_{c a}$	0.0E+00
0	-1.8E-14	$t_{i a}$	0.0E+00
0	-9.2E-17	$t_{d m}$	0.0E+00
0	-1.2E-12	$t_{c m}$	0.0E+00
0	3.1E-11	$t_{i m}$	0.0E+00
0	1.8E-13	$n_{p a}$	0.0E+00
0	-1.6E-13	$n_{p m}$	0.0E+00
0	-3.9E-06	$k_{0 Au(a)}$	0.0E+00
0	1.7E-08	$k_{0 Au(m)}$	0.0E+00
0	-1.9E-08	$G_{th a}$	0.0E+00
0	-3.0E-09	$G_{e a}$	0.0E+00
0	1.9E-08	$G_{th m}$	0.0E+00
0	2.9E-09	$G_{e m}$	0.0E+00
0	6.6E-12	f	0.0E+00
0	7.6E-09	α	0.0E+00
0	-1.6E-09	$Q_{0 a}$	0.0E+00

0	-3.4E-14	E_{r_a}	0.0E+00	0.0E+00
0	1.5E-09	Q_{0_m}	0.0E+00	0.0E+00
0	6.1E-13	E_{r_m}	0.0E+00	0.0E+00
0	2.3E-08	$\varepsilon_{p_m}^{geo} / \varepsilon_{p_a}^{geo}$	0.0E+00	0.0E+00
0	2.6E-08	COI_m / COI_a	0.0E+00	0.0E+00
0	2.6E-06	m_m	0.0E+00	0.0E+00
0	-9.2E-08	m_a	0.0E+00	0.0E+00
0	4.8E-06	w_m	0.0E+00	0.0E+00
1	-2.2E-10	ν	0.0E+00	0.0E+00
		c_i	3.2E-16	-1.1E-09

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
9.5E-16	-1.3E-16	7.3E-16	1.1E-15	-1.8E-14	-9.2E-17

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-1.2E-12	3.1E-11	1.8E-13	-1.6E-13	-3.9E-06	1.7E-08

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-1.9E-08	-3.0E-09	1.9E-08	2.9E-09	6.6E-12

0.0E+00	0.0E+00	6.6E+04	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	3.6E-03	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	4.8E+01	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	3.6E-04
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
7.6E-09	-1.6E-09	-3.4E-14	1.5E-09	6.1E-13	2.3E-08

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
2.9E-04	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	2.5E-09	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	2.5E-09	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	2.1E-09	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.4E+00
2.6E-08	2.6E-06	-9.2E-08	4.8E-06	-2.2E-10

Irradiation and γ -spectrometry

end irradiation 9/12/2017 2.46 PM
 irradiation time / s 21600

library CSF.Lib
 calib OR50_source2016_geom_cont_12052017.Clb
 sm type CSF.Lib (ROI32 Analysis)

Nuclide	Channel	Energy	Background
Co60		4692.95	1173.2
Co60		4691.96	1173.2

	target	product
analite, a	^{59}Co	^{60}Co
monitor, m	^{59}Co	^{60}Co

Uncertainty budget of ρ_a

Input Quantity	Quantity	Unit	Value
X_i	X_i	$[X_i]$	x_i
t_i		s	21600
μ		1	0.0445
$t_{1/2 a}$		s	166345920
	λ_a	s^{-1}	4.2E-09
$t_{1/2 m}$		s	1.7E+08
	λ_m	s^{-1}	4.2E-09
$t_{d a}$		s	2404405
$t_{c a}$		s	1292628
$t_{i a}$		s	1264268
$t_{d m}$		s	3722775
$t_{c m}$		s	797
$t_{i m}$		s	740
	δ_a	1	1.022
	δ_m	1	1.077
	ξ_a	1	1.00098
	ξ_m	1	1.00319
$n_{p a}$		1	4676
$n_{p m}$		1	137487
$k_{0 Au(a)}$		1	1.3200
$k_{0 Au(m)}$		1	1.3200
$G_{th a}$		1	1

$G_{e a}$		1	1
$G_{th m}$		1	1
$G_{e m}$		1	1
f		1	15.60
α		1	-0.0360
$Q_{0 a}$		1	1.993
$E_{r a}$		eV	136.0
	$Q_{0 a}(\alpha)$	1	2.32
$Q_{0 m}$		1	1.993
$E_{r m}$		eV	136.0
	$Q_{0 m}(\alpha)$	1	2.319
$\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$		1	1.0000
COI_m / COI_a		1	1.000
m_m		g	0.00847
m_a		g	0.24000
w_m		$g g^{-1}$	0.004597
ν		$mg L^{-1}$	99.2
Y		[Y]	y
ρ_a		$g mL^{-1}$	3.24E-11

Uncertainty budget of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

Input Quantity	Quantity	Unit	Value
X_i	X_i	[X_i]	x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
$a_{.1}$		Mev	0.403
$a_{.2}$		Mev2	-0.0320
$a_{.3}$		Mev3	0.000573
$E_{\gamma m}$		MeV	1.17320
$E_{\gamma a}$		MeV	1.17320
Δd_a		mm	0
Δd_m		mm	0
	e_4	keV-4	-7.1E-11
	e_3	keV-3	5.2E-08
	e_2	keV-2	-1.4E-05
	e_1	keV-1	1.8E-03
	e_0		1 -4.5E-02
	d_1	keV-1	5.6E-06

	d_0		1	4.2E-02
$\delta\epsilon_{ra}$		mm^{-1}		0.048
$\delta\epsilon_{rm}$		mm^{-1}		0.048
Y		[Y]	y	
$\epsilon_{pm}^{\text{geo}} / \epsilon_{pa}^{\text{geo}}$		1		1.000

Uncertainty budget of $\text{COI}_m / \text{COI}_a$

Input Quantity	Quantity X_i	Unit [X_i]	Value x_i
a_1		Mev-1	-0.472
a_0			1 -3.229
a_{-1}		Mev	0.403
a_2		Mev2	-0.0320
a_3		Mev3	0.000573
	b_1		1 -0.571
	b_0		1 1.079
	c_2		1 -1.625
	c_1		1 6.678
	c_0		1 -7.006
$E_{\gamma 2m}$		keV	1332.5
$a_{\gamma 2m}$			1 1.000
$c_{\gamma 2m}$			1 1.000
$P/T_{\gamma 2m}$			1 0.197
$E_{\gamma 2a}$		keV	1332.5
$a_{\gamma 2a}$			1 1.000
$c_{\gamma 2a}$			1 1.000
$P/T_{\gamma 2a}$			1 0.197
	Y	[Y]	y
	$\text{COI}_m / \text{COI}_a$		1 1.000

Net area	Cnts/s	Uncert %	FWHM	source file	start counting
4676	0.004	9.36	1.630	OR50_20171025_CSF_s	10/10/2017
137487	185.919	0.32	1.798	OR50_20170925_Co_sa	10/25/2017

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance y $u^2_y(x_i)$	Index	Input for sensit coeff $x_i+u(x_i)$ $y(x_i+u(x_i))$	
17	0.1%	1.9E-28	1.0E-53	0.0%	2.2E+04	3.2E-11
0.0005	1.1%	-1.6E-12	6.5E-31	0.0%	4.5E-02	3.2E-11
25920	0.0%	1.9E-19	7.1E-32	0.0%	1.7E+08	3.2E-11
6.5E-13	0.0%					
2.6E+04	0.0%	-1.9E-19	-7.0E-32	0.0%	1.7E+08	3.2E-11
6.5E-13	0.0%					
35	0.0%	1.4E-19	2.2E-35	0.0%	2.4E+06	3.2E-11
0.3	0.0%	1.2E-18	1.1E-37	0.0%	1.3E+06	3.2E-11
0.3	0.0%	-2.7E-17	6.0E-35	0.0%	1.3E+06	3.2E-11
35	0.0%	-1.4E-19	2.2E-35	0.0%	3.7E+06	3.2E-11
0.3	0.0%	-1.7E-15	2.4E-31	0.0%	8.0E+02	3.2E-11
0.3	0.0%	4.6E-14	1.7E-28	0.0%	7.4E+02	3.2E-11
0.000	0.0%					
0.001	0.1%					
0.00001	0.0%					
0.00004	0.0%					
438	9.4%	6.9E-15	9.2E-24	92.8%	5.1E+03	3.5E-11
440	0.3%	-2.4E-16	1.1E-26	0.1%	1.4E+05	3.2E-11
0.0053	0.4%	-2.5E-11	2.7E-31	0.0%	1.3E+00	3.2E-11
0.0053	0.4%	2.5E-11	-2.7E-31	0.0%	1.3E+00	3.3E-11
0	0.0%	-2.8E-11	0.0E+00	0.0%	1.0E+00	3.2E-11

	0.0000	0.0%					
	0.006	11.5%	0.0E+00	0.0E+00	0.0%	5.4E-02	1.0E+00
	0.006	11.5%	0.0E+00	0.0E+00	0.0%	5.4E-02	1.0E+00
$u_c(y)$	$u_{c,r}(y)$				Σ		
	0.020	2.0%					100.0%

Std unc $u(x_i)$	Rel std unc $u_r(x_i)$	Sensit coeff c_i	Variance y $u^2_y(x_i)$	Index	Input for sensit coeff		
					$x_i+u(x_i)$	$y(x_i+u(x_i))$	
0.043	9.2%	0.0000	0.0E+00	0.0%	-4.3E-01	1.0E+00	
0.057	1.8%	0.0000	0.0E+00	0.0%	-3.2E+00	1.0E+00	
0.020	4.8%	0.0000	0.0E+00	0.0%	4.2E-01	1.0E+00	
0.0022	6.9%	0.0000	0.0E+00	0.0%	-3.0E-02	1.0E+00	
0.000075	13.1%	0.0000	0.0E+00	0.0%	6.5E-04	1.0E+00	
0	0.0%						
0	0.0%						
0	0.0%						
0	0.0%						
0	0.0%						
0.1	0.0%	0.0001	-3.0E-19	0.0%	1.3E+03	1.0E+00	
0.012	1.2%	-0.1663	-1.4E-11	-0.1%	1.0E+00	1.0E+00	
0.012	1.2%	-0.1663	-1.4E-11	-0.1%	1.0E+00	1.0E+00	
0.023	11.5%	0.8564	-1.9E-06	-20439%	2.2E-01	1.0E+00	
0.12	0.0%	-0.0001	3.0E-19	0.0%	1.3E+03	1.0E+00	
0.012	1.2%	0.1663	1.4E-11	0.1%	1.0E+00	1.0E+00	
0.012	1.2%	0.1663	1.4E-11	0.1%	1.0E+00	1.0E+00	
0.023	11.5%	-0.8606	1.9E-06	20539%	2.2E-01	9.8E-01	
$u_c(y)$	$u_r(y)$						
	0.000	0.0%					100.0%

	t_c / s	t_i / s	$t_{dead r} / \%$	t_d / s	$t_c / t_{1/2}$	$t_d / t_{1/2}$
10:39 AM	1292628	1264268	2.2%	2404405	0.01	0.0
4:52 PM	797	740	7.2%	3722775	0.00	0.0

Correlation matrix of ρ_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		t_i	μ	$t_{1/2 a}$	$t_{1/2 m}$
2.2E+04	3.2E-11	t_i	1	0	0	0
4.4E-02	3.2E-11	μ	0	1	0	0
1.7E+08	3.2E-11	$t_{1/2 a}$	0	0	1	1
		$t_{1/2 m}$	0	0	1	1
1.7E+08	3.2E-11	$t_{d a}$	0	0	0	0
		$t_{c a}$	0	0	0	0
2.4E+06	3.2E-11	$t_{i a}$	0	0	0	0
1.3E+06	3.2E-11	$t_{d m}$	0	0	0	0
1.3E+06	3.2E-11	$t_{c m}$	0	0	0	0
3.7E+06	3.2E-11	$t_{i m}$	0	0	0	0
8.0E+02	3.2E-11	$n_{p a}$	0	0	0	0
7.4E+02	3.2E-11	$n_{p m}$	0	0	0	0
		$k_{0 Au(a)}$	0	0	0	0
		$k_{0 Au(m)}$	0	0	0	0
		$G_{th a}$	0	0	0	0
		$G_{e a}$	0	0	0	0
4.2E+03	2.9E-11	$G_{th m}$	0	0	0	0
1.4E+05	3.3E-11	$G_{e m}$	0	0	0	0
1.3E+00	3.3E-11	f	0	0	0	0
1.3E+00	3.2E-11	α	0	0	0	0
1.0E+00	3.2E-11	$Q_{0 a}$	0	0	0	0

1.0E+00	3.2E-11	E_{ra}	0	0	0	0
1.0E+00	3.2E-11	Q_{0m}	0	0	0	0
1.0E+00	3.2E-11	E_{rm}	0	0	0	0
1.5E+01	3.2E-11	$\varepsilon_{pm}^{geo} / \varepsilon_{pa}^i$	0	0	0	0
-4.2E-02	3.2E-11	COI_m / COI_a	0	0	0	0
1.9E+00	3.3E-11	m_m	0	0	0	0
1.3E+02	3.2E-11	m_a	0	0	0	0
		w_m	0	0	0	0
1.9E+00	3.2E-11	v	0	0	0	0
1.3E+02	3.2E-11					
9.8E-01	3.2E-11					
1.0E+00	3.2E-11					
8.4E-03	3.2E-11					
2.4E-01	3.2E-11					
4.6E-03	3.2E-11					
9.8E+01	3.3E-11					

Correlation matrix of $\varepsilon_{pm}^{geo} / \varepsilon_{pa}^{geo}$

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	1.0E+00	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	1.0E+00	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	1.0E+00	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	1.0E+00	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	1.0E+00	a_{-3}	0.748	-0.848	0.957	-0.993
1.2E+00	1.0E+00	$E_{\gamma m}$	0	0	0	0
1.2E+00	1.0E+00	$E_{\gamma a}$	0	0	0	0
-2.9E-01	9.9E-01	Δd_a	0	0	0	0
-2.9E-01	1.0E+00	Δd_m	0	0	0	0
		$\delta \varepsilon_{ra}$	0	0	0	0
		$\delta \varepsilon_{rm}$	0	0	0	0

4.3E-02 1.0E+00
 4.3E-02 1.0E+00

Correlation matrix of COI_m / COI_a

$x_i - u(x_i)$	$y(x_i - u(x_i))$		a_1	a_0	a_{-1}	a_{-2}
-5.2E-01	1.0E+00	a_1	1.000	-0.973	0.884	-0.804
-3.3E+00	1.0E+00	a_0	-0.973	1.000	-0.957	0.896
3.8E-01	1.0E+00	a_{-1}	0.884	-0.957	1.000	-0.984
-3.4E-02	1.0E+00	a_{-2}	-0.804	0.896	-0.984	1.000
5.0E-04	1.0E+00	a_{-3}	0.748	-0.848	0.957	-0.993
		$E_{\gamma 2 m}$	0	0	0	0
		$a_{\gamma 2 m}$	0	0	0	0
		$C_{\gamma 2 m}$	0	0	0	0
		$P/T_{\gamma 2 m}$	0	0	0	0
		$E_{\gamma 2 a}$	0	0	0	0
1.3E+03	1.0E+00	$a_{\gamma 2 a}$	0	0	0	0
9.9E-01	1.0E+00	$C_{\gamma 2 a}$	0	0	0	0
9.9E-01	1.0E+00	$P/T_{\gamma 2 a}$	0	0	0	0
1.7E-01	9.8E-01					
1.3E+03	1.0E+00					
9.9E-01	1.0E+00					
9.9E-01	1.0E+00					
1.7E-01	1.0E+00					

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$	Δd_a	Δd_m	$\delta \varepsilon_{ra}$	$\delta \varepsilon_{rm}$	c_i
0.748	0	0	0	0	0	0	0.0E+00
-0.848	0	0	0	0	0	0	0.0E+00
0.957	0	0	0	0	0	0	0.0E+00
-0.993	0	0	0	0	0	0	0.0E+00
1.000	0	0	0	0	0	0	0.0E+00
0	1	0	0	0	0	0	-7.3E-01
0	0	1	0	0	0	0	7.3E-01
0	0	0	1	0	0	0	4.8E-02
0	0	0	0	1	0	0	-4.8E-02
0	0	0	0	0	1	1	0.0E+00
0	0	0	0	0	1	1	0.0E+00

a_{-3}	$E_{\gamma 2 m}$	$a_{\gamma 2 m}$	$c_{\gamma 2 m}$	$P/T_{\gamma 2 m}$	$E_{\gamma 2 a}$	$a_{\gamma 2 a}$	$c_{\gamma 2 a}$	$P/T_{\gamma 2 a}$	
0.748	0	0	0	0	0	0	0	0	0
-0.848	0	0	0	0	0	0	0	0	0
0.957	0	0	0	0	0	0	0	0	0
-0.993	0	0	0	0	0	0	0	0	0
1.000	0	0	0	0	0	0	0	0	0
0	1	0	0	0	0	1	0	0	0
0	0	1	0	0	0	0	1	0	0
0	0	0	1	0	0	0	0	1	0
0	0	0	0	1	0	0	0	0	1
0	1	0	0	0	0	1	0	0	0
0	0	1	0	0	0	0	1	0	0
0	0	0	1	0	0	0	0	1	0
0	0	0	0	1	0	0	0	0	1

0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	1	0
0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Covariance matrix of $\varepsilon_{p m}^{geo} / \varepsilon_{p a}^{geo}$

	a_1	a_0	a_{-1}	a_{-2}	a_{-3}	$E_{\gamma m}$	$E_{\gamma a}$
a_1	1.9E-03	-2.4E-03	7.5E-04	-7.7E-05	2.4E-06	0.0E+00	0.0E+00
a_0	-2.4E-03	3.2E-03	-1.1E-03	1.1E-04	-3.6E-06	0.0E+00	0.0E+00
a_{-1}	7.5E-04	-1.1E-03	3.8E-04	-4.3E-05	1.4E-06	0.0E+00	0.0E+00
a_{-2}	-7.7E-05	1.1E-04	-4.3E-05	4.9E-06	-1.7E-07	0.0E+00	0.0E+00
a_{-3}	2.4E-06	-3.6E-06	1.4E-06	-1.7E-07	5.7E-09	0.0E+00	0.0E+00
$E_{\gamma m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08	0.0E+00
$E_{\gamma a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-08
Δd_a	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
Δd_m	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r a}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
$\delta \varepsilon_{r m}$	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
c_i	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	-7.3E-01	7.3E-01

Covariance matrix of COI_m/COI_a

c_i		a_1	a_0	a_{-1}
0.0E+00	a_1	1.9E-03	-2.4E-03	7.5E-04
0.0E+00	a_0	-2.4E-03	3.2E-03	-1.1E-03
0.0E+00	a_{-1}	7.5E-04	-1.1E-03	3.8E-04
0.0E+00	a_2	-7.7E-05	1.1E-04	-4.3E-05
0.0E+00	a_3	2.4E-06	-3.6E-06	1.4E-06
1.1E-04	$E_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
-1.7E-01	$a_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
-1.7E-01	$c_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
8.6E-01	$P/T_{\gamma 2 m}$	0.0E+00	0.0E+00	0.0E+00
-1.1E-04	$E_{\gamma 2 a}$	0.0E+00	0.0E+00	0.0E+00
1.7E-01	$a_{\gamma 2 a}$	0.0E+00	0.0E+00	0.0E+00
1.7E-01	$c_{\gamma 2 a}$	0.0E+00	0.0E+00	0.0E+00
-8.6E-01	$P/T_{\gamma 2 a}$	0.0E+00	0.0E+00	0.0E+00
	c_i	0.0E+00	0.0E+00	0.0E+00

0	1	0	0	0	0	0
1	0	0	0	0	0	0
0	1	0	0	0	0	0
0	0	1	0	0	0	0
0	0	0	1	0	0	0
0	0	0	0	1	0	0
0	0	0	0	0	1	0
0	0	0	0	0	0	1
0	0	0	0	0	0	0

Δd_a	Δd_m	$\delta \varepsilon_{r_a}$	$\delta \varepsilon_{r_m}$
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00
8.3E-02	0.0E+00	0.0E+00	0.0E+00
0.0E+00	8.3E-02	0.0E+00	0.0E+00
0.0E+00	0.0E+00	3.1E-05	3.1E-05
0.0E+00	0.0E+00	3.1E-05	3.1E-05
4.8E-02	-4.8E-02	0.0E+00	0.0E+00

a_{-2}	a_{-3}	$E_{\gamma 2 m}$	$a_{\gamma 2 m}$	$c_{\gamma 2 m}$	$P/T_{\gamma 2 m}$	$E_{\gamma 2 a}$
-7.7E-05	2.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
1.1E-04	-3.6E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-4.3E-05	1.4E-06	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
4.9E-06	-1.7E-07	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-1.7E-07	5.7E-09	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	1.3E-02	0.0E+00	0.0E+00	0.0E+00	1.3E-02
0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	5.2E-04	0.0E+00
0.0E+00	0.0E+00	1.3E-02	0.0E+00	0.0E+00	0.0E+00	1.3E-02
0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.3E-04	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	5.2E-04	0.0E+00
0.0E+00	0.0E+00	1.1E-04	-1.7E-01	-1.7E-01	8.6E-01	-1.1E-04

Covariance matrix of ρ_a

ν	c_i	t_i	μ
0	1.9E-28	t_i	3.0E+02
0	-1.6E-12	μ	0.0E+00
0	1.9E-19	$t_{1/2 a}$	0.0E+00
0	-1.9E-19	$t_{1/2 m}$	0.0E+00
0	1.4E-19	$t_{d a}$	0.0E+00
0	1.2E-18	$t_{c a}$	0.0E+00
0	-2.7E-17	$t_{i a}$	0.0E+00
0	-1.4E-19	$t_{d m}$	0.0E+00
0	-1.7E-15	$t_{c m}$	0.0E+00
0	4.6E-14	$t_{i m}$	0.0E+00
0	6.9E-15	$n_{p a}$	0.0E+00
0	-2.4E-16	$n_{p m}$	0.0E+00
0	-2.5E-11	$k_{0 Au(a)}$	0.0E+00
0	2.5E-11	$k_{0 Au(m)}$	0.0E+00
0	-2.8E-11	$G_{th a}$	0.0E+00
0	-4.2E-12	$G_{e a}$	0.0E+00
0	2.8E-11	$G_{th m}$	0.0E+00
0	4.2E-12	$G_{e m}$	0.0E+00
0	0.0E+00	f	0.0E+00
0	0.0E+00	α	0.0E+00
0	-2.2E-12	$Q_{0 a}$	0.0E+00

0	-8.9E-16	E_{r_a}	0.0E+00	0.0E+00
0	2.2E-12	Q_{0_m}	0.0E+00	0.0E+00
0	8.9E-16	E_{r_m}	0.0E+00	0.0E+00
0	3.2E-11	$\varepsilon_{p_m}^{geo} / \varepsilon_{p_a}^{geo}$	0.0E+00	0.0E+00
0	3.2E-11	COI_m / COI_a	0.0E+00	0.0E+00
0	3.8E-09	m_m	0.0E+00	0.0E+00
0	-1.4E-10	m_a	0.0E+00	0.0E+00
0	7.0E-09	w_m	0.0E+00	0.0E+00
1	-3.3E-13	ν	0.0E+00	0.0E+00
		c_i	1.9E-28	-1.6E-12

$a_{\gamma 2 a}$	$c_{\gamma 2 a}$	$P/T_{\gamma 2 a}$
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00
1.3E-04	0.0E+00	0.0E+00
0.0E+00	1.3E-04	0.0E+00
0.0E+00	0.0E+00	5.2E-04
0.0E+00	0.0E+00	0.0E+00
1.3E-04	0.0E+00	0.0E+00
0.0E+00	1.3E-04	0.0E+00
0.0E+00	0.0E+00	5.2E-04
1.7E-01	1.7E-01	-8.6E-01

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
1.9E-19	-1.9E-19	1.4E-19	1.2E-18	-2.7E-17	-1.4E-19

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-1.7E-15	4.6E-14	6.9E-15	-2.4E-16	-2.5E-11	2.5E-11

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
-2.8E-11	-4.2E-12	2.8E-11	4.2E-12	0.0E+00

0.0E+00	0.0E+00	4.8E+01	0.0E+00	4.8E+01	0.0E+00
0.0E+00	3.6E-03	0.0E+00	3.6E-03	0.0E+00	0.0E+00
0.0E+00	0.0E+00	4.8E+01	0.0E+00	4.8E+01	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	3.9E-04
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	-2.2E-12	-8.9E-16	2.2E-12	8.9E-16	3.2E-11

0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	0.0E+00
9.1E-09	0.0E+00	0.0E+00	0.0E+00	0.0E+00
0.0E+00	2.5E-09	0.0E+00	0.0E+00	0.0E+00
0.0E+00	0.0E+00	2.5E-09	0.0E+00	0.0E+00
0.0E+00	0.0E+00	0.0E+00	2.1E-09	0.0E+00
0.0E+00	0.0E+00	0.0E+00	0.0E+00	1.4E+00
3.2E-11	3.8E-09	-1.4E-10	7.0E-09	-3.3E-13

1

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4 Title: **An uncertainty spreadsheet for the k_0 -standardisation method in Neutron Activation**
5 **Analysis**

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14 **An uncertainty spreadsheet for the k_0 -standardisation**
15 **method in Neutron Activation Analysis**

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21 **Abstract**

22 This paper focuses on the use of the spreadsheet technique to set up the uncertainty budget
23 for the k_0 -standardisation method in Neutron Activation Analysis. The adopted
24 measurement model included most of presently recognized error sources and was written
25 to limit the covariances between input quantities. The calculations were implemented in a
26 worksheet file and tested in a multi-elemental analysis of a biological material. Besides, it
27 was demonstrated that the k_0 -standardisation turns to the relative-standardisation when the
28 monitor element corresponds to the analyte element. The developed worksheet is available
29 and suitable for the analysis of other materials in different experimental conditions.

30 **Keywords**

31 k_0 -standardisation method, uncertainty budget, spreadsheet technique, correlated input
32 quantities, cerebrospinal fluid

33 **Introduction**

34 In 1995, a guide was published by EURACHEM/CITAC [1] to illustrate the use in
35 chemistry measurements of the general rules outlined in the Guide to the Expression of

36 Uncertainty in Measurement (GUM) [2] for the evaluation and expression of uncertainty.
37 Afterwards, since specific applications in nuclear chemistry measurements were missing
38 in the guide, practical examples for the most common nuclear analytical techniques were
39 included in a report of the International Atomic Energy Agency (IAEA) [3].

40 The Neutron Activation Analysis (NAA) was addressed in the IAEA report, as regards the
41 existing standardisation methods, i.e. the relative- and k_0 -NAA. A detailed list of sources
42 of error were identified and grouped in four categories: i) preparation of samples, ii)
43 neutron irradiation, iii) γ -spectrometry measurements and iv) radiochemical separation, if
44 executed. Two uncertainty budgets were given as examples for the relative-NAA, the first
45 dealing with vanadium in coal fly ash by Instrumental NAA (INAA) and the latter with
46 manganese in animal freeze dried blood by Radiochemical NAA (RNAA). **Only one**
47 example for the k_0 -NAA was cited, with a reference to the (preliminary) evaluation
48 performed by de Corte [4].

49 Next, several studies focused on the k_0 -NAA. Robouch et al [5] suggested the use of the
50 spreadsheet technique developed by Kragten [6] and recommended a general equation to
51 express the uncertainty of the results. Younes et al [7] showed that the sensitivity
52 coefficients, computed by finite difference approximations in the spreadsheet technique,
53 could also be expressed in analytical form. In fact, subsequent works were all based on
54 analytical expressions of the sensitivity coefficients [8, 9].

55 To date, the most comprehensive examples of uncertainty budgets for k_0 -NAA were
56 reported in [9] and concerned the determination of Au, Cr, Rb and Sb in compressed
57 cellulose pellets. The covariances between input quantities, in practice always neglected in
58 the previously available literature, **were** to some extent considered. However, values and
59 expressions of correlation and sensitivity coefficients were omitted.

60 In this study, we adopted a measurement equation modeling most of the acknowledged
61 sources of error and written to limit the covariances. Due to the complexity of the resulting
62 functional relationship, we used the spreadsheet technique and the matrix formalism to
63 propagate the uncertainties, including the outstanding correlations. The formulae were
64 implemented and tested for the determination of trace elements in a biological material.

65 Details on the neutron activation experiment as well as on the characterization of the
66 detection system are here presented to assign estimates, uncertainties and correlation
67 coefficients of the input quantities. Lastly, the uncertainty budgets are briefly discussed to
68 point out the **main** contributors to the combined uncertainties of the results.

69 **Model**

70 The theoretical basis of k_0 -NAA is well established and extensively reported in literature.
71 Simonits et al. proposed the original idea in 1975 [10] following a preliminary study carried
72 out by Girardi et al. [11]. In 1987, de Corte published the most comprehensive development
73 of the method [4], including references to previous papers focused on definitions and
74 assumptions of the standardisation. Here, the basic concepts are briefly recalled to term the
75 input quantities of the measurement model.

76 The formalism underlying the method is based on a rather simple description of the reaction
77 rate per target nuclide, R , following the Høgdahl convention [12] in the case of a (target)
78 nuclide having a $1/E^{1/2}$ dependence of the (n,γ) cross section function, $\sigma(E)$, versus the
79 neutron energy, E .

80 According to the convention, the neutron spectrum is divided in the sub- and epi-cadmium
81 regions, respectively below and above the cadmium cut-off energy fixed to 0.55 eV. The
82 fission component is neglected under the hypothesis that the corresponding contribution to
83 R is small. Accordingly:

$$84 \quad R = G_{\text{th}} \Phi_s \sigma_0 + G_e \Phi_e I_0(\alpha), \quad (1)$$

85 where Φ_s and Φ_e are the (conventional) sub- and epi-cadmium neutron fluxes, G_{th} and G_e
86 are correction factors accounting for the thermal and epithermal neutron self-shielding, σ_0
87 is the thermal cross section, and $I_0(\alpha)$ is the resonance integral for a $1/E^{1+\alpha}$ neutron
88 spectrum in the epi-cadmium region.

89 The knowledge of the time dependence of the amount of produced radionuclide during and
90 after activation combined to the counting of the emitted γ -photons links the number of

91 target nuclides in a sample, N_t , to the number of counts in the full-energy peak of the
92 collected γ -spectrum, n_p , via R .

93 With the exception of branching activation and mother-daughter decay, and neglecting
94 burn-up effects, the relation between N_t and n_p is:

$$95 \quad R N_t \varepsilon_p^{\text{geo}} P_\gamma = \frac{\lambda n_p (\delta \xi / \text{COI})}{(1 - e^{-\lambda t_i}) e^{-\lambda t_d} (1 - e^{-\lambda t_c})}, \quad (2)$$

96 where $R N_t$ is the total reaction rate, $\varepsilon_p^{\text{geo}}$ is the full-energy γ -peak detection efficiency for
97 the actual position and geometry of the sample, P_γ is the absolute emission probability of
98 the γ -photons, t_c and t_i are the counting and live times of the detection system, t_i is the
99 irradiation time, t_d is the decay time after irradiation, COI is the true-coincidence
100 correction factor, $\lambda = \ln(2) / t_{1/2}$ is the decay constant of the produced radionuclide, given
101 its half-life $t_{1/2}$, $\delta = t_c / t_i$ is the dead time correction factor and $\xi = e^{\mu(1 - t_i / t_c)}$ is the
102 **excess counting loss** correction factor, given the **excess counting loss** constant of the
103 detection system, μ , defined in [13].

104 In the case that the (target) nuclide is an isotope of an element in a m mass sample, N_t can
105 be expressed as:

$$106 \quad N_t = \frac{w m x N_A}{M}, \quad (3)$$

107 where x is the abundance of the isotope, N_A is the Avogadro constant, and w and M are the
108 mass fraction and molar mass of the element in the sample, respectively.

109 From eqs. (1), (2) and (3), it follows:

$$110 \quad \frac{\sigma_0 P_\gamma x N_A}{M} = \frac{\lambda n_p (\delta \xi / \text{COI})}{(1 - e^{-\lambda t_i}) e^{-\lambda t_d} (1 - e^{-\lambda t_c}) \varepsilon_p^{\text{geo}}} \frac{1}{m w \phi_s \left(G_{\text{th}} + \frac{G_e Q_0(\alpha)}{f} \right)}, \quad (4)$$

111 where $Q_0(\alpha) = I_0(\alpha) / \sigma_0$ and $f = \Phi_s / \Phi_e$. The $Q_0(\alpha)$ value is obtained by applying the
112 formula $Q_0(\alpha) = (Q_0 - 0.429) \bar{E}_r^{-\alpha} + 0.429 / [0.55^\alpha (1 + 2\alpha)]$, where $Q_0 = I_0 / \sigma_0$ is the

113 ratio of the resonance integral (for a $1/E$ neutron spectrum in the epi-cadmium region) to
 114 the thermal cross section and \bar{E}_r is the effective resonance energy of the target nuclide.

115 It is worth remarking that the parameters on the left-hand side of (4) are independent of the
 116 experimental conditions of irradiation and γ -counting. In fact, the product $\sigma_0 P_\gamma N_A$ is a
 117 constant quantity and the ratio x/M depends on the isotopic composition.

118 The k_0 -NAA measurement model is derived from the application of (4) to the element to
 119 be quantified, i.e. the analyte, and to an element used as a monitor of the of the neutron
 120 fluence rate.

121 The following equation holds under the assumption that analyte and monitor are exposed
 122 to the same (constant) values of Φ_s and Φ_e during the irradiation:

$$123 \quad W_a = \frac{\left. \frac{\lambda n_p \delta \xi}{(1-e^{-\lambda t_i}) e^{-\lambda t_d} (1-e^{-\lambda t_c})} \right|_a}{\left. \frac{\lambda n_p \delta \xi}{(1-e^{-\lambda t_i}) e^{-\lambda t_d} (1-e^{-\lambda t_c})} \right|_m} k_{0 \text{ Au}}(m) \frac{(G_{\text{th } m} + \frac{G_{e m} Q_{0 m}(\alpha)}{f}) \varepsilon_{p m}^{\text{geo}} \text{COI}_m m_m}{k_{0 \text{ Au}}(a) (G_{\text{th } a} + \frac{G_{e a} Q_{0 a}(\alpha)}{f}) \varepsilon_{p a}^{\text{geo}} \text{COI}_a m_a} W_m, \quad (5)$$

124 where the parameters $k_{0 \text{ Au}}(m) = \frac{M_{\text{Au}} \sigma_{0 m} P_{\gamma m} x_m}{M_m \sigma_{0 \text{ Au}} P_{\gamma \text{ Au}} x_{\text{Au}}}$ and $k_{0 \text{ Au}}(a) = \frac{M_{\text{Au}} \sigma_{0 a} P_{\gamma a} x_a}{M_a \sigma_{0 \text{ Au}} P_{\gamma \text{ Au}} x_{\text{Au}}}$ are the
 125 so-called k_0 factors; subscripts a and m refer to the analyte and to the monitor, respectively.

126 The k_0 values have been experimentally determined for the most important (n, γ) reactions
 127 and γ -photons energies with respect to the 411 keV γ -photons emitted by ^{198}Au produced
 128 from ^{197}Au via (n, γ) reaction. A compilation of the recommended $k_{0 \text{ Au}}$, Q_0 and \bar{E}_r values
 129 can be found in [14].

130 **Experimental**

131 To exemplify the use of the equation model (5), we measured a lyophilized sample of
 132 cerebrospinal fluid (CSF). The experiment was intended to set up the uncertainty budget
 133 and not to reach the minimum uncertainty. The results were given in terms of mass

134 concentrations, $\rho_a = w_a/v$, where v is the factor used to convert the mass of lyophilized
135 CSF to the volume of reconstituted CSF.

136 *Preparation of the samples*

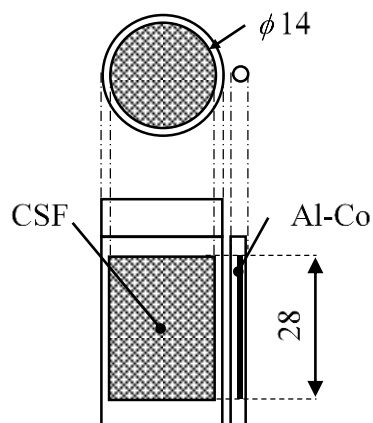
137 Ten vials of lyophilized CSF, each one corresponding to 3 mL volumes of reconstituted
138 CSF, were purchased. The content of every single vial was moved to an acid-cleaned 8 mL
139 cut polyethylene (PE) vial and sealed. The mass to volume conversion factor, $v =$
140 $99.2(12) \text{ mL g}^{-1}$, was obtained as the ratio of 3 mL to the average of the (ten) mass
141 differences between the filled and empty (washed and dried out) vials. Here and hereafter,
142 unless otherwise specified, the brackets refer to the standard uncertainty and apply to the
143 last digits.

144 One sample, about 28 mm length, of an Al-0.46%Co wire (Reactor Experiment, 99.9313%
145 purity, 0.38 mm diameter) was used as a Co monitor. The weighed mass, $m_m =$
146 $8.47(5) \text{ mg}$, was sealed in one PE micro-tube. A conservative 1% relative standard
147 uncertainty was assigned to the declared Co mass fraction value, $w_m = 4.597(46) \times$
148 10^{-3} g g^{-1} .

149 *Neutron irradiation*

150 The neutron irradiation lasted $t_i = 6.000(5) \text{ h}$ and was performed in the 250 kW TRIGA
151 Mark II reactor at the Laboratory of Applied Nuclear Energy (LENA) of the University of
152 Pavia. The quoted uncertainty corresponds to a uniform probability distribution assigned
153 to the t_i value and having a 30 s half-width.

154 The vial containing the lyophilized CSF sample and the micro-tube containing the Al-Co
155 wire were put in one PE container used for irradiation and located in the central channel
156 (CC) of the reactor; the neutron flux parameters at CC, $f = 15.6(3)$ and $\alpha = -0.036(6)$, were
157 recently measured [15]. The position of the lyophilized CSF sample and of the Al-Co wire
158 during the irradiation is shown in Figure 1.



159

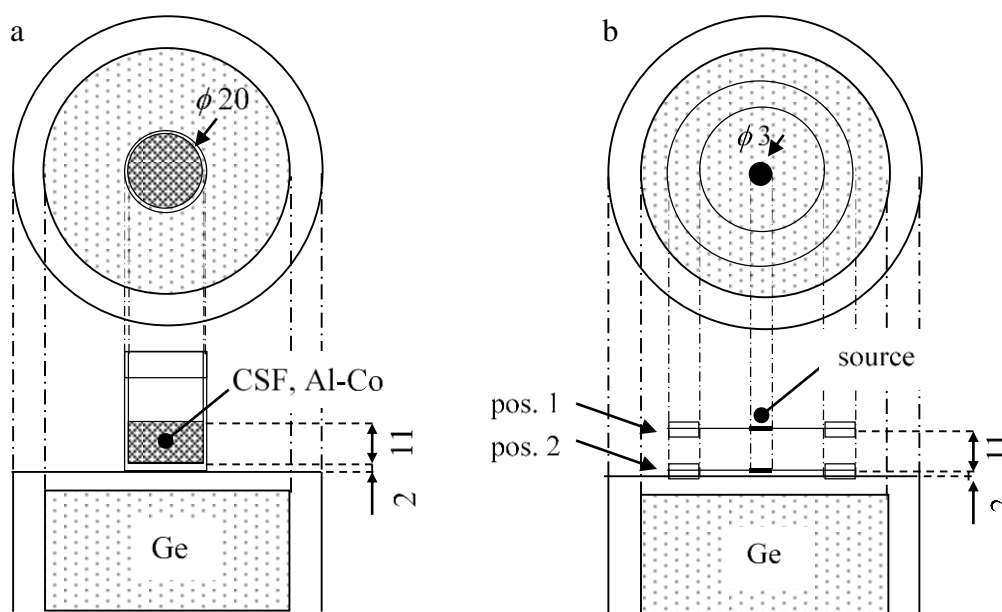
160 **Fig 1** Position of the lyophilized CSF sample and of the Al-Co wire during the
161 irradiation. Dimensions in mm

162 *Gamma spectrometry*

163 After irradiation, the lyophilized CSF sample was moved from its vial to a new 10 mL PE
164 vial and **weighed**; the mass, m_a , **was found** to be 240.00(5) mg, corresponding to 23.81(28)
165 mL volume of reconstituted CSF in the case of negligible effect due **to** humidity. The
166 relative loss of sample was about 20%, probably due to the lyophilized CSF residuals in
167 the vials. The Al-Co wire was removed from its micro-tube, placed in a new 10 mL vial
168 and dissolved using a few drops of nitric and hydrochloric acid (1:1) solution. After
169 complete digestion, water was added to obtain the same volume **as** the lyophilized CSF
170 sample.

171 The γ -spectra were recorded with a high purity germanium (HPGe) detector, ORTEC
172 GEM50P4-83 (relative efficiency 50%, resolution 1.90 keV at 1332 keV) inside a low-
173 background graded shield. The detector was connected to a digital signal processor ORTEC
174 DSPEC 502 and the data were collected and processed using the ORTEC Gamma Vision
175 software (version 6.08). The acquisition was performed in extended live-time correction
176 mode using the Gedcke-Hale method with pulse pile-up rejection in automatic set
177 threshold; the **excess counting loss** constant of the detection system, $\mu = 0.0445(5)$, was
178 recently measured [13].

179 The position of the lyophilized CSF and dissolved Al-Co wire samples with respect to the
 180 detector end-cap is shown in Figure 2a.



181 **Fig 2** Position of the lyophilized CSF and dissolved Al-Co wire samples (a), and of the
 182 disk source (b) with respect to the detector end-cap. Dimensions in mm

183 The collection of the γ -spectrum emitted by the CSF sample started at $t_{d a} =$
 184 667.890(10) h, lasted $t_{c a} = 359.0633(1)$ h and ended with a live time $t_{l a} =$
 185 351.1856(1) h. The dissolved Al-Co monitor was successively measured. The collection
 186 of the γ -spectrum started at $t_{d m} = 1034.10(1)$ h, lasted $t_{c m} = 797.0(3)$ s and ended with
 187 a live time $t_{l m} = 740.0(3)$ s. The quoted uncertainties correspond to uniform probability
 188 distributions assigned to the t_d , t_c and t_l values and having 60 s, 0.5 s and 0.5 s half-widths,
 189 respectively.

190 **Detection system characterization**

191 *Full-energy γ -peak detection efficiency*

192 The $\varepsilon_p^{\text{geo}}$ values in (5) depend on the actual position and geometry of the measured samples.
193 The dependence is strengthened when extensive samples are measured close to the detector
194 end-cap, as in this case.

195 In principle, the reconstruction of the $\varepsilon_p^{\text{geo}}$ versus the γ -energy, E_γ , might be performed by
196 measuring the γ -emissions of an extensive standard source having the same shape as the
197 analyte and monitor sample and located at the same position with respect to the detector
198 end-cap. In addition, the material of the source should have the same major elemental
199 composition as the monitor and analyte sample in order to mimic the γ self-absorption.

200 Actually, a more flexible procedure based on a computational technique coupled to a quasi-
201 point standard source measured at large source-detector distance is commonly adopted
202 [16]; geometries and major elemental composition of sample and layers between the Ge
203 crystal and sample are required.

204 As an approximated alternative, we recorded two γ -spectra with a disk standard source
205 positioned at the vertical ends of the measured extended samples, as shown in Figure 2b.
206 The efficiency of the (virtual) extensive source, $\varepsilon_p^{\text{ext}}$, was estimated by the average of the
207 disk efficiencies in positions 1 and 2, $\varepsilon_{p \text{ pos1}}^{\text{disk}}$ and $\varepsilon_{p \text{ pos2}}^{\text{disk}}$, respectively.

208 The coincidence free γ -emissions selected to reconstruct the efficiency curves were ^{241}Am
209 59.54 keV, ^{109}Cd 88.03 keV, ^{57}Co 122.06 keV, ^{139}Ce 165.86 keV, ^{113}Sn 391.70 keV, ^{137}Cs
210 661.66 keV, ^{54}Mn 834.85 keV and ^{65}Zn 1115.54 keV.

211 The $\varepsilon_{p \text{ pos1}}^{\text{disk}}$, $\varepsilon_{p \text{ pos2}}^{\text{disk}}$ and $\varepsilon_p^{\text{ext}}$ versus E_γ data were fitted by the equation model

$$212 \quad \ln \varepsilon_p = a_1 E_\gamma + a_0 + a_{-1} E_\gamma^{-1} + a_{-2} E_\gamma^{-2} + a_{-3} E_\gamma^{-3}, \quad (6)$$

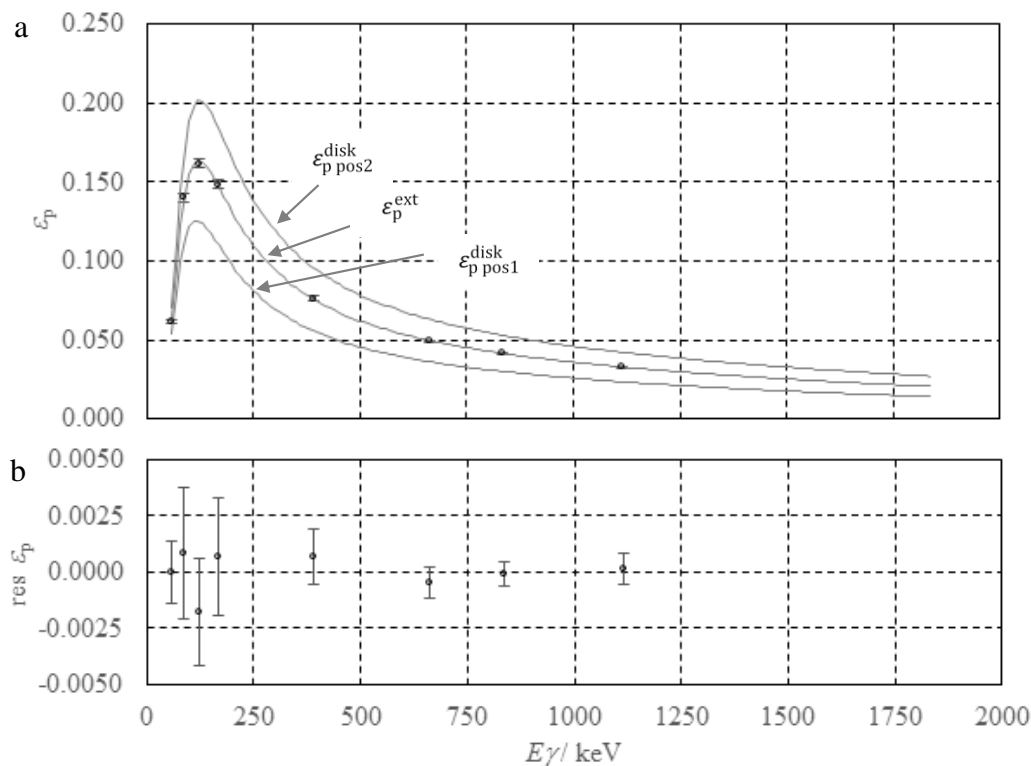
213 where a_1 , a_0 , a_{-1} , a_{-2} and a_{-3} are the fitting parameters. Best values, including
214 uncertainties and correlation matrix, were calculated using the algorithm implemented in
215 the OriginPro 2017.

216 The values obtained with the $\varepsilon_p^{\text{ext}}$ data were $a_1 = -4.72(43) \times 10^{-1} \text{ MeV}^{-1}$, $a_0 =$
 217 $-3.229(57)$, $a_{-1} = 4.03(20) \times 10^{-1} \text{ MeV}$, $a_{-2} = -3.20(22) \times 10^{-2} \text{ MeV}^2$, $a_{-3} =$
 218 $-5.73(75) \times 10^{-4} \text{ MeV}^3$; the corresponding correlation matrix is shown in Table 1.

219 **Table 1** Correlation matrix of the fitting
 220 parameters obtained with the $\varepsilon_p^{\text{ext}}$ data

	a_1	a_0	a_{-1}	a_{-2}	a_{-3}
a_1	1.000	-0.973	0.884	-0.804	0.748
a_0	-0.973	1.000	-0.957	0.896	-0.848
a_{-1}	0.884	-0.957	1.000	-0.984	0.957
a_{-2}	-0.804	0.896	-0.984	1.000	-0.993
a_{-3}	0.748	-0.848	0.957	-0.993	1.000

221 The $\varepsilon_{p \text{ pos1}}^{\text{disk}}$, $\varepsilon_{p \text{ pos2}}^{\text{disk}}$ and $\varepsilon_p^{\text{ext}}$ versus E_γ curves and the $\varepsilon_p^{\text{ext}}$ residuals are plotted in Figure 3a
 222 and Figure 3b, respectively. The error bars indicate a 95% confidence interval due to fitting,
 223 taking into account the correlations.



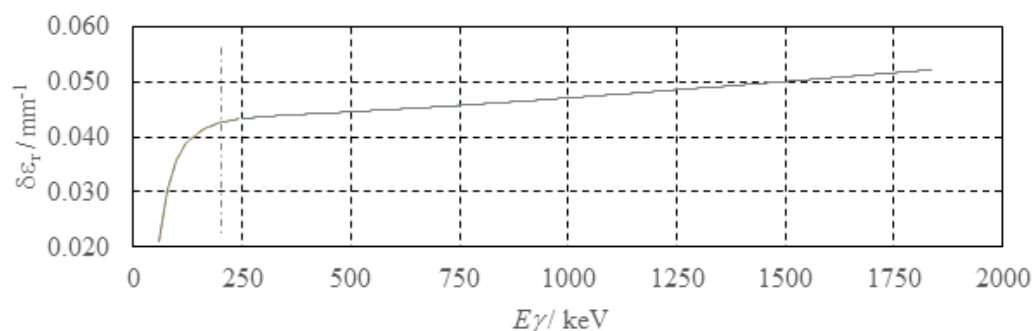
224 **Fig 3** $\varepsilon_{p \text{ pos2}}^{\text{disk}}$, $\varepsilon_p^{\text{ext}}$ and $\varepsilon_{p \text{ pos1}}^{\text{disk}}$ versus E_γ curves (a) and the residuals obtained with the $\varepsilon_p^{\text{ext}}$
 225 data (b). The error bars indicate a 95% confidence interval due to fitting

226 Possible differences in counting positions of the measured samples with respect to the
 227 (virtual) extensive source were considered according to:

$$228 \quad \frac{\varepsilon_{p\ m}^{\text{geo}}}{\varepsilon_{p\ a}^{\text{geo}}} = \frac{\varepsilon_{p\ m}^{\text{ext}} (1 - \delta\varepsilon_{r\ m} \Delta d_m)}{\varepsilon_{p\ a}^{\text{ext}} (1 - \delta\varepsilon_{r\ a} \Delta d_a)}, \quad (7)$$

229 where Δd_m and Δd_a are the vertical position differences between the dissolved Al-Co wire
 230 and the (virtual) extensive source and between the lyophilized CSF sample and the (virtual)
 231 extensive source, respectively, and $\delta\varepsilon_{r\ m}$ and $\delta\varepsilon_{r\ a}$ are the relative variations of the detection
 232 efficiency per unit of vertical position for the monitor and the analyte, respectively.

233 The $\delta\varepsilon_r$ values were obtained from the ratio of $(\varepsilon_{p\ \text{pos}2}^{\text{disk}} - \varepsilon_{p\ \text{pos}1}^{\text{disk}}) / \varepsilon_{p\ \text{ext}}^{\text{ext}}$ to the difference
 234 between the vertical positions 1 and 2, i.e. 11 mm, and plotted versus E_γ in Figure 4.



235

236 **Fig 4** $\delta\varepsilon_r$ versus E_γ curve. The vertical dashed line at about 240 keV splits the curve in
 237 two different regions

238 The data were fitted by $\delta\varepsilon_r = d_0 + d_1 E_\gamma$ and $\delta\varepsilon_r = e_0 + e_1 E_\gamma + e_2 E_\gamma^2 + e_3 E_\gamma^3 + e_4 E_\gamma^4$, for
 239 γ -energies above and below the 240 keV threshold, respectively. The resulting values were
 240 $e_4 = -7.10 \times 10^{-11} \text{ keV}^{-4}$, $e_3 = 5.19 \times 10^{-8} \text{ keV}^{-3}$, $e_2 = -1.43 \times 10^{-5} \text{ keV}^{-2}$, $e_1 =$
 241 $1.78 \times 10^{-3} \text{ keV}^{-1}$, $e_0 = -4.46 \times 10^{-2}$ and $d_1 = 5.56 \times 10^{-6} \text{ keV}^{-1}$, $d_0 = 4.17 \times$
 242 10^{-2} .

243 *Peak-to-total ratio*

244 True-coincidence occurs when two or more cascading γ -photons are emitted with
245 negligible time delay by a radionuclide. The effect becomes significant when samples are
246 measured close to the detector end-cap.

247 The number of counts collected in the full-energy γ -peak, n_p , is adjusted using the
248 correction factor

$$249 \quad \text{COI} = (1 - L_\gamma)(1 + S_\gamma), \quad (8)$$

250 where L_γ and S_γ are the overall probabilities for coincidence loss and summing,
251 respectively [4].

252 The formulae adopted to calculate L_γ and S_γ values depend on the cascade schemes and
253 include several nuclear parameters, the most important ones being the absolute emission
254 probability of the γ -photons, P_γ , the branching ratio, a_γ , and the total internal conversion
255 coefficient, α_t . In addition, $\varepsilon_p^{\text{geo}}$ and the peak-to-total ratio, P/T , of the detection system
256 are required.

257 E.g., the probability for coincidence loss of γ_A and γ_B in the case of $\gamma_A \rightarrow \gamma_B$ decay scheme
258 is

$$259 \quad L_{\gamma_A} = a_{\gamma_B} c_{\gamma_B} \frac{\varepsilon_p^{\text{geo}}}{(P/T)_{\gamma_B}} \quad \text{and} \quad L_{\gamma_B} = \frac{P_{\gamma_A}}{P_{\gamma_B}} a_{\gamma_B} c_{\gamma_B} \frac{\varepsilon_p^{\text{geo}}}{(P/T)_{\gamma_A}}, \quad (9)$$

260 respectively, where $c_\gamma = 1/(1 + \alpha_{t\gamma})$, whereas the probability for coincidence summing
261 of γ_A with the $\gamma_B \rightarrow \gamma_C$ decay scheme is

$$262 \quad S_{\gamma_A} = \frac{P_{\gamma_B}}{P_{\gamma_A}} a_{\gamma_C} c_{\gamma_C} \frac{\varepsilon_p^{\text{geo}}}{\varepsilon_p^{\text{geo}}} \frac{\varepsilon_p^{\text{geo}}}{\varepsilon_p^{\text{geo}}}. \quad (10)$$

263 A compilation of the nuclear parameters values and the cascade schemes concerning the
264 radionuclides generally used in NAA are reported in [4].

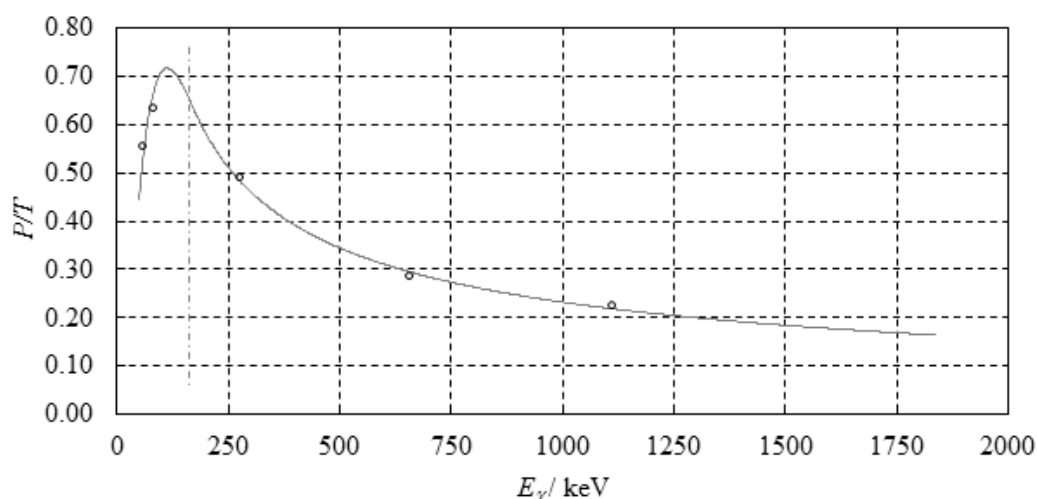
265 Similar to $\varepsilon_p^{\text{geo}}$, the P/T ratio versus E_γ data can be ideally obtained from γ -spectra of
266 coincidence free radionuclides embedded in extensive sources having the same material

267 and shape as the analyte and monitor sample and located at the same position with respect
268 to the detector end-cap. In practice, since the P/T ratio is above all depending on the
269 position and to a smaller extent on the composition and geometry of the samples, use of
270 quasi-point γ -sources might be accepted.

271 In this study, we used five γ -emissions, i.e. ^{241}Am 59.54 keV, ^{170}Tm 84.25 keV, ^{203}Hg
272 279.19 keV, ^{137}Cs 661.66 keV and ^{65}Zn 1115.54 keV, to reconstruct the P/T ratio curve.

273 The data were fitted by $\log P/T = b_0 + b_1 \log E_\gamma$ and $\log P/T = c_0 + c_1 \log E_\gamma +$
274 $c_2(\log E_\gamma)^2$, for γ -energies above and below the 170 keV threshold, respectively. To avoid
275 a discontinuity, the first derivative with respect to $\log E_\gamma$ of the latter equation model at
276 170 keV was imposed to be the b_1 value. The resulting values were $b_1 = -0.571$, $b_0 =$
277 1.079 , $c_2 = -1.625$, $c_1 = 6.678$ and $c_0 = -7.006$.

278 The P/T ratio versus E_γ curve is plotted in Figure 5.



279

280 **Fig 5** P/T ratio versus E_γ curve. The vertical dashed line at about 170 keV splits the
281 curve in two different regions

282 Results and discussion

283 The analysis of the γ -spectrum of the lyophilized CSF sample pointed out ^{233}Pa , ^{51}Cr , ^{131}Ba ,
284 ^{124}Sb , ^{46}Sc , ^{86}Rb , ^{59}Fe , ^{65}Zn and ^{60}Co γ -emissions produced by neutron capture reactions

285 from ^{232}Th , ^{50}Cr , ^{130}Ba , ^{123}Sb , ^{45}Sc , ^{85}Rb , ^{58}Fe , ^{64}Zn and ^{59}Co . The mass concentrations of
 286 the corresponding elements were quantified using the ^{60}Co γ -emission of the monitor.

287 The number of counts collected in the γ -peaks were evaluated with the algorithm
 288 implemented in the ROI32 analysis engine of the Gamma Vision software. The γ -peak
 289 energies and n_p values of the detected radionuclides in the CSF sample and monitor are
 290 reported in Table 2; the uncertainty (conservatively) assigned to E_γ corresponds to a
 291 uniform distribution with 0.2 keV half-width whereas the n_p uncertainty is due to counting
 292 statistics, including background.

293 **Table 2** γ -peak energies and corresponding number
 294 of counts of the detected radionuclides

Radionuclide	E_γ / keV	$n_p / 1$
$^{233}\text{Pa}^{(\text{CSF})}$	311.90(12)	$1.017(24) \times 10^5$
$^{51}\text{Cr}^{(\text{CSF})}$	320.10(12)	$5.26(15) \times 10^4$
$^{131}\text{Ba}^{(\text{CSF})}$	496.30(12)	$5.08(12) \times 10^4$
$^{124}\text{Sb}^{(\text{CSF})}$	1691.00(12)	$2.47(21) \times 10^2$
$^{46}\text{Sc}^{(\text{CSF})}$	889.30(12)	$1.3070(80) \times 10^5$
$^{86}\text{Rb}^{(\text{CSF})}$	1077.00(12)	$4.56(44) \times 10^3$
$^{59}\text{Fe}^{(\text{CSF})}$	1099.30(12)	$9.46(59) \times 10^3$
$^{65}\text{Zn}^{(\text{CSF})}$	1115.50(12)	$1.2260(47) \times 10^5$
$^{60}\text{Co}^{(\text{CSF})}$	1173.20(12)	$4.68(44) \times 10^3$
$^{60}\text{Co}^{(\text{monitor})}$	1173.20(12)	$1.3749(44) \times 10^5$

295 The full-energy γ -peak detection efficiencies ratio, $\varepsilon_{p\ m}^{\text{geo}}/\varepsilon_{p\ a}^{\text{geo}}$, was computed according to
 296 (7) using $a_1, a_0, a_{-1}, a_{-2}, a_{-3}$ and $d_1, d_0, e_0, e_1, e_2, e_3, e_4$ to obtain $\varepsilon_{p\ m}^{\text{ext}}/\varepsilon_{p\ a}^{\text{ext}}$ and $\delta\varepsilon_r$,
 297 respectively, as a function of E_γ . The uncertainty of the $\varepsilon_{p\ m}^{\text{ext}}/\varepsilon_{p\ a}^{\text{ext}}$ was evaluated taking into
 298 account uncertainties and correlations of the fitting parameters whereas a uniform
 299 probability distribution with a (conservative) 20% relative half-width was directly assigned
 300 to the $\delta\varepsilon_r$ value. In addition, it was assumed that the vertical position of the samples was
 301 within ± 0.5 mm with respect to the (virtual) extensive γ -source; accordingly, $\Delta d_m = \Delta d_a =$
 302 $0.00(29)$ mm, the quoted uncertainty corresponding to a uniform probability distribution
 303 having 0.5 mm half-width.

304 The true-coincidence correction factors ratio, COI_m/COI_a , was obtained via (8) using b_0 ,
 305 b_1 , c_0 , c_1 and c_2 to determine P/T as a function of E_γ . A uniform probability distribution
 306 with a (conservative) 20% relative half-width was directly assigned to the P/T value. The
 307 effect due to possible differences in counting positions was neglected; specifically, ε_p^{geo}
 308 was used instead of ε_p^{ext} in (9) and (10). Cascade schemes, notations and P_γ , a_γ , α_t values
 309 proposed in [4] were adopted with uncertainties corresponding to uniform probability
 310 distributions having 0.0002, 0.02 and 0.02 half-widths, respectively.

311 A list of neutron capture reactions and $t_{1/2}$, k_{0Au} , Q_0 , \bar{E}_r values recommended in the k_0
 312 database [14] and used in this study are reported in Table 3 for reader's convenience.

313 **Table 3** Neutron capture reactions and adopted $t_{1/2}$, k_{0Au} , Q_0 , \bar{E}_r values.

Reaction	$t_{1/2}$ / h	k_{0Au} / 1	Q_0 / 1	\bar{E}_r / eV
$^{232}\text{Th}(n,\gamma)^{233}\text{Pa}$	647.280(48)	$2.520(13) \times 10^{-2}$	11.50(41)	54.40(49)
$^{50}\text{Cr}(n,\gamma)^{51}\text{Cr}$	664.800(58)	$2.620(13) \times 10^{-3}$	0.53(11)	$753(83) \times 10^1$
$^{130}\text{Ba}(n,\gamma)^{131}\text{Ba}$	276.0(14)	$6.480(13) \times 10^{-5}$	24.8(50)	69.9(35)
$^{123}\text{Sb}(n,\gamma)^{124}\text{Sb}$	1444.80(72)	$1.410(16) \times 10^{-2}$	28.8(11)	28.2(18)
$^{45}\text{Sc}(n,\gamma)^{46}\text{Sc}$	2011.92(48)	1.2200(49)	0.430(86)	$513(87) \times 10^1$
$^{85}\text{Rb}(n,\gamma)^{86}\text{Rb}$	447.12(48)	$7.650(77) \times 10^{-4}$	14.80(37)	839(50)
$^{58}\text{Fe}(n,\gamma)^{59}\text{Fe}$	1068.00(14)	$7.770(39) \times 10^{-5}$	0.975(10)	$64(15) \times 10^1$
$^{64}\text{Zn}(n,\gamma)^{65}\text{Zn}$	5863.2(24)	$5.720(23) \times 10^{-3}$	1.91(10)	$256(26) \times 10^1$
$^{59}\text{Co}(n,\gamma)^{60}\text{Co}$	46207.2(72)	1.3200(53)	1.993(60)	136.0(69)

314 Values and uncertainties assigned to t_i , t_{da} , t_{ca} , t_{la} , t_{dm} , t_{cm} , t_{lm} , μ , f , α , m_a , m_m , w_m
 315 and v are given in the section 3. The thermal and epithermal neutron self-shielding of the
 316 lyophilized CSF sample and of the dissolved (and diluted) Co monitor were considered
 317 insignificant. Accordingly, $G_{thm} = G_{tha} = G_{em} = G_{ea} = 1.000$ with negligible
 318 uncertainty.

319 *Uncertainty budget*

320 The spreadsheet technique was applied to set up the uncertainty budget of the analyte mass
 321 concentration, ρ_a , via the measurement model (5).

322 The input quantities for ρ_a were $t_i, \mu, t_{1/2 a}, t_{1/2 m}, t_{d a}, t_{c a}, t_{l a}, t_{d m}, t_{c m}, t_{l m}, n_{p a}, n_{p m},$
323 $k_{0 Au}(a), k_{0 Au}(m), G_{th a}, G_{e a}, G_{th m}, G_{e m}, f, \alpha, Q_{0 a}, \bar{E}_{r a}, Q_{0 m}, \bar{E}_{r m}, \varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}, COI_m/COI_a,$
324 m_m, m_a, w_m and v . The intermediate quantities $\lambda_a, \lambda_m, \delta_a, \delta_m, \xi_a, \xi_m, Q_{0 a}(\alpha)$ and $Q_{0 m}(\alpha)$
325 were calculated for information.

326 For simplicity, the $\varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}$ and COI_m/COI_a values and uncertainties were computed
327 separately via the measurement models (7) and (8), respectively. The input quantities for
328 $\varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}$ were $a_1, a_0, a_{-1}, a_{-2}, a_{-3}, E_{\gamma m}, E_{\gamma a}, \Delta d_a, \Delta d_m, \delta\varepsilon_{r a}$ and $\delta\varepsilon_{r m}$ while the input
329 quantities for COI_m/COI_a were $a_1, a_0, a_{-1}, a_{-2}, a_{-3}$ and additional parameters depending
330 on the cascade scheme, e.g. $E_{\gamma}, a_{\gamma}, c_{\gamma}, P/T$ and P_{γ} either for the monitor and for the analyte.
331 The quantities $e_4, e_3, e_2, e_1, e_0, d_1$ and d_0 used to compute $\delta\varepsilon_r$ and the quantities $b_1, b_0,$
332 c_2, c_1 and c_0 used to compute P/T were given for information. The (small) correlation
333 effect due to the shared parameters a_1, a_0, a_{-1}, a_{-2} and a_{-3} was neglected.

334 The formulae were implemented in a MS excel file [17] consisting of nine worksheets, one
335 for each quantified analyte. A single worksheet included four sections. Irradiation time,
336 day and time of the irradiation end, day and time of the γ -counting start, outputs of the
337 Gamma Vision software, target nuclide and produced radionuclide were given in the first
338 section, called “Irradiation and γ -spectrometry”. Values, standard uncertainties and
339 correlation coefficients of the input quantities were added in the main section, called
340 “Uncertainty budget of ρ_a ”, with the exception of the $\varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}$ and COI_m/COI_a ratios,
341 whose data were added and calculated in two sub-sections, called “Uncertainty budget of
342 $\varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}$ ” and “Uncertainty budget of COI_m/COI_a ”, respectively.

343 Values and combined uncertainties of $\rho_a, \varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}$ and COI_m/COI_a were calculated
344 together with sensitivity coefficients of the input quantities and their relative contribution;
345 the matrix formalism was used to propagate the uncertainties via the correlation matrices
346 $R_{\rho_a}, R_{\varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}}$ and R_{COI_m/COI_a} .

347 The analysis quantified $2.32(11) \times 10^{-10}$ g mL⁻¹ of Th, $2.096(99) \times 10^{-9}$ g mL⁻¹ of Cr,
348 $6.89(96) \times 10^{-8}$ g mL⁻¹ of Ba, $4.01(39) \times 10^{-11}$ g mL⁻¹ of Sb, $5.06(15) \times 10^{-11}$ g mL⁻¹ of Sc,

349 $8.00(85) \times 10^{-10}$ g mL⁻¹ of Rb, $3.87(27) \times 10^{-8}$ g mL⁻¹ of Fe, $2.220(77) \times 10^{-8}$ g mL⁻¹ of Zn
350 and $3.24(31) \times 10^{-11}$ g mL⁻¹ of Co.

351 The uncertainty budgets are given in the developed MS excel file available in the
352 Supplementary Information; cells dealing with informative or intermediate data were
353 grayed. In $R_{\varepsilon_{p m}^{\text{geo}}/\varepsilon_{p a}^{\text{geo}}}$ and $R_{\text{COI}_m/\text{COI}_a}$, we set the correlation coefficients of a_1, a_0, a_{-1}, a_{-2}
354 and a_{-3} according to the data shown in Table 1; in addition, as a first attempt, in $R_{\varepsilon_{p m}^{\text{geo}}/\varepsilon_{p a}^{\text{geo}}}$,
355 we set to the unity value the correlation between $\delta\varepsilon_{r a}$ and $\delta\varepsilon_{r m}$, and in $R_{\text{COI}_m/\text{COI}_a}$, we set
356 to the unity value the correlation between P/T_γ values, if existing.

357 A survey of the main contributors to the combined uncertainties is given in Table 4 while
358 the (complete) Cr budget is shown in the Supplementary Information.

359 **Table 4** Main contributors to the combined uncertainty of the quantified elements. Input
360 quantities, X_i , are explained in the text. The index I is the relative contribution of X_i

Th		Cr		Ba		Sb		Sc		Rb		Fe		Zn		Co	
X_i	I / %	X_i	I / %	X_i	I / %	X_i	I / %	X_i	I / %	X_i	I / %	X_i	I / %	X_i	I / %	X_i	I / %
$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	26.7	$n_{p a}$	35.3	$Q_{0 a}$	89.3	$n_{p a}$	77.6	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	49.3	$n_{p a}$	83.4	$n_{p a}$	78.0	$\frac{\text{COI}_m}{\text{COI}_a}$	33.1	$n_{p a}$	92.8
$n_{p a}$	25.1	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	27.4	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	3.2	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	8.0	v	16.0	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	3.5	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	7.9	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	32.6	$\frac{\varepsilon_{p m}^{\text{geo}}}{\varepsilon_{p a}^{\text{geo}}}$	4.1
$\frac{\text{COI}_m}{\text{COI}_a}$	16.1	$\frac{\text{COI}_m}{\text{COI}_a}$	17.6	$n_{p a}$	2.9	$Q_{0 a}$	6.6	w_m	10.9	$\frac{\text{COI}_m}{\text{COI}_a}$	3.5	$\frac{\text{COI}_m}{\text{COI}_a}$	6.9	v	12.3		
$Q_{0 a}$	12.0	v	6.5					$Q_{0 a}$	5.8					w_m	8.4		
v	6.4	w_m	4.5					$n_{p a}$	4.1					$Q_{0 a}$	4.1		

361 In summary, the uncertainty of the results was largely due to $\varepsilon_{p m}^{\text{geo}}/\varepsilon_{p a}^{\text{geo}}$, $n_{p a}$ and
362 $\text{COI}_m/\text{COI}_a$. In a few cases, v , w_m and m_m had an influence while the 20% uncertainty of
363 the $Q_{0 a}$ recommended in the k_0 database [14] had the overriding effect for the
364 determination of Ba.

365 It is worth to observe that the contribution to $\varepsilon_{p m}^{\text{geo}}/\varepsilon_{p a}^{\text{geo}}$ due to possible differences in
366 counting positions of samples could be canceled if the monitor element was embedded in

367 the analyte sample [18, 19]; this was confirmed by setting the correlation coefficient
368 between Δd_a and Δd_m in $R_{\varepsilon_{p m}^{\text{geo}}/\varepsilon_{p a}^{\text{geo}}}$ to the unity value.

369 Besides, the result of Co deserves attention. In this case, i.e. when the analyte corresponds
370 to the monitor element and the same γ -emission is used, the k_0 -NAA turns into the relative-
371 NAA. Accordingly, we set to the unity value the correlation coefficients between $t_{1/2}$, $t_{1/2}$,
372 $k_{0 \text{ Au}}$, Q_0 and \bar{E}_r in R_{ρ_a} and between E_γ , a_γ , c_γ , P/T_γ in $R_{\text{COI}_m/\text{COI}_a}$. As a result, the
373 contributions due to the “intrinsic” uncertainty characteristic of the k_0 -NAA method [8]
374 and due to the $\text{COI}_m/\text{COI}_a$ were reset; moreover, the correlation coefficients of a_1 , a_0 , a_{-1} ,
375 a_{-2} and a_{-3} in $R_{\varepsilon_{p m}^{\text{geo}}/\varepsilon_{p a}^{\text{geo}}}$ made their contribution to $\varepsilon_{p m}^{\text{ext}}/\varepsilon_{p a}^{\text{ext}}$ zero as well.

376 **Conclusions**

377 The spreadsheet approach proved to be suitable to set up the uncertainty budget for the k_0 -
378 standardisation method in NAA when the majority of the recognized sources of error are
379 considered and the measurement model is written to limit the correlations between input
380 quantities. The use of the matrix formalism was straightforward to propagate the
381 uncertainties by taking into account the covariances.

382 A MS excel file was developed and tested for the determination of Th, Cr, Ba, Sb, Sc, Rb,
383 Fe, Zn and Co in a lyophilized CSF sample. The uncertainty budget of each element was
384 compiled once the estimates, the uncertainties and the correlation coefficients associated
385 with the input quantities were specified. The value and combined uncertainty of the result
386 were calculated and the most overriding contributors were pointed out.

387 It was shown that when the monitor element corresponded to the analyte element and the
388 same γ -emission was used, the worksheet set up the uncertainty budget for the relative-
389 NAA method; this makes the proposed approach applicable either in the relative- and k_0 -
390 NAA.

391 The MS excel file is open and free available to users. The implemented measurement model
392 allows a broad application, e.g. in case of different sample material, monitor element,

393 neutron irradiation and γ -spectrometry conditions. The extension to other elements is
394 possible by a simple duplication of the existing worksheets; only the modification of the
395 formulae adopted to compute the COI_m/COI_a ratio might be required for other decay
396 schemes.

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440

Supplementary information441 *Developed worksheet file*

442 See the MS excel file “uncertainty_k0_spreadsheet.xlsx”

443 *Uncertainty budget of Cr*

444 The (complete) uncertainty budget of the Cr determination is here reported. According to
 445 Table 1, the most overriding contributors to the combined uncertainty were n_{p_a} (35.3%),
 446 $\varepsilon_{p_m}^{\text{geo}}/\varepsilon_{p_a}^{\text{geo}}$ (27.4%) and $\text{COI}_m/\text{COI}_a$ (17.6%). The remaining 19.7% was due to v , w_m ,
 447 $Q_{0_a}, m_m, k_{0_{\text{Au}}(a)}, k_{0_{\text{Au}}(m)}, Q_{0_m}, n_{p_m}, \alpha$ and f , in decreasing order of importance. As
 448 regards to $\varepsilon_{p_m}^{\text{geo}}/\varepsilon_{p_a}^{\text{geo}}$ (see Table 2), the main contributors were a_1, a_{-1}, a_{-2} (44.0%), Δd_a
 449 (25.6%) and Δd_m (31.5%), while the uncertainty of $\text{COI}_m/\text{COI}_a$ (see Table 3) was due to
 450 $P/T_{\gamma 2m}$ (96.1%).

451 The a_0 value is not affecting $\varepsilon_{p_m}^{\text{geo}}/\varepsilon_{p_a}^{\text{geo}}$. In fact, a_0 in equation (6) models a constant
 452 multiplying factor that is deleted from the detection efficiency ratio. In addition, since we
 453 considered $\Delta d_a = \Delta d_m = 0$ mm, the contribution of $\delta\varepsilon_{r_a}$ and $\delta\varepsilon_{r_m}$ was reset.

454 **Table 1** Uncertainty budget of the mass concentration of Cr in
 455 the lyophilized CSF sample. Quantities are explained in the text.
 456 The column Index gives the relative contribution of the input
 457 quantity, X_i , to the output quantity, Y . Values of the sensitivity
 458 coefficient, c_i , and Index are omitted for those quantities that are
 459 not actual inputs of the measurement model.

Quantity X_i	Unit [X_i]	Value x_i	Std. Uncertainty $u(x_i)$	Sens. Coeff. c_i	Index I / %
t_i	s	2.1600×10^4	1.7×10^1	3.0×10^{-16}	0.0
μ	1	4.45×10^{-2}	5×10^{-4}	-1.0×10^{-10}	0.0
$t_{1/2 a}$	s	2.39328×10^6	2.1×10^2	1.1×10^{-16}	0.0
λ_a	s ⁻¹	2.89622×10^{-7}	2.5×10^{-11}		
$t_{1/2 m}$	s	1.66346×10^8	2.6×10^4	-1.2×10^{-17}	0.0
λ_m	s ⁻¹	4.16690×10^{-9}	6.5×10^{-13}		
$t_{d a}$	s	2.404405×10^6	3.5×10^1	6.1×10^{-16}	0.0

$t_{c a}$	s	1.29262800×10^6	2.9×10^{-1}	3.6×10^{-16}	0.0
$t_{l a}$	s	1.26426800×10^6	2.9×10^{-1}	-1.7×10^{-15}	0.0
$t_{d m}$	s	3.722775×10^6	3.5×10^1	-8.7×10^{-18}	0.0
$t_{c m}$	s	7.9700×10^2	2.9×10^{-1}	-1.1×10^{-13}	0.0
$t_{l m}$	s	7.400×10^2	2.9×10^{-1}	2.9×10^{-12}	0.0
δ_a	1	1.022	0.000		
δ_m	1	1.077	0.001		
ξ_a	1	1.00098	1×10^{-5}		
ξ_m	1	1.00319	4×10^{-5}		
$n_{p a}$	1	5.26×10^4	1.5×10^3	4.0×10^{-14}	35.3
$n_{p m}$	1	1.3749×10^5	4.4×10^2	-1.5×10^{-14}	0.5
$k_{0 Au(a)}$	1	2.620×10^{-3}	1.3×10^{-5}	-8.0×10^{-7}	1.1
$k_{0 Au(m)}$	1	1.3200	5.3×10^{-3}	1.6×10^{-9}	0.7
$G_{th a}$	1	1.000	0.000	-2.0×10^{-9}	0.0
$G_{e a}$	1	1.000	0.000	-7.7×10^{-11}	0.0
$G_{th m}$	1	1.000	0.000	1.8×10^{-9}	0.0
$G_{e m}$	1	1.000	0.000	2.7×10^{-10}	0.0
f	1	1.560×10^1	3.3×10^{-1}	-1.2×10^{-11}	0.2
α	1	-3.60×10^{-2}	6.4×10^{-3}	-9.0×10^{-10}	0.3
$Q_{0 a}$	1	5.3×10^{-1}	1.1×10^{-1}	-1.8×10^{-10}	3.6
$\bar{E}_{r a}$	eV	7.53×10^3	8.3×10^2	-8.7×10^{-17}	0.0
$Q_{0 a}(\alpha)$	1	5.9×10^{-1}	1.5×10^{-1}		
$Q_{0 m}$	1	1.993	6.0×10^{-2}	1.4×10^{-10}	0.7
$\bar{E}_{r m}$	eV	1.360×10^2	6.9	5.8×10^{-14}	0.0
$Q_{0 m}(\alpha)$	1	2.319	9.5×10^{-2}		
$\varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}$	1	3.507×10^{-1}	8.7×10^{-3}	6.0×10^{-9}	27.4
COI_m/COI_a	1	8.57×10^{-1}	1.7×10^{-2}	2.4×10^{-9}	17.6
m_m	g	8.47×10^{-3}	5×10^{-5}	2.5×10^{-7}	1.6
m_a	g	2.4000×10^{-1}	5×10^{-5}	-8.7×10^{-9}	0.0
w_m	g g ⁻¹	4.597×10^{-3}	4.6×10^{-5}	4.6×10^{-7}	4.5
v	mg L ⁻¹	99.2	1.2	-2.1×10^{-11}	6.6
Y	[Y]	y	$u_c(y)$		
ρ_a	g mL ⁻¹	2.096×10^{-9}	9.9×10^{-11}		

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Table 2. Uncertainty budget of the $\varepsilon_{p m}^{geo}/\varepsilon_{p a}^{geo}$ ratio given in Table 1.

Quantity X_i	Unit [X_i]	Value x_i	Std. Uncertainty $u(x_i)$	Sens. Coeff. c_i	Index I / %
a_1	MeV ⁻¹	-4.72×10^{-1}	4.3×10^{-2}	3.0×10^{-1}	74.1

a_0	1	-3.229	5.7×10^{-2}	0.0	0.0
a_{-1}	MeV	4.03×10^{-1}	2.0×10^{-2}	-8.0×10^{-1}	-43.1
a_{-2}	MeV ²	3.20×10^{-2}	2.2×10^{-3}	-3.2	13.0
a_{-3}	MeV ³	5.73×10^{-4}	7.5×10^{-5}	-1.0×10^1	-1.1
$E_{\gamma m}$	MeV	1.17320	1.2×10^{-4}	-2.5×10^{-1}	0.0
$E_{\gamma a}$	MeV	3.2010×10^{-1}	1.2×10^{-4}	9.2×10^{-1}	0.0
Δd_a	mm	0.00	0.29	1.5×10^{-2}	25.6
Δd_m	mm	0.00	0.29	-1.7×10^{-2}	31.5
e_4	keV ⁻⁴	-7.10×10^{-11}	0.00×10^{-11}		
e_3	keV ⁻³	5.19×10^{-8}	0.00×10^{-8}		
e_2	keV ⁻²	-1.43×10^{-5}	0.00×10^{-5}		
e_1	keV ⁻¹	1.78×10^{-3}	0.00×10^{-3}		
e_0	1	-4.46×10^{-2}	0.00×10^{-2}		
d_1	keV ⁻¹	5.56×10^{-6}	0.00×10^{-6}		
d_0	1	4.17×10^{-2}	0.00×10^{-2}		
$\delta \varepsilon_{ra}$	mm ⁻¹	4.3×10^{-2}	5×10^{-3}	0.0	0.0
$\delta \varepsilon_{rm}$	mm ⁻¹	4.8×10^{-2}	6×10^{-3}	0.0	0.0
Y	[Y]	y	$u_c(y)$		
$\varepsilon_{pm}^{\text{geo}}/\varepsilon_{pa}^{\text{geo}}$	1	3.507×10^{-1}	8.7×10^{-3}		

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Table 3 Uncertainty budget of the $\text{COI}_m/\text{COI}_a$ ratio given in Table 1. (*) Notation reported in [4] and adopted for the cascade scheme.

Quantity X_i	Unit [X_i]	Value x_i	Std. Uncertainty $u(x_i)$	Sens. Coeff. c_i	Index I / %
a_1	MeV ⁻¹	-4.72×10^{-1}	4.3×10^{-2}	-1.9×10^{-1}	5.9
a_0	1	-3.229	5.7×10^{-2}	-1.4×10^{-1}	-4.9
a_{-1}	MeV	4.03×10^{-1}	2.0×10^{-2}	-1.1×10^{-1}	1.0
a_{-2}	MeV ²	3.20×10^{-2}	2.2×10^{-3}	-8.0×10^{-2}	-0.1
a_{-3}	MeV ³	5.73×10^{-4}	7.5×10^{-5}	-6.0×10^{-2}	0.0
b_1	1	-0.571	0.000		
b_0	1	1.079	0.000		
c_2	1	-1.625	0.000		
c_1	1	6.678	0.000		
c_0	1	-7.006	0.000		
$E_{\gamma 2m}$	keV	1.3325×10^3	1.2×10^{-1}	9.6×10^{-5}	0.0
$a_{\gamma 2m}$	1	1.000	0.012	-1.4×10^{-1}	0.9
$c_{\gamma 2m}$	1	1.000	0.012	-1.4×10^{-1}	0.9
$P/T_{\gamma 2m}$	1	0.197	0.023	7.3×10^{-1}	96.1

Y	$[Y]$	y	$u_c(y)$		
$\text{COI}_m/\text{COI}_a$	1	8.57×10^{-1}	1.7×10^{-2}		

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467 the webpage containing the electronic supplementary information will appear when one
468 clicks on the hyperlink. Here you can list the details of your research which would be too
469 long for the main text, *e.g.* a larger number of spectra *etc.* Start with 1 for Figure and Table
470 numbers in this section.